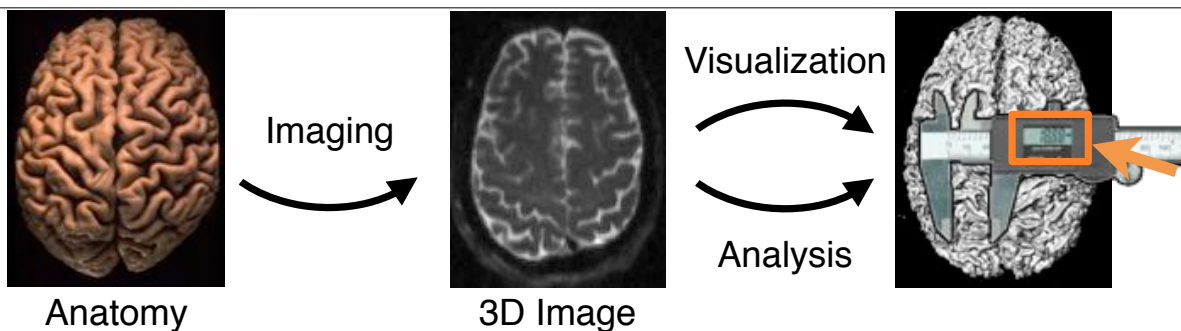


Optimizing Particle Systems for Image Feature Sampling

Gordon L. Kindlmann



Imaging as starting point for Computational Science



- Imaging measures whole 3D objects
- Examples: CT, MRI (functional, diffusion, etc)
- Imaging is a powerful way to detect & quantify biology
- Visualization → **pictures**, for seeing qualitative whole
 - e.g. Volume rendering
- Analysis → geometric **models**, for quantitative measurements
 - e.g. Segmentation, Classification, Feature Extraction
 - **This talk: Particle Systems for Feature Extraction**

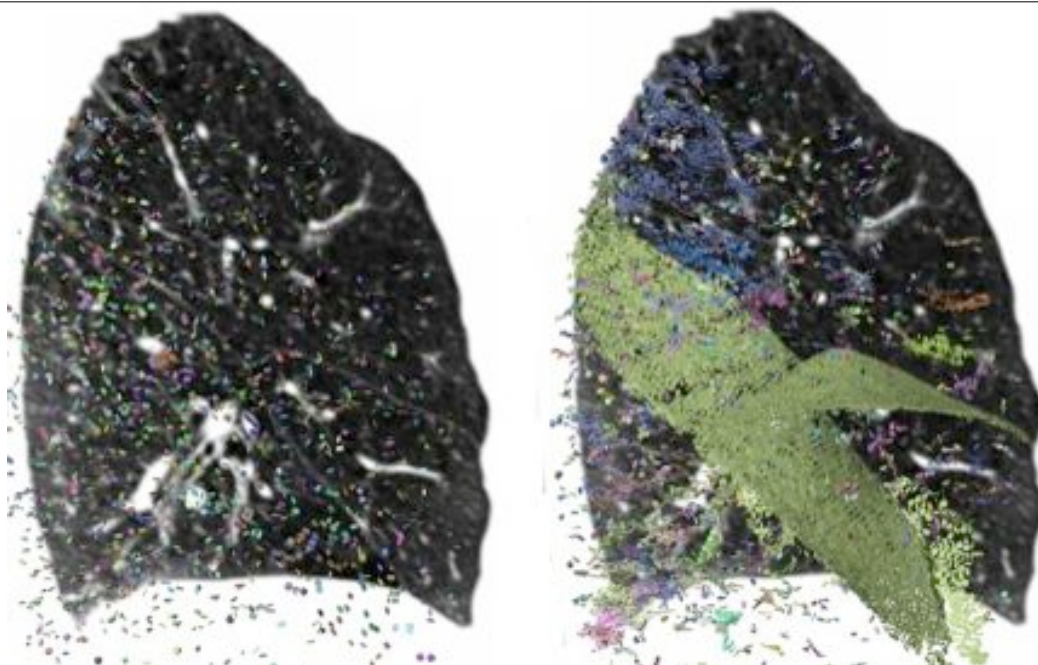
Outline

Please interrupt!

- Applications
 - Clinical Lung Studies (chest CT, Emphysema)
 - Brain Structure (diffusion MRI, white matter)
 - Zebrafish phenotyping (micro CT, eyes, etc)
- Method: Particle Systems for Features
 - Feature definition & extraction
 - Decomposition into Particles
 - System Optimization
- Particle System Economization
 - Decomposition of Costs
 - Parameter tuning, algorithmic tuning?

3

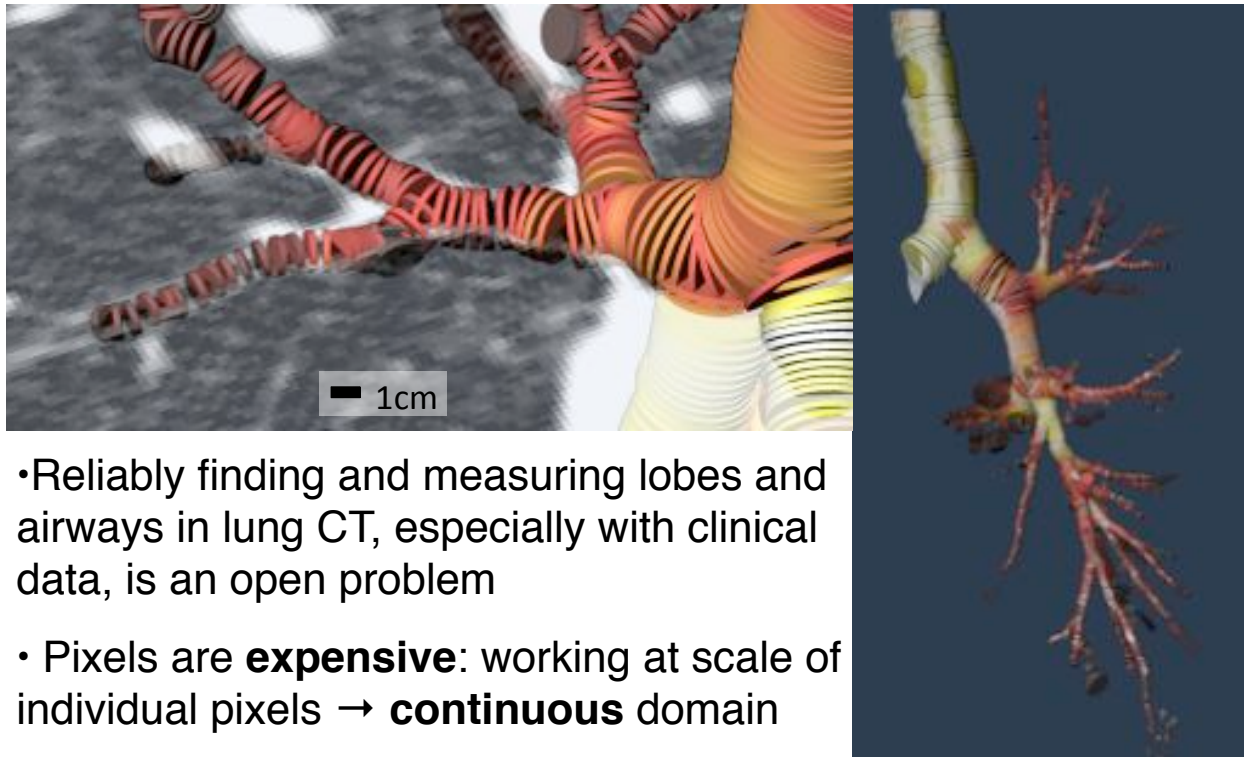
Lung lobes from clinical CT



J Ross, RSJ Estepar, G Kindlmann, A Diaz, C-F Westin, E Silverman, G Washko, "Automatic Lung Lobe Segmentation Using Particles, Thin Plate Splines, and Maximum a Posteriori Estimation", Proceedings MICCAI 2010, pp 163-171

4 (Applications)

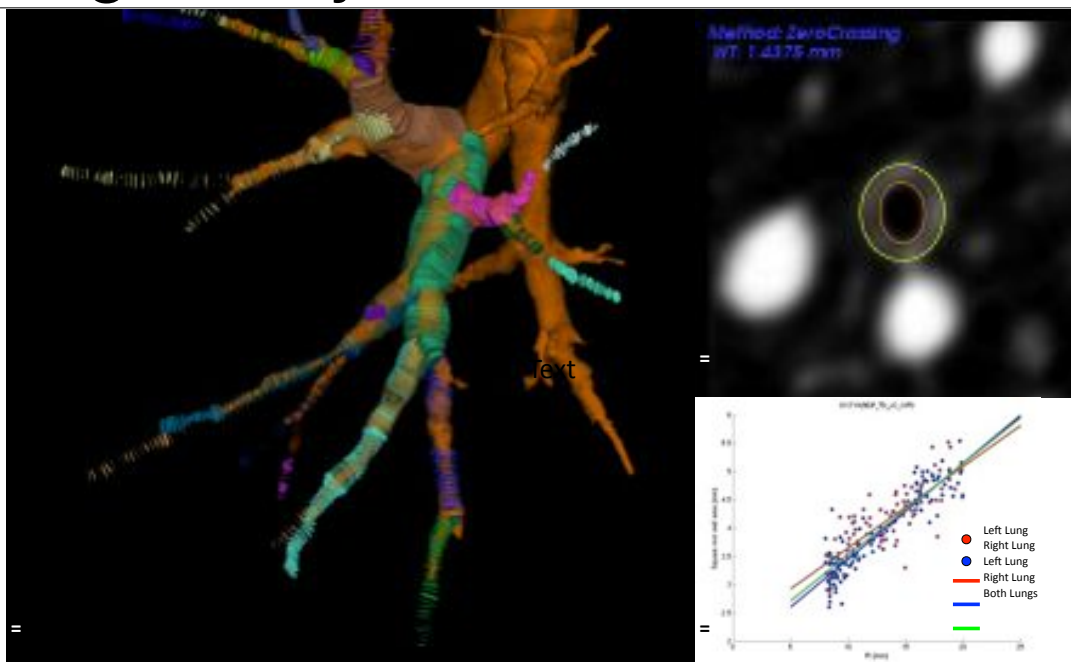
Lung airways from clinical CT



- Reliably finding and measuring lobes and airways in lung CT, especially with clinical data, is an open problem
- Pixels are **expensive**: working at scale of individual pixels → **continuous** domain

5 (Applications)

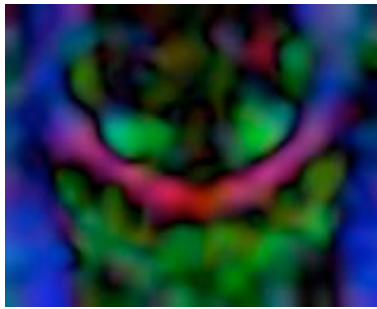
Lung airways from clinical CT



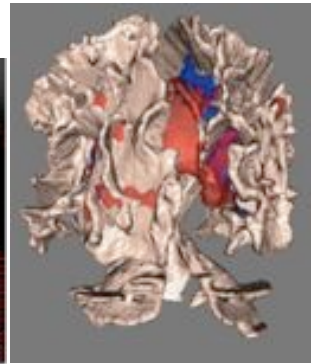
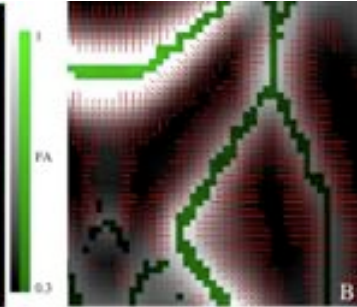
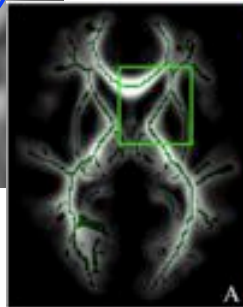
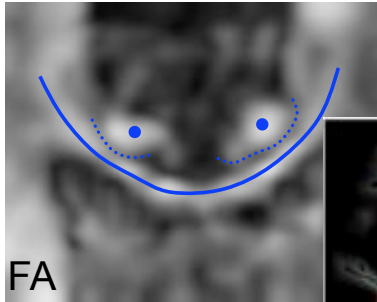
Collaboration with Brigham & Women's Hospital, Harvard Medical School: Raúl San José Estépar, Ph.D., James C. Ross, M.S. Alejandro A. Diaz, M.D., Edwin K. Silverman, M.D., Ph.D., George R Washko², M.D. and the COPDGene Investigators

6 (Applications)

Brain white matter from diffusion MRI



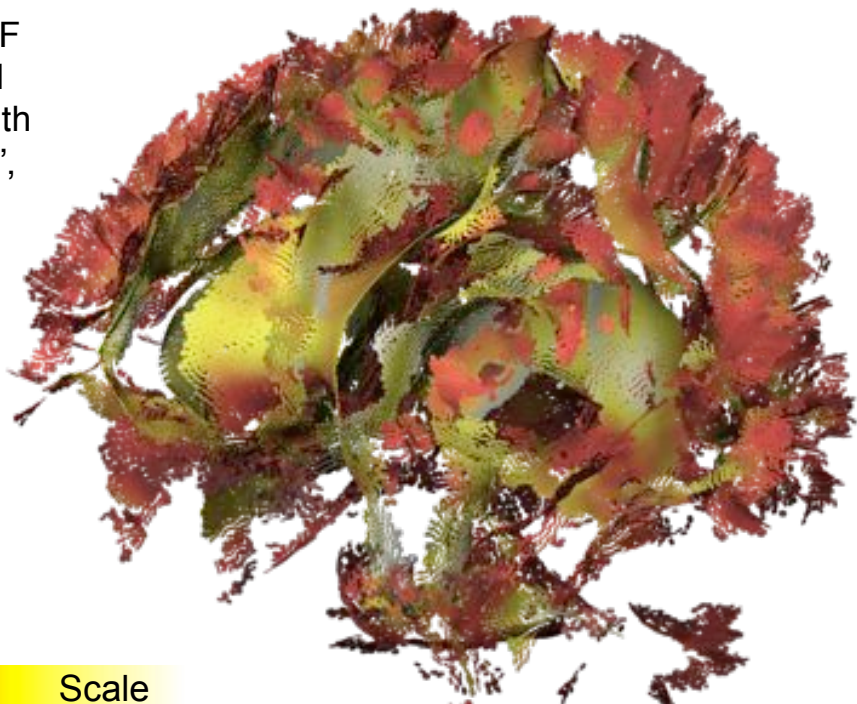
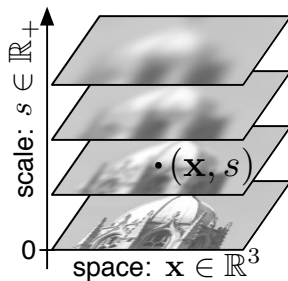
- Goal: automatically delineate large-scale white matter structures
- “Sulci for white matter”
- **Shape**, not connectivity
- Smith et. al. “Tract-Based Spatial Statistics” NeuroImage '06



7 (Applications)

Brain white matter from diffusion MRI

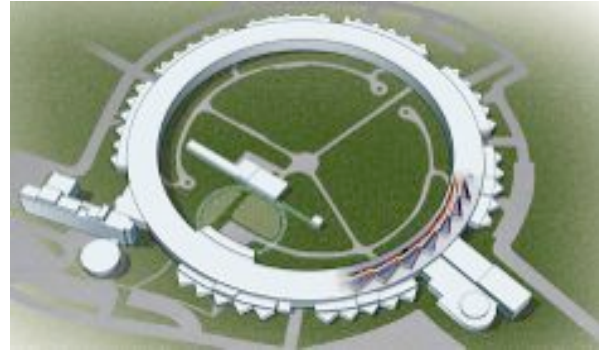
G Kindlmann, RSJ Estepar, SM Smith, C-F Westin, “Sampling and Visualizing Creases with Scale-Space Particles”, IEEE Trans. on Visualization and Computer Graphics, 2009, 15:1415-1424



8 (Applications)

Genetics Model Organisms w/ MicroCT

- Argonne National Lab; Advanced Photon Source
- Multiple beamlines, one for microscopic CT



- ~5 micron resolution;
output volumes
2000 x 2000 x 4000
(versus clinical CT $\approx 256 \times 256 \times 256$)
- Working on building infrastructure for data
movement between Argonne and UChicago

9 (Applications)

Genetics Model Organisms w/ MicroCT

- Zebrafish is a model organism for genetics
 - Visual system model for human vision
 - Dr. Keith Cheng, Penn State University
- Some phenotypes are manifest only in adult zebrafish
- Opaque \Rightarrow No Confocal \Rightarrow MicroCT

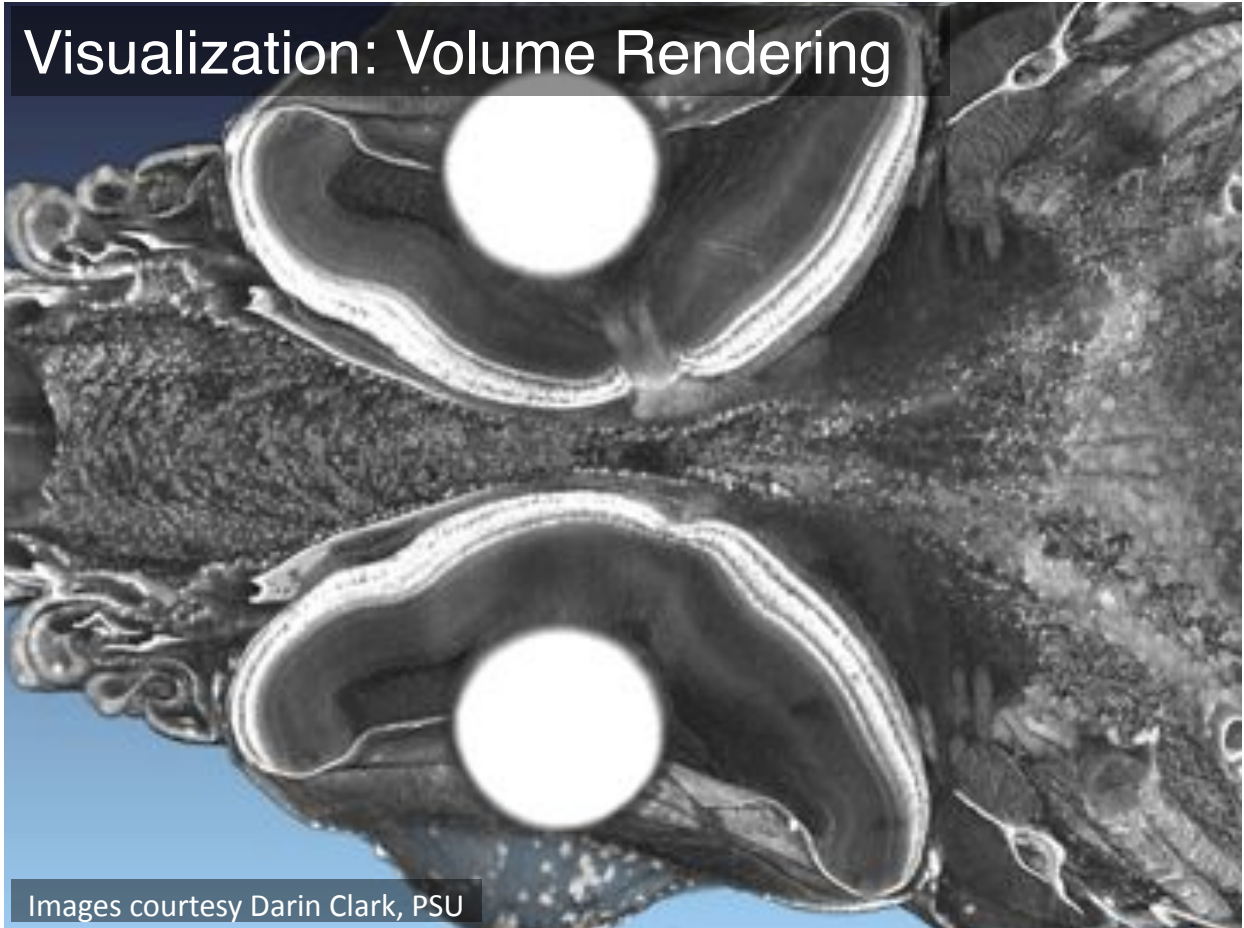
- Have 1000s of mutants



- Need high-throughput tools for:
 - inspecting acquisition & analysis pipeline
 - feature quantification for phenotyping

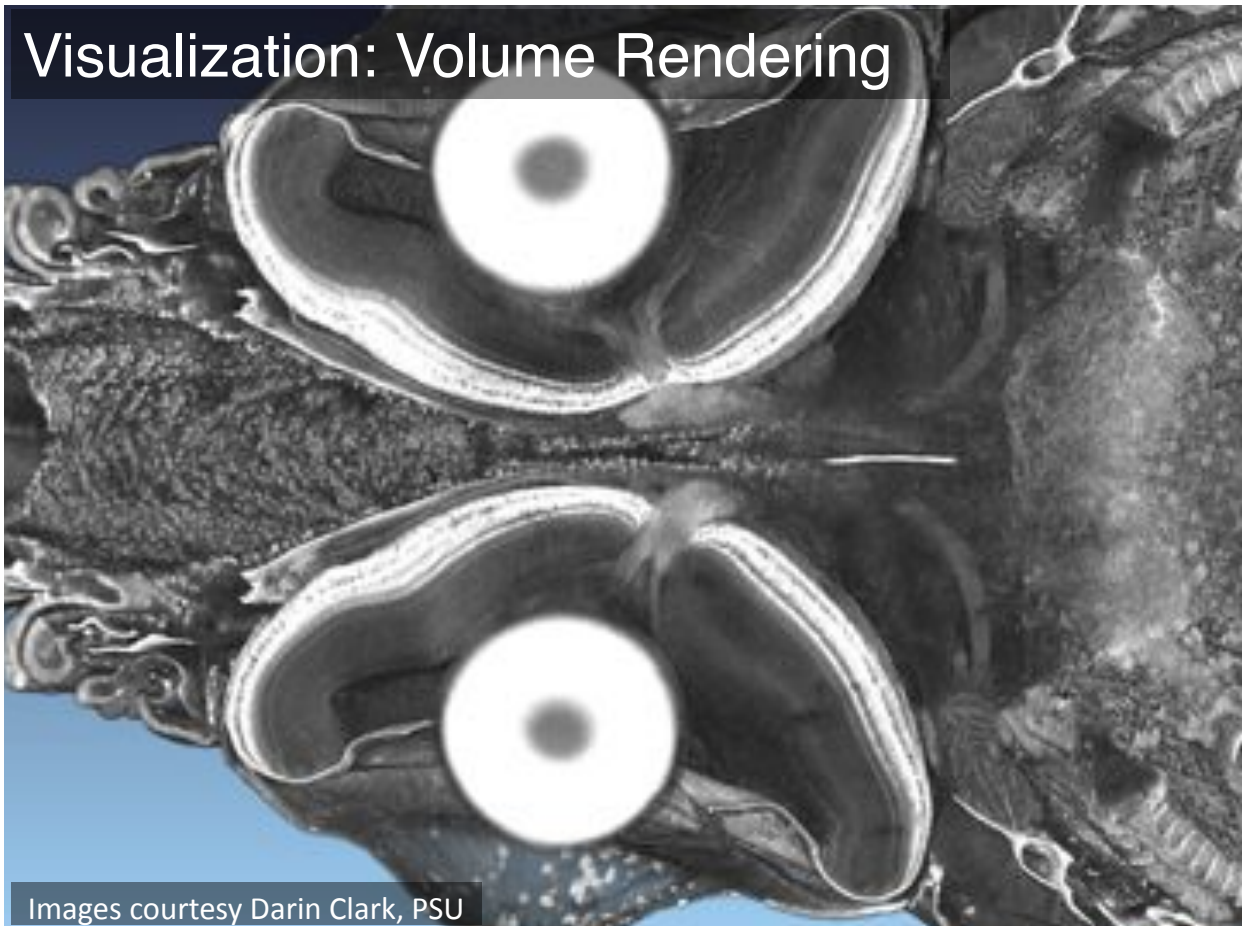
10 (Applications)

Visualization: Volume Rendering



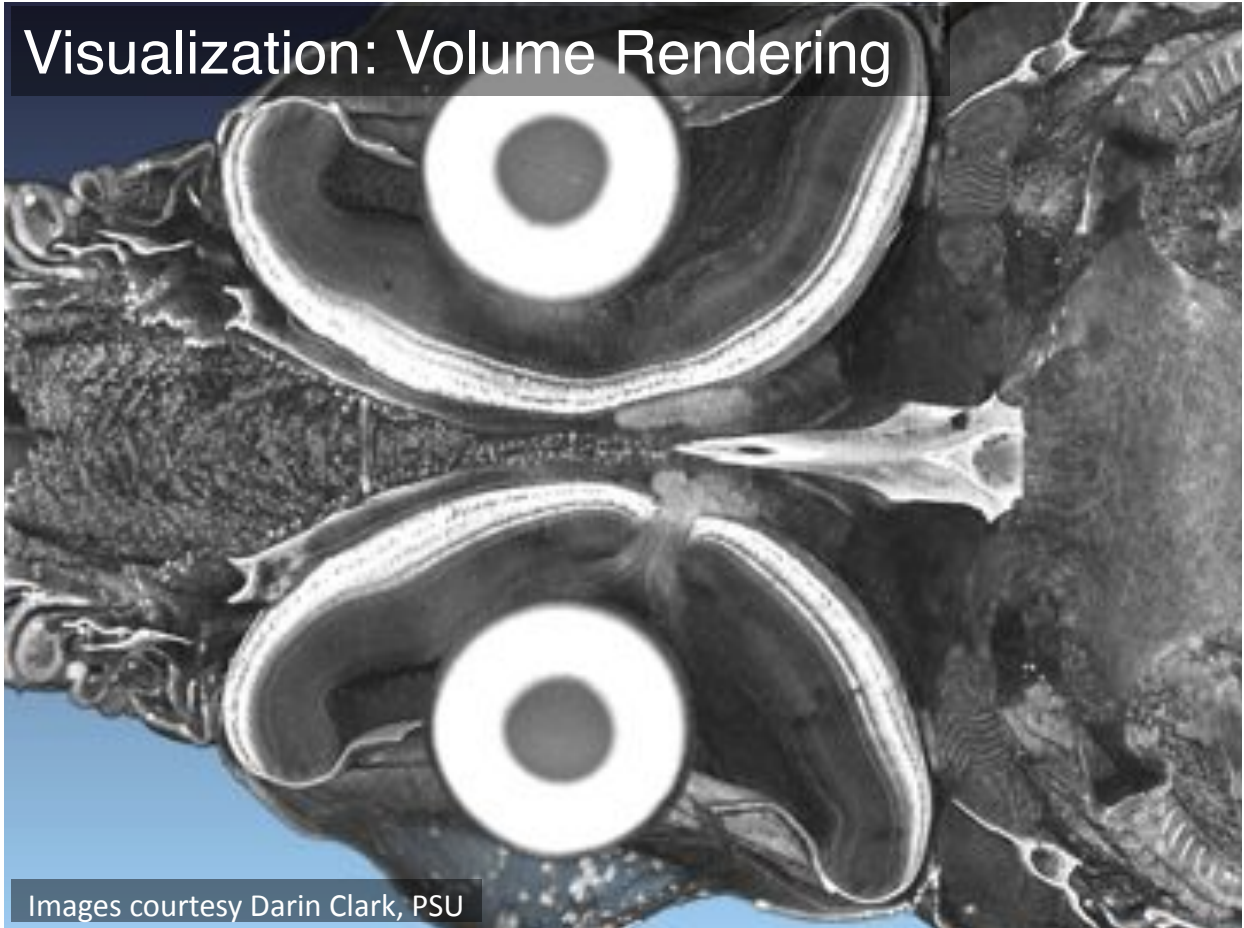
Images courtesy Darin Clark, PSU

Visualization: Volume Rendering



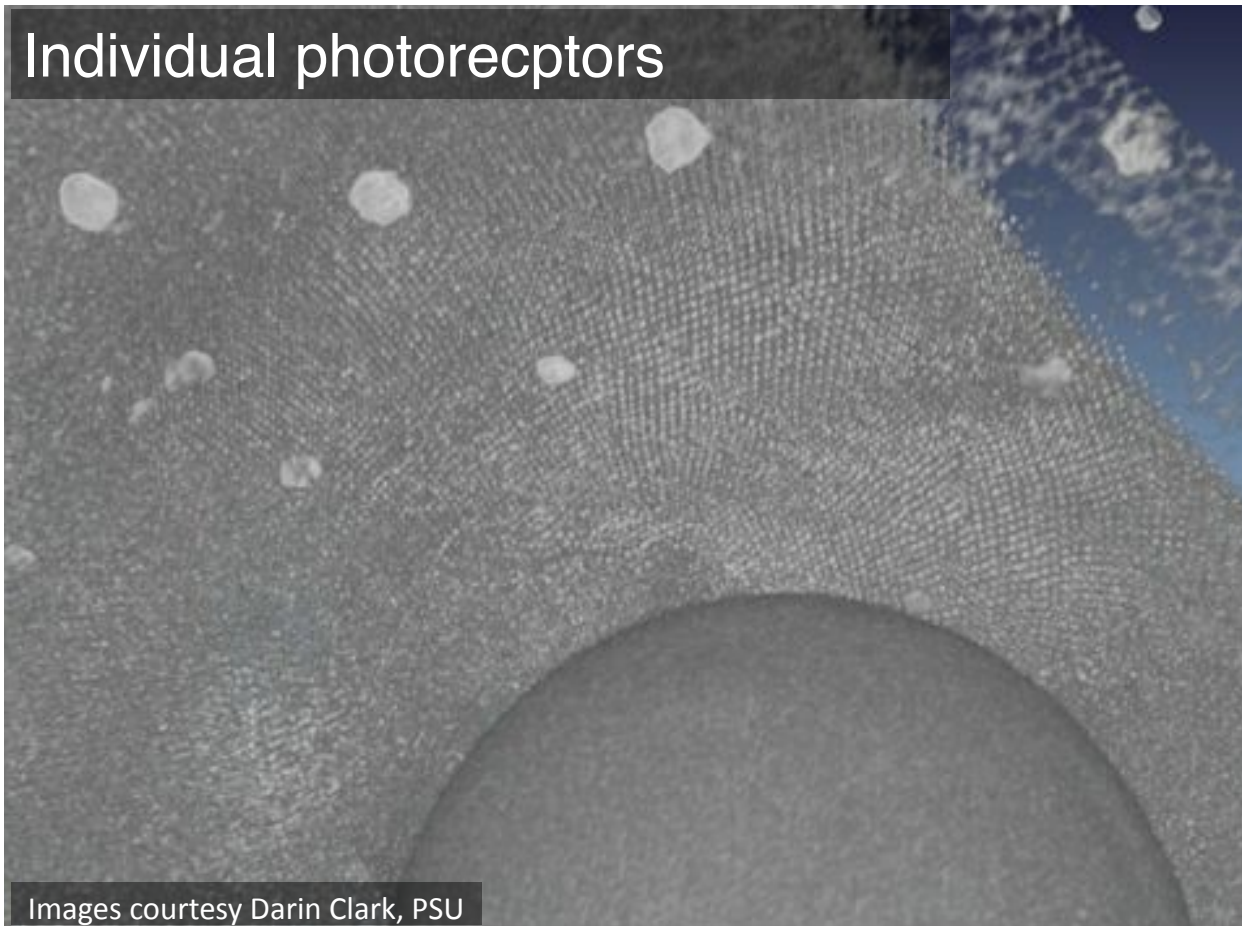
Images courtesy Darin Clark, PSU

Visualization: Volume Rendering



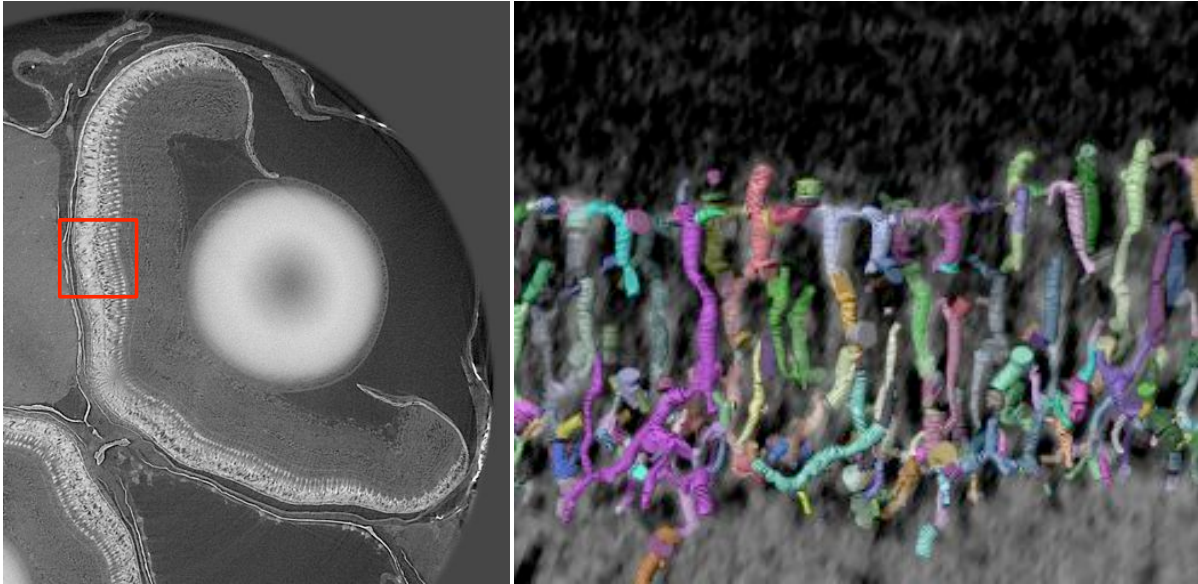
Images courtesy Darin Clark, PSU

Individual photoreceptors



Images courtesy Darin Clark, PSU

Particle systems for micro-anatomy



- First extraction of individual photoreceptors from microCT
- Wealth of anatomical features at larger scales

15 (Applications)

Outline

- Applications
 - Clinical Lung Studies (chest CT, Emphysema)
 - Brain Structure (diffusion MRI, white matter)
 - Zebrafish phenotyping (micro CT, eyes, etc)

- **Method: Particle Systems for Features**

- Feature definition & extraction
- Decomposition into Particles
- System Optimization

**Tell me how I
can be doing
this better!**

- **Particle System Economization**

- Decomposition of Costs
- Parameter tuning, algorithmic tuning?

16

Feature Definition

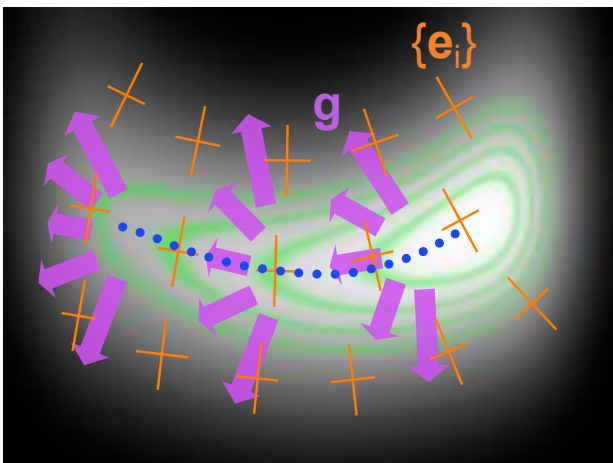
- Assume: continuous, differentiable image $f(\mathbf{x})$
- **Feature**: set of positions \mathbf{x} in image domain satisfying a defining formula $p(f, \mathbf{x}) = \text{true}$
 - Relies on local measurements, especially derivatives
 - Intent: Properties of the feature should correspond to properties of underlying object of scientific study
- **Feature strength**: measure of validity or reliability of feature $s(f, \mathbf{x}) \in \mathbb{R}$
 - Intent: Avoid extracting feature at locations where it is not meaningful or informative

Feature Definition Examples

- Isosurface at v_0
 - $f(\mathbf{x}) = v_0$
 - $s(f, \mathbf{x}) = ?$
 - One parameter
- Laplacian 0-crossing
 - $\nabla^2 f(\mathbf{x}) = 0$
 - $s(f, \mathbf{x}) = |\nabla f(\mathbf{x})|$
 - Zero parameters



Ridges/Valleys = Creases



“Ridges in Image and Data Analysis” Eberly '96

Constrained extremum

Gradient \mathbf{g}

Hessian eigensystem \mathbf{e}_i, λ_i

Crease: \mathbf{g} orthogonal to one or more \mathbf{e}_i

Eigenvalues determine strength s

$$\text{Ridge surface: } \mathbf{g} \cdot \mathbf{e}_3 = 0; \quad s = -\lambda_3$$

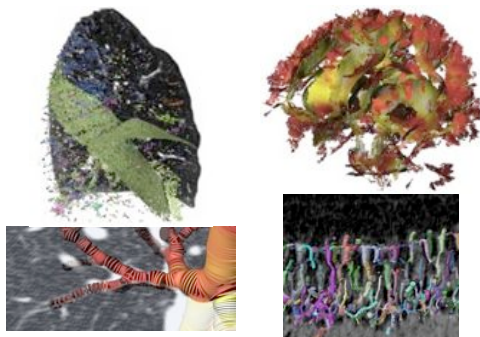
$$\text{Ridge line: } \mathbf{g} \cdot \mathbf{e}_3 = \mathbf{g} \cdot \mathbf{e}_2 = 0; \quad s = -\lambda_2$$

$$\text{Valley surface: } \mathbf{g} \cdot \mathbf{e}_1 = 0; \quad s = \lambda_1$$

Feature Definition Examples



Creases ...



Isosurface

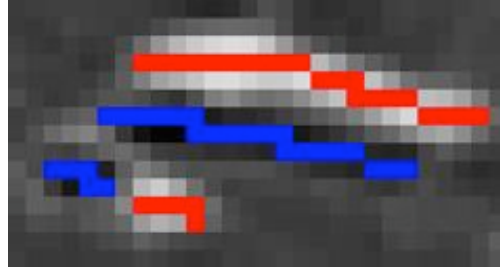


Laplacian zero-crossing



Feature Extraction Options

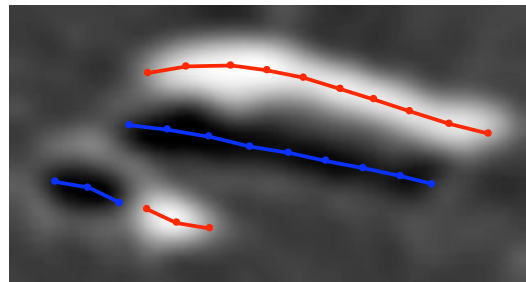
- Representation: **Raster** or **Polygonal**
- **Raster**: Binary mask (traditional classification) computes pixels of $g[\mathbf{x}] \in \{0,1\}$; $p(f, \mathbf{x}) \Leftrightarrow g(\mathbf{x})=1$
 - Loose sub-pixel accuracy
 - Often seeking structure at limits of resolution (pixels are expensive)
- Level-Sets (Sethian&Osher) compute pixels in new raster image of $g(\mathbf{x}) \in \mathbb{R}$; $p(f, \mathbf{x}) \Leftrightarrow g(\mathbf{x})=0$
 - Assumes that features are co-dimension 1; not the case with crease lines (co-dimension 2)



21 (Method: Particles: Feature Extraction)

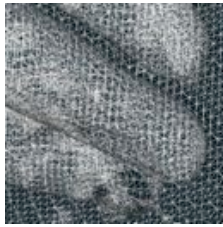
Feature Extraction

- **Polygonal** representation
 - sub-pixel accuracy
 - co-dimension 1 or 2
- To extract feature:
 - Compute vertex locations and connectivity
- Marching Cubes does both at same time
- Image grid determines both vertex location and connectivity
- Location could be optimized separately ...



22 (Method: Particles: Feature Extraction)

Particles for Image Features



Miriah Meyer's work 2005-2008

- Compute vertex location separately from computing vertex connectivity
- vertex location: local image feature detection
 - entirely determined by feature definition
 - implement one particle, and you're done
- vertex connectivity: computational geometry
 - many apps don't actually need connectivity
- Handles different co-dimensions equally well

23 (Method: Particles: Decomposition into Particles)

Driving equation for particle system

$$\underset{\substack{\mathbf{x}_i, N \\ \uparrow \quad \uparrow \\ \text{Particle} \quad \text{Number of} \\ \text{positions} \quad \text{Particles}}}{\operatorname{argmin}} \mathcal{E} = \underset{\mathbf{x}_i, N}{\operatorname{argmin}} (1 - \alpha) \underbrace{\sum_{i=1}^N E_i}_{\substack{\text{Particle-image} \\ \text{energy (for feature} \\ \text{detection in scale-space)}}} + \frac{\alpha}{2} \underbrace{\sum_{i,j=1}^N E_{ij}}_{\substack{\text{Inter-particle} \\ \text{energy:} \\ \text{induces} \\ \text{uniform} \\ \text{sampling}}}$$

without scale-space:

$$\underset{\mathbf{x}_i, N}{\operatorname{argmin}} \mathcal{E} = \underset{\mathbf{x}_i, N}{\operatorname{argmin}} \sum_{i,j=1}^N E_{ij}$$

- **Particle system goal: minimize inter-particle energy in the presence of (energy-free) feature constraints**
 - Minimizing energy: Moving, adding, removing particles
 - Constraints: isosurface ($f(\mathbf{x}) - v_0 = 0$): Newton's method
 - Ridges and Valleys ($\nabla f(\mathbf{x}) \cdot \mathbf{e}_3 = 0$): Newton optimization

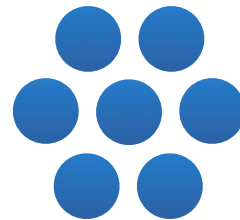
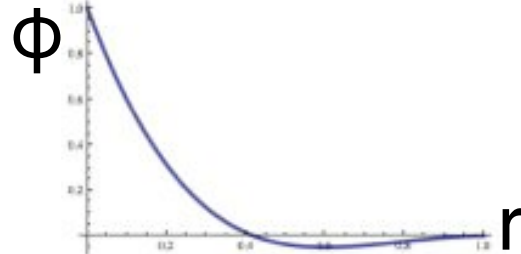
24 (Method: Particles: Decomposition into Particles)

Inter-particle energy E_{ij}

- Determines system behavior and converged configuration

$$E_{ij} = \Phi \left(\frac{|\mathbf{x}_i - \mathbf{x}_j|}{\sigma_r} \right)$$

- Currently:
 - no orientation wrt feature
 - uniform scale σ_r
 - small zone of attraction
- Attractive zone allows population control to be folded into energy minimization



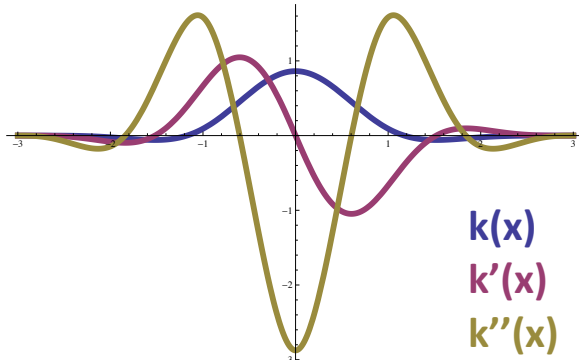
Current Energy minimization

- No particle mass; Asynchronous updates
- For each particle i (at position \mathbf{x}_i , with step size h_i)
 - Learn neighbors j and compute
 - energy $e_i = \sum_j \phi(\mathbf{x}_j - \mathbf{x}_i)$ & force $\mathbf{f}_i = -\sum_j \nabla \phi(\mathbf{x}_j - \mathbf{x}_i)$
 - do {
 - $\mathbf{x}_{test} = \text{ConstraintSatisfy}(\mathbf{x}_i + h_i * \mathbf{f}_i)$
 - $e_{test} = \sum_j \phi(\mathbf{x}_j - \mathbf{x}_{test})$
 - $badstep = e_{test} > e_i + e_{perm}$
 - if $badstep$: $h_i = h_i * backoff$
 - } while $badstep$
 - $\mathbf{x}_i = \mathbf{x}_{test}$
 - $h_i = h_i * creepup$
- parms: $backoff=0.1$, $creepup=1.1$, $e_{perm}=0.001$

Bottleneck!

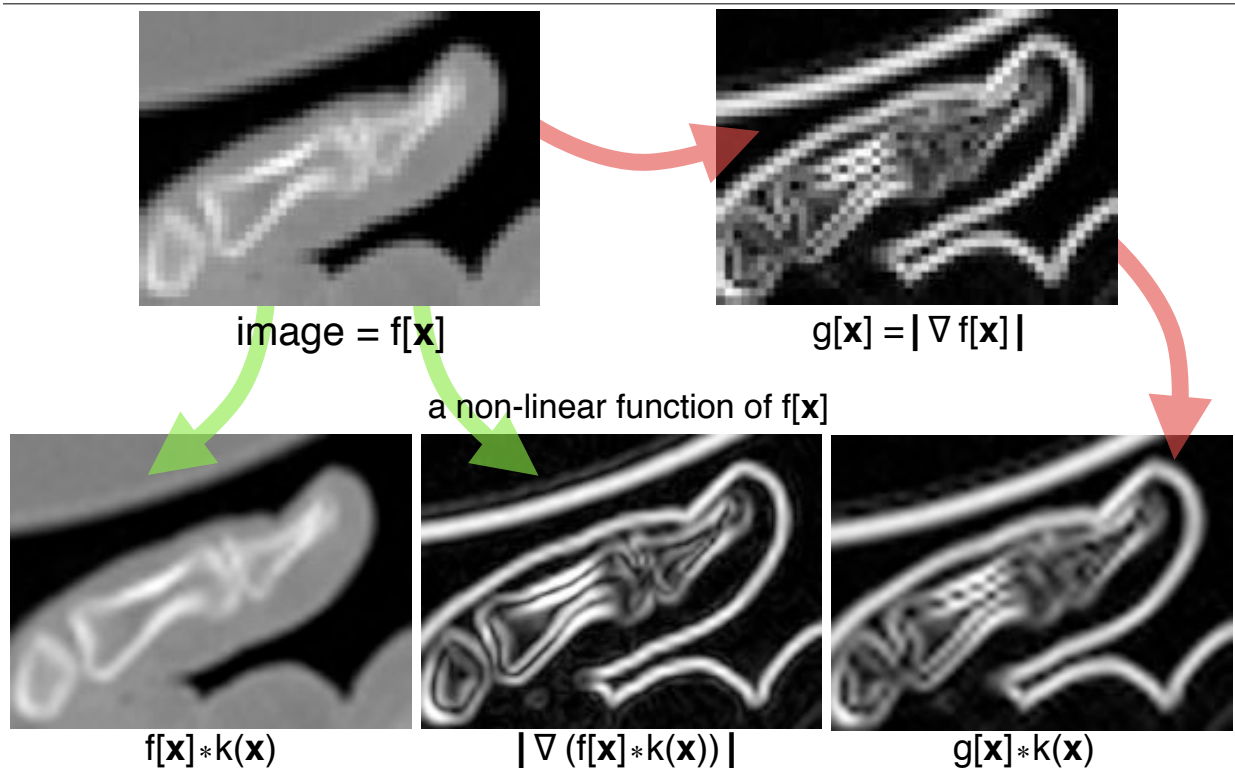
Value & Derivative measurement

- Need smooth field from discrete image data
- **Convolution** (Separable \rightarrow 3D kernels)
- Differentiability required for gradients, Hessians used in constraint satisfaction
- Accuracy (in the Taylor sense) avoids sample-frequency ripple in image features



6-sample support Piece-wise 6th-order polynomial
 C^4 continuity 4th-order error
 "Evaluation and Design of Filters Using a Taylor Series Expansion,"
 Möller et al. IEEE TVCG '97

Derivative measurement: Can't skimp

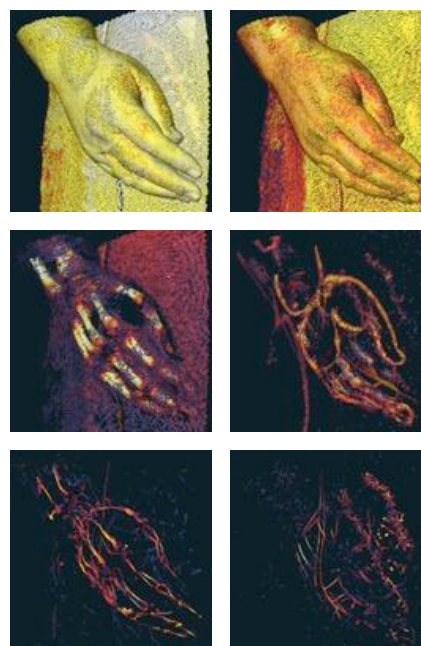


Demo on synthetic dataset ...

29 (Method: Particles: Decomposition into Particles)

Gallery of particles for different features

- Illustrated with hand from Visible Human, Female CT
- Feature types
 - Isosurface
 - Laplacian zero-crossing
 - Ridges & Valleys (“creases”)
 - surfaces or lines
- **Particle system samples features**
 - each little glyph = one particle
 - show local feature ingredients

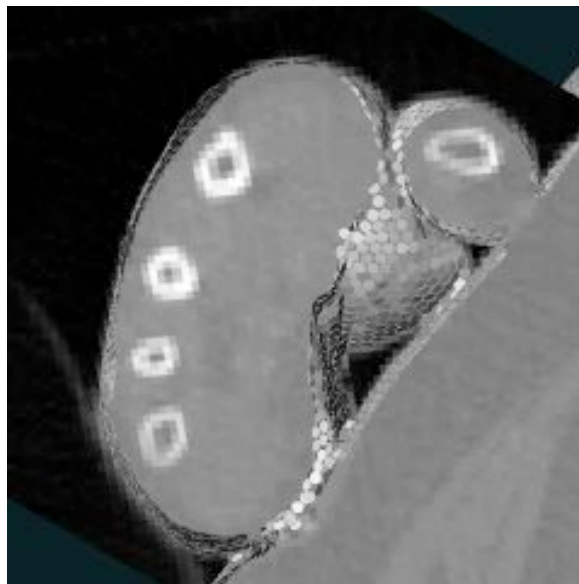


30 (Method: Particles: Results)

Isosurface



Outside 3D view

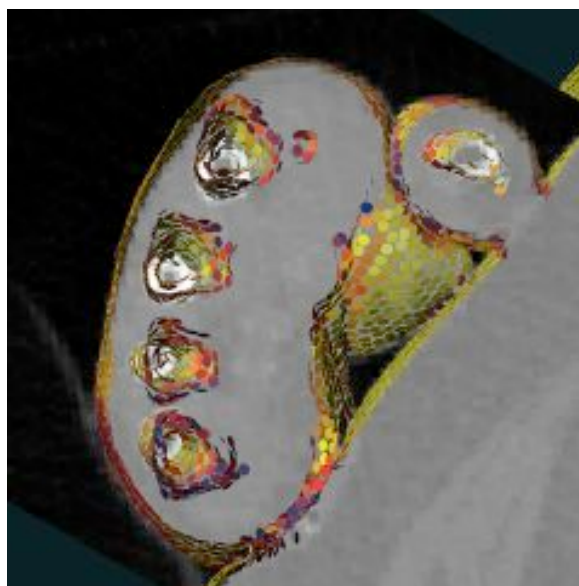


Different, Cropped 3D view w/ 2D plane

- AKA isophote, isocontour, level set
- $f(\mathbf{x}) = v_0$

31 (Method: Particles: Results)

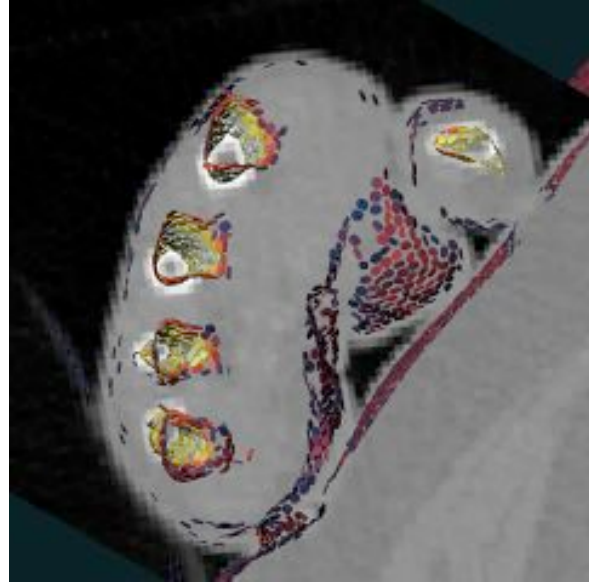
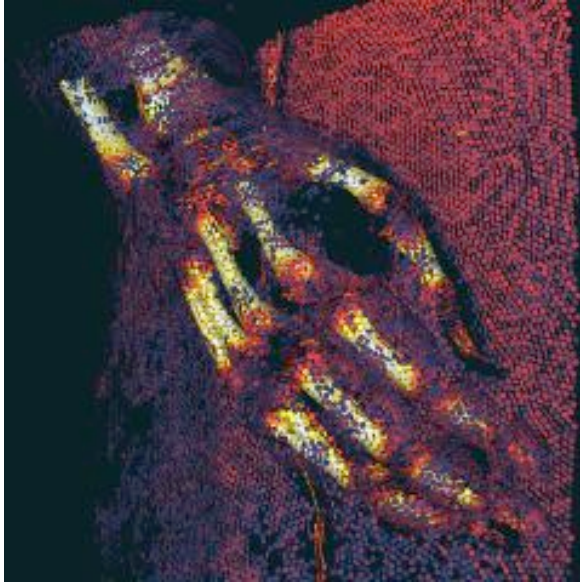
Laplacian 0-crossing



- Classical definition of edge
- $\nabla^2 f(\mathbf{x}) = 0$; strength = $|\nabla f(\mathbf{x})|$

32 (Method: Particles: Results)

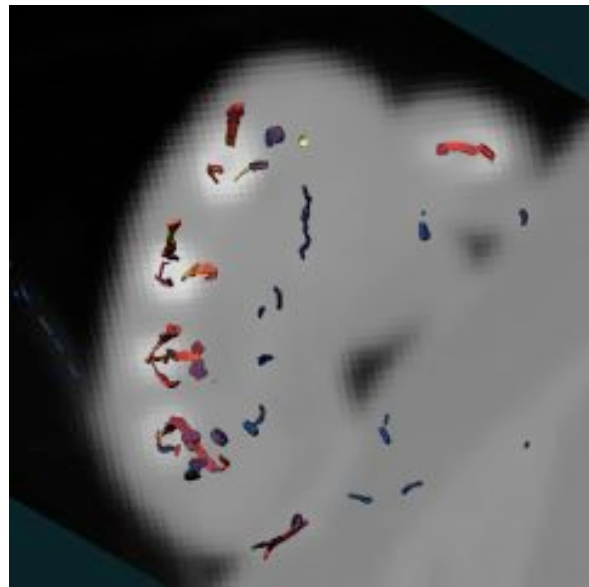
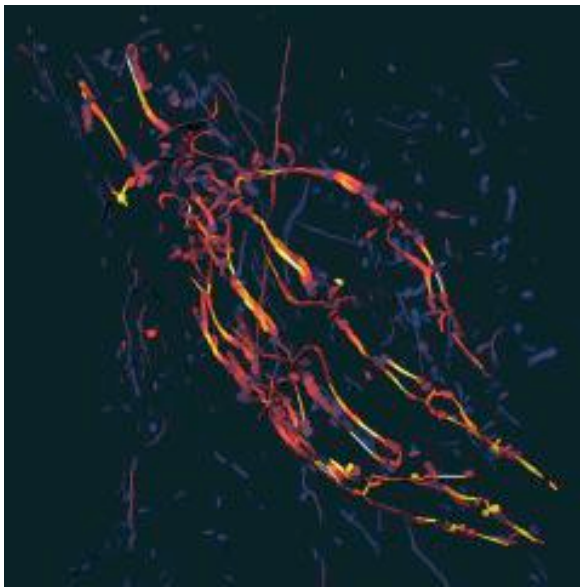
Ridge Surface



- Maximal surface wrt Hessian minor eigenvector \mathbf{e}_3
- $\nabla f(\mathbf{x}) \cdot \mathbf{e}_3(\mathbf{x}) = 0$; strength = $-\lambda_3$

33 (Method: Particles: Results)

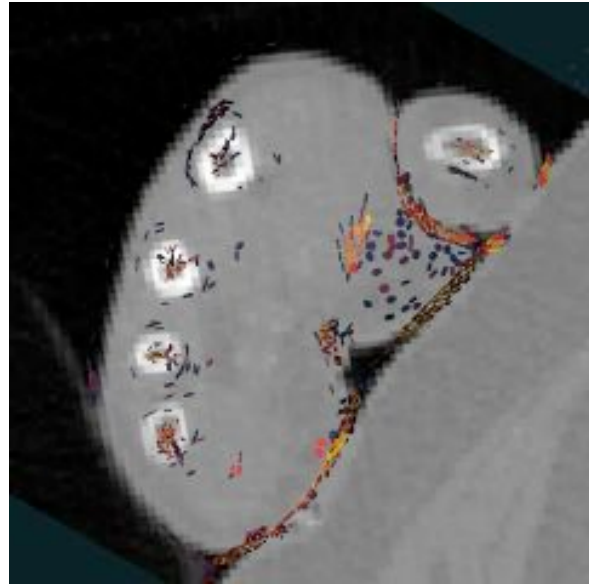
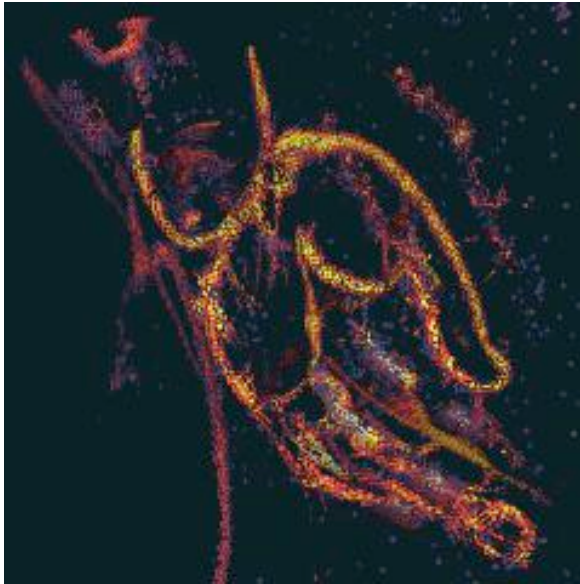
Ridge Line



- Maximal curve wrt Hessian minor, medium eigenvectors
- $\nabla f(\mathbf{x}) \cdot \mathbf{e}_3(\mathbf{x}) = 0$, $\nabla f(\mathbf{x}) \cdot \mathbf{e}_2(\mathbf{x}) = 0$; strength = $-\lambda_2$

34 (Method: Particles: Results)

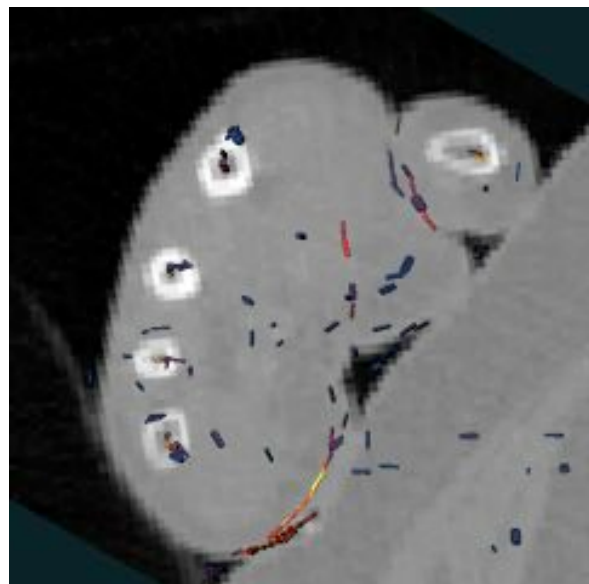
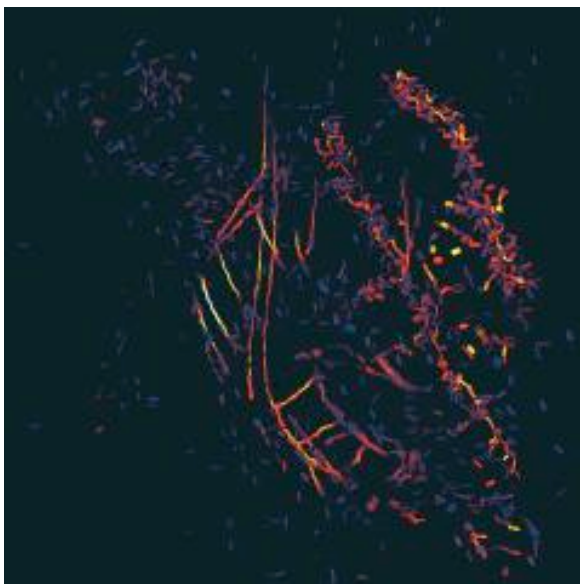
Valley Surface



- Minimal surface wrt Hessian major eigenvector \mathbf{e}_1
- $\nabla f(\mathbf{x}) \cdot \mathbf{e}_1(\mathbf{x}) = 0$; strength = λ_1

35 (Method: Particles: Results)

Valley Line



- Minimal curve wrt Hessian major, medium eigenvectors
- $\nabla f(\mathbf{x}) \cdot \mathbf{e}_1(\mathbf{x}) = 0$, $\nabla f(\mathbf{x}) \cdot \mathbf{e}_2(\mathbf{x}) = 0$; strength = λ_2

36 (Method: Particles: Results)

Outline

- Applications
 - Clinical Lung Studies (chest CT, Emphysema)
 - Brain Structure (diffusion MRI, white matter)
 - Zebrafish phenotyping (micro CT, eyes, etc)
- Method: Particle Systems for Features
 - Feature definition & extraction
 - Decomposition into Particles
 - Results
- Particle System Economization
 - Decomposition of Costs
 - Parameter tuning, algorithmic tuning?

Want new ideas & connections & terminology!

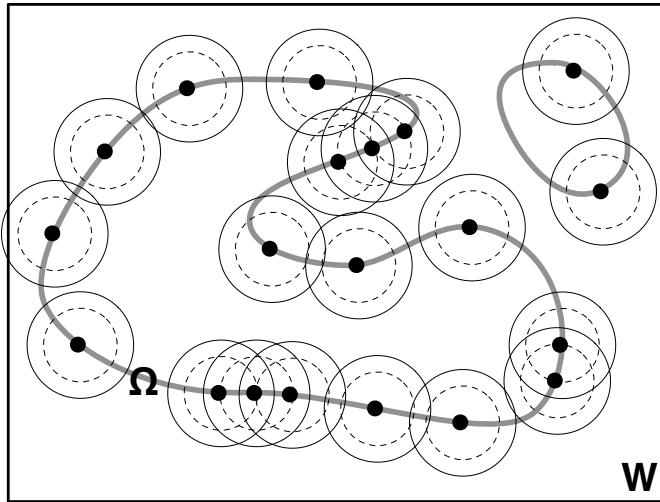
37

Parameters in current approach

- Want to minimize computation to find convergence
- Algorithm for energy minimization
 - currently opportunistic gradient descent
- Method of population control
 - when/how to check if add/nix → decrease energy
- Shape of inter-particle potential function ϕ
 - some shapes may lead faster to nice distribution
- Initialization (seeding system with particles)
 - currently brute-force search through ~all voxels
- **What is the conceptual framework for optimizing (in the sense of computational economization) all these choices & parameters?**

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Conceptual view: governing eq.s



$$P = \{\mathbf{x}_i\}_{i=1}^N; \mathbf{x}_i \in \Omega$$

Set of particles on feature

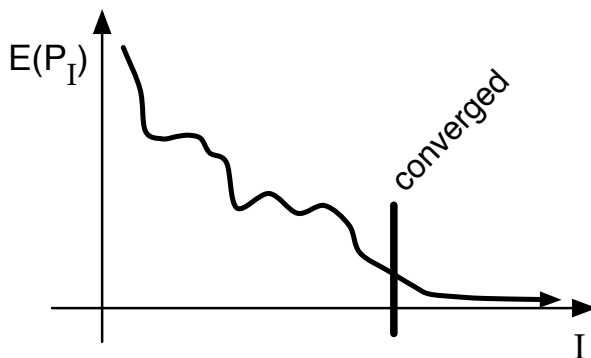
$$E(P) = \frac{1}{2} \sum_{i,j=1}^N \phi\left(\frac{|\mathbf{x}_i - \mathbf{x}_j|}{\sigma}\right)$$

Energy of particle set

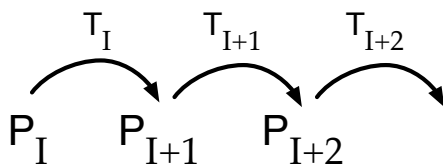
$$\operatorname{argmin}_{\{\mathbf{x}_i\}, N} E(P) = \operatorname{argmin}_{\{\mathbf{x}_i\}, N} \frac{1}{2} \sum_{i,j=1}^N \phi\left(\frac{|\mathbf{x}_i - \mathbf{x}_j|}{\sigma}\right)$$

System adds/nixes/moves particles to minimize energy

Conceptual view: iteration/convergence



- Computation of system should be towards convergence: condition where add/kill/move particles won't make a dramatic difference

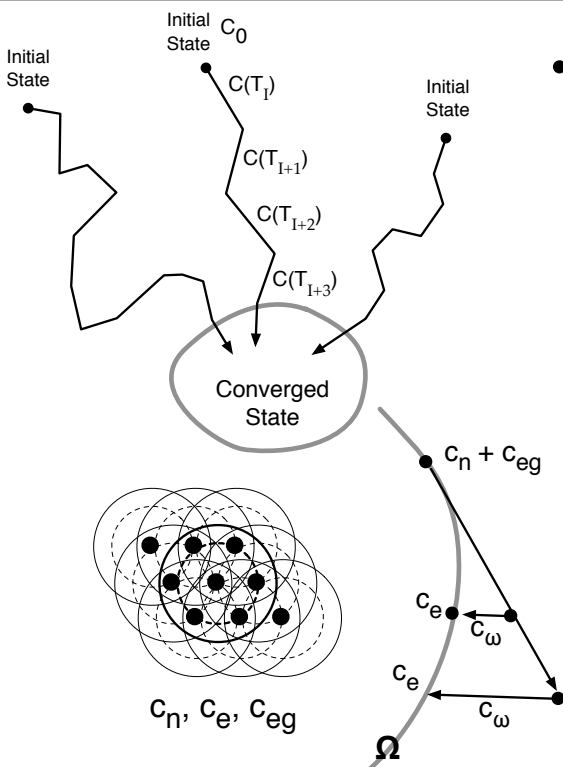


$$P_{I+1} = T(P_I) = T(\{\mathbf{x}_i\}_{i=1}^{N_I}) = \bigcup_{i=1}^{N_I} t(\mathbf{x}_i)$$

$$t(\mathbf{x}_i) = \begin{cases} \{\} & \mathbf{x}_i \text{ is killed} \\ \{\mathbf{x}'_i\} & \mathbf{x}_i \text{ is moved} \\ \{\mathbf{x}'_i, \mathbf{y}'_i\} & \mathbf{x}_i \text{ created new particle} \end{cases}$$

- Transition function T computes next iteration

Conceptual view: Economization

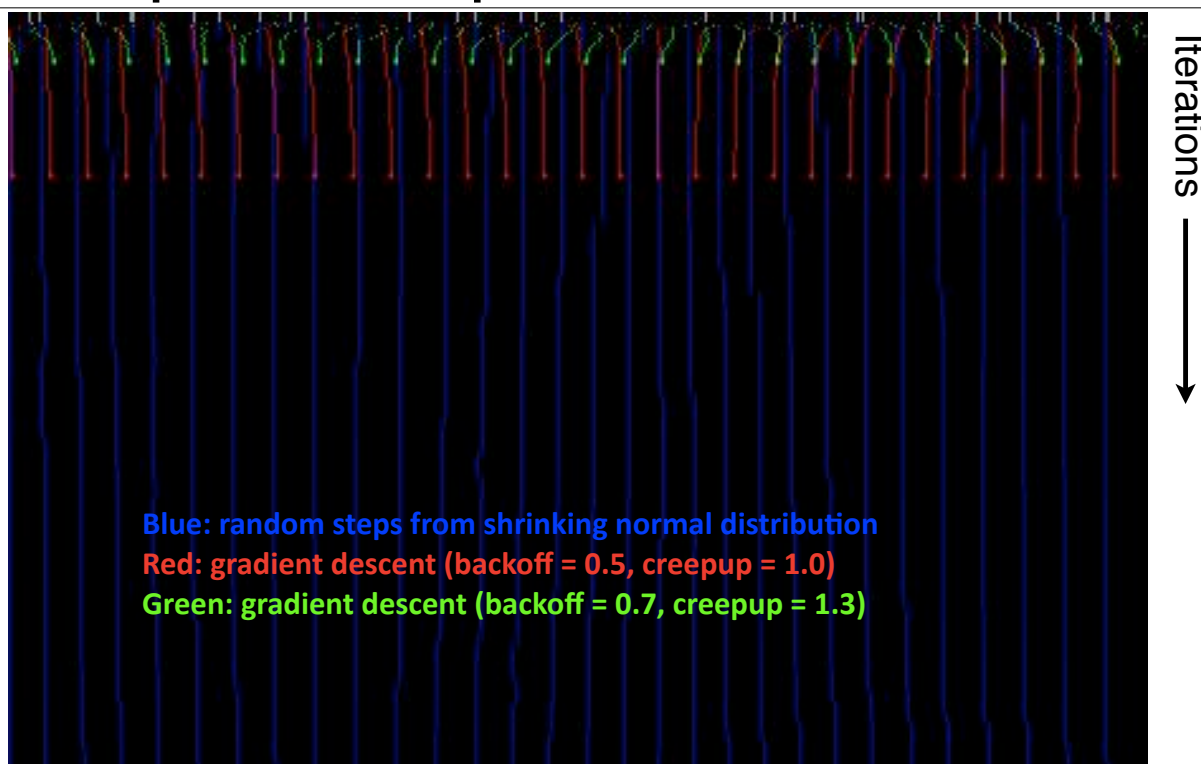


- Every transition has a cost $C(T)$, and we want to find a path into convergence that minimizes $C_0 + \sum_I C(T_I)$

- c_n : cost of learning neighb in support of $\Phi(r)$
- c_e : cost of computing energy due to neighbors
- c_{eg} : cost of computing energy and gradient
- c_ω : cost of re-asserting the constraint

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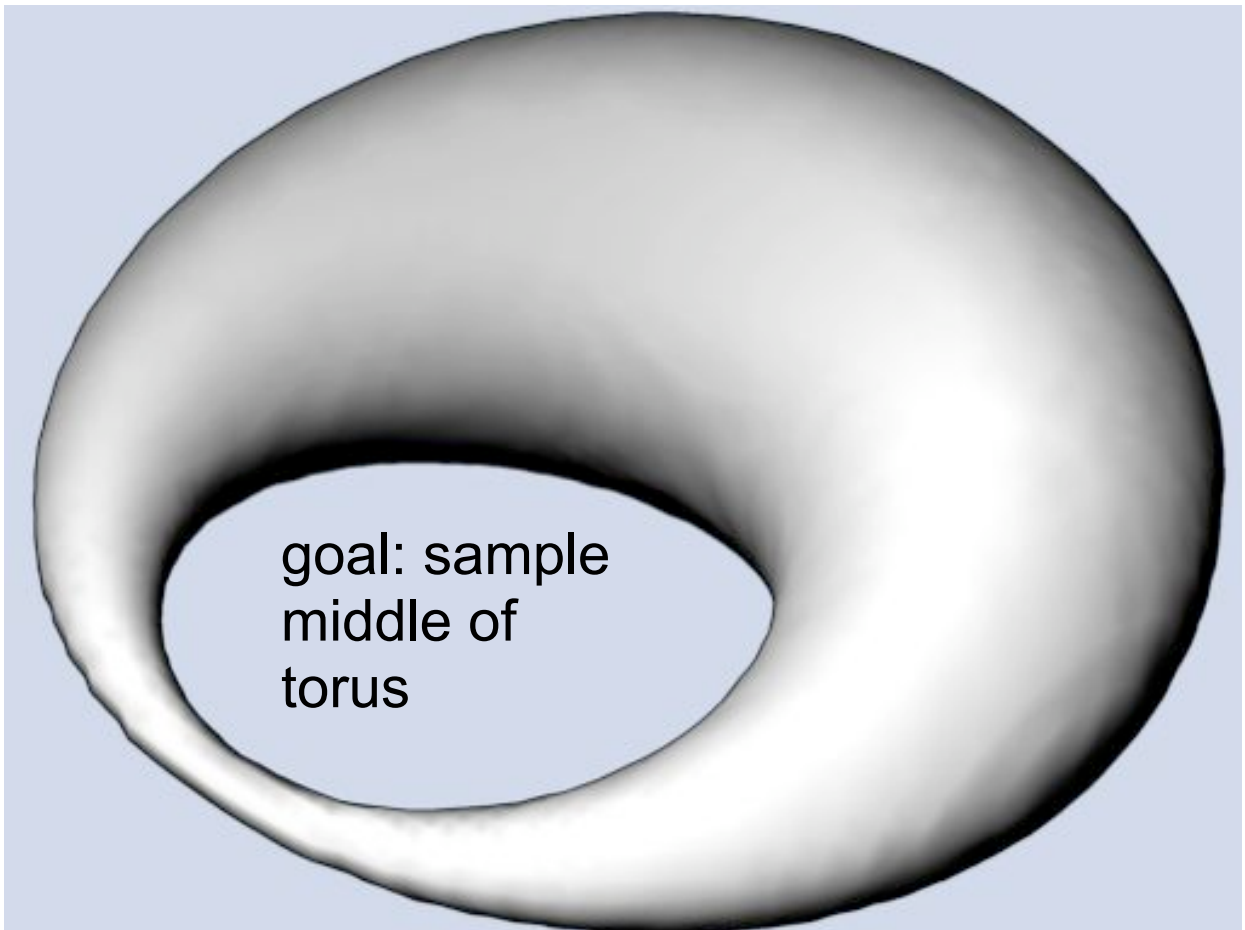
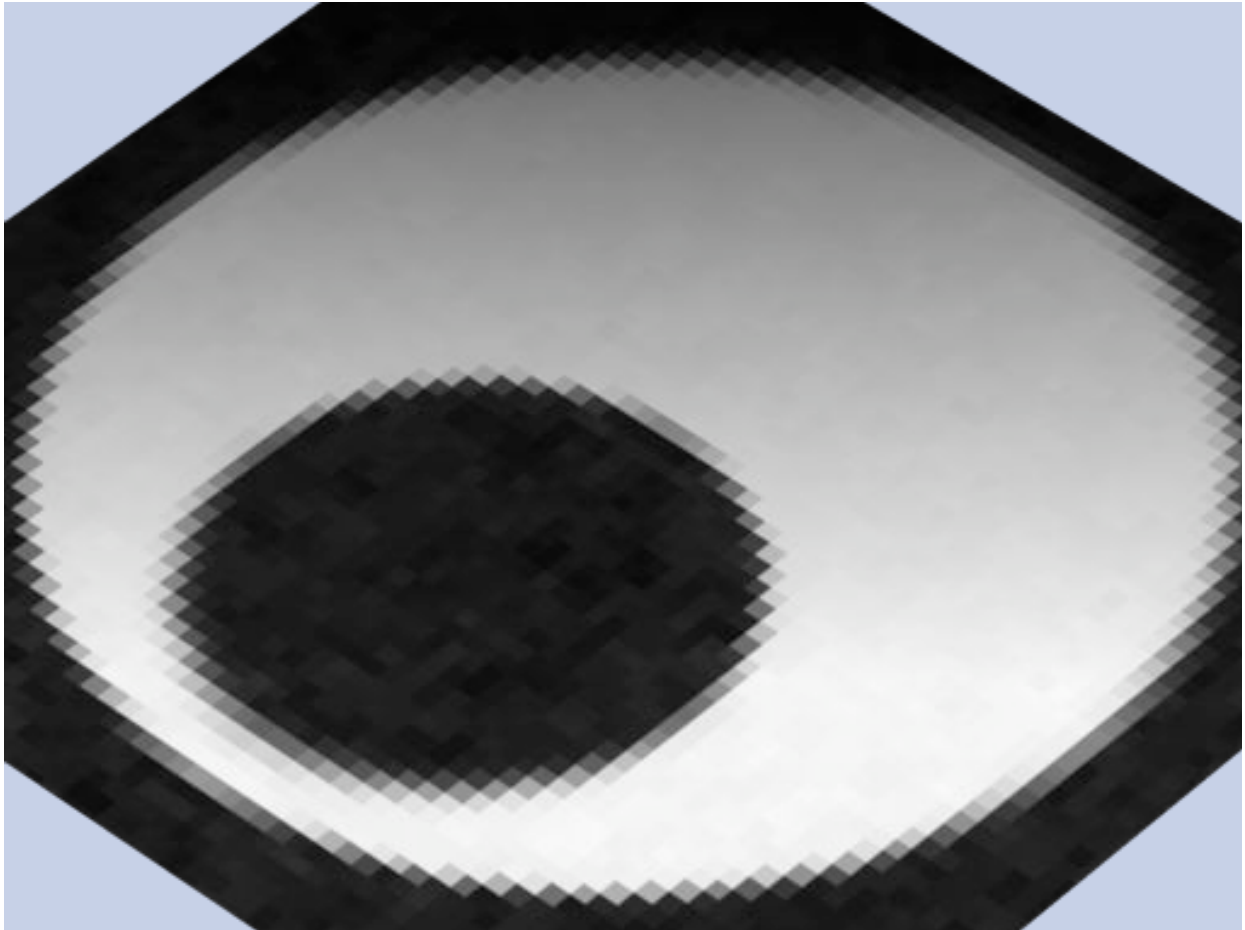
Simple case: particles on a circle

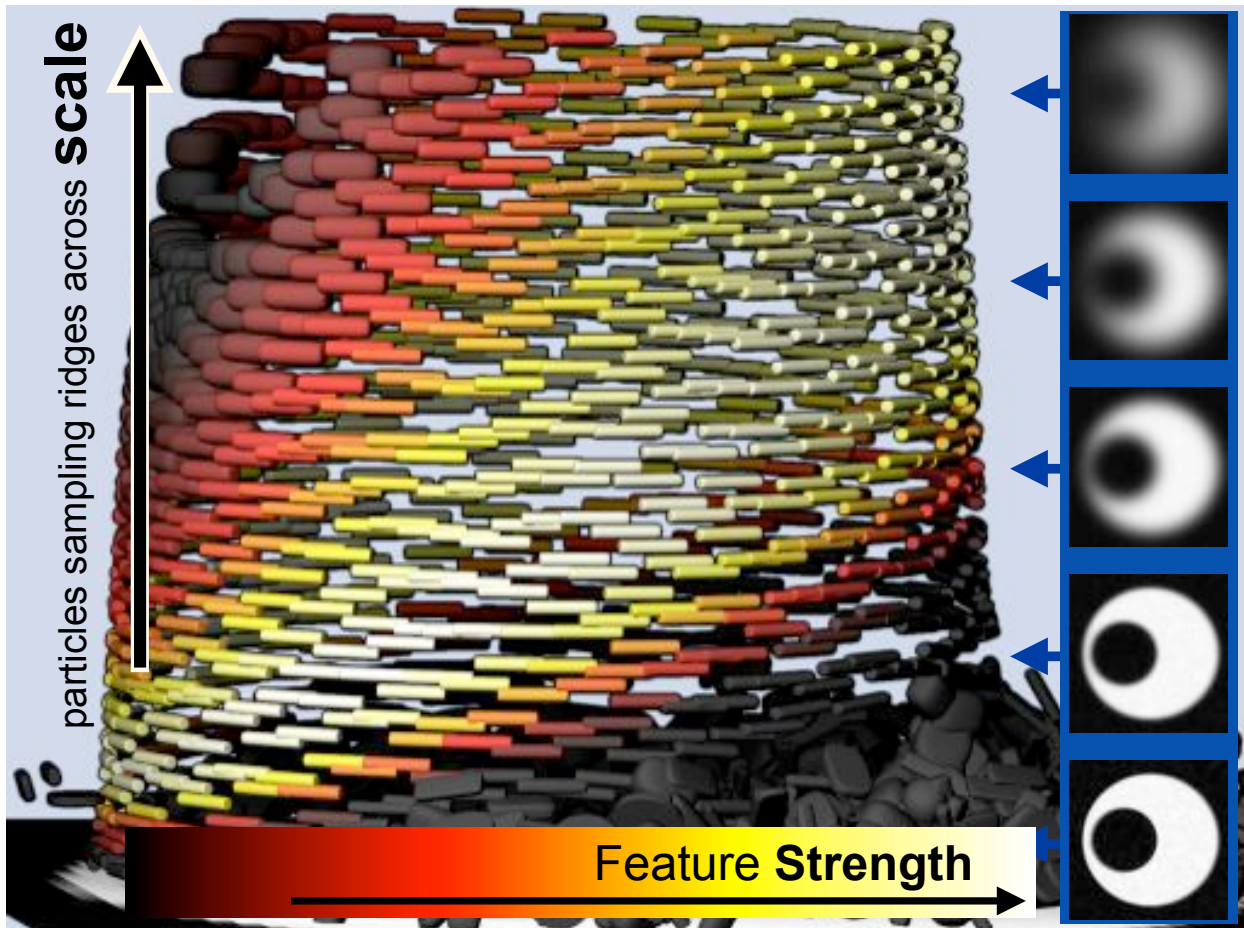
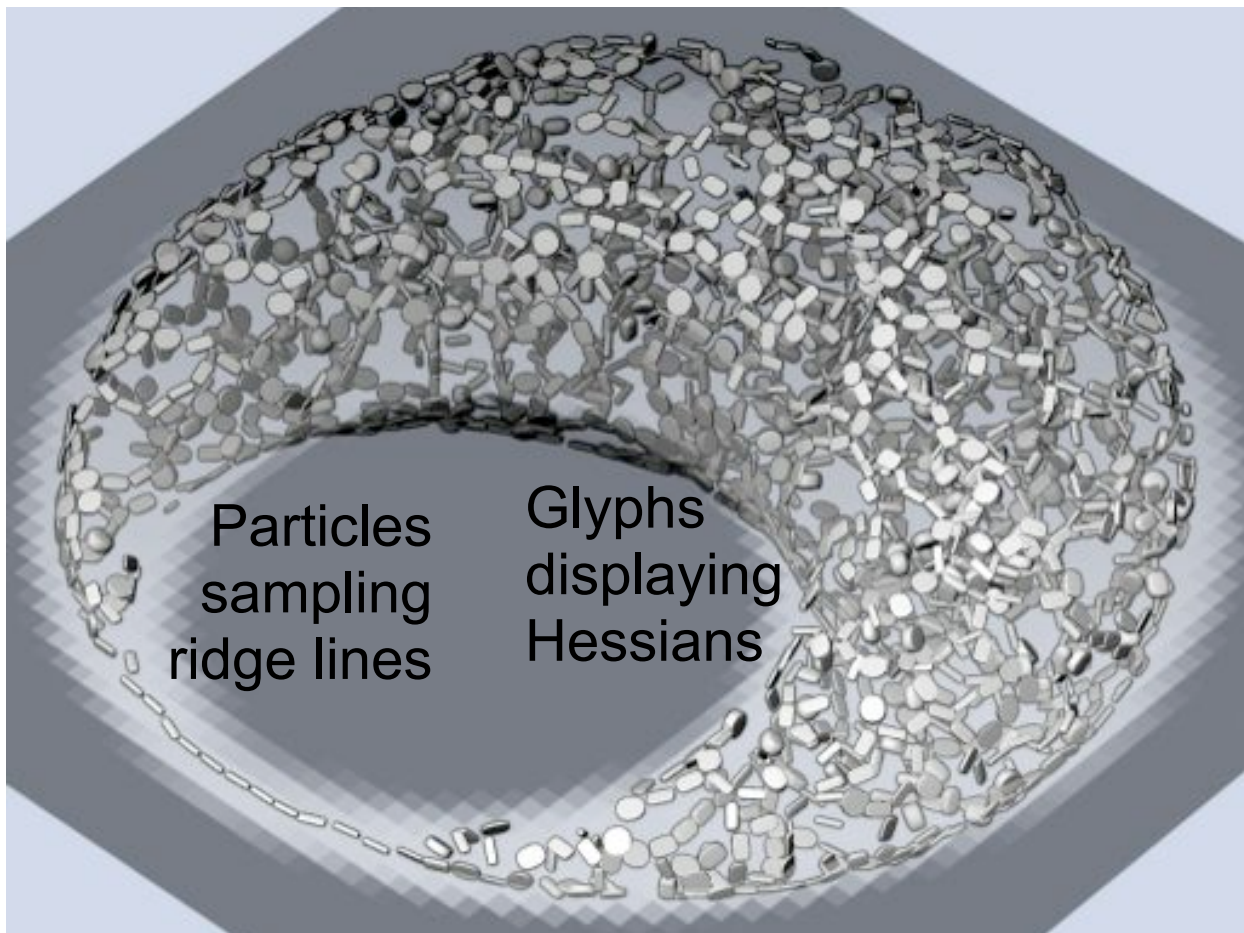


42

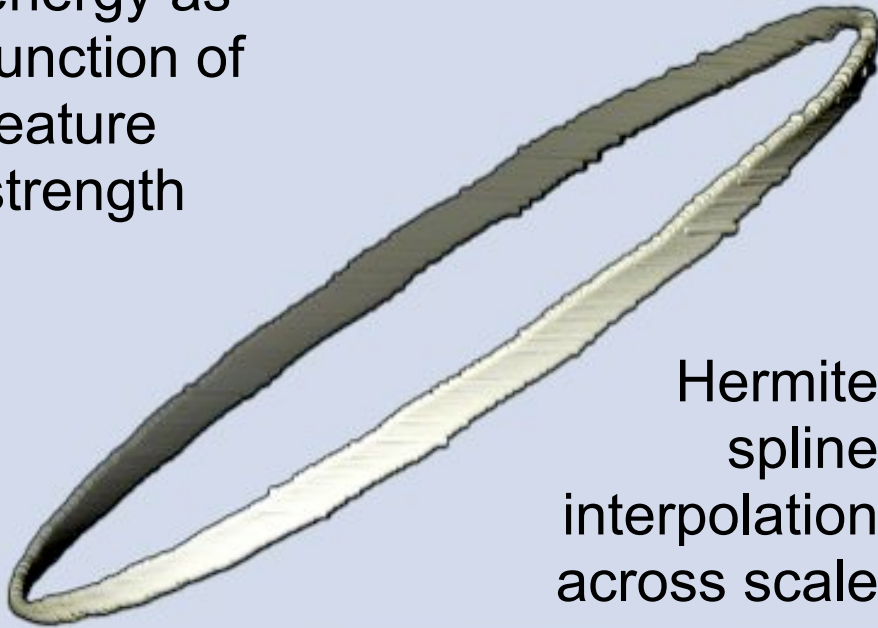
Conclusions/Discussion

- Particles powerful tool for feature sampling
 - many biomedical applications
 - likely non-biomedical applications!
- Particles separate feature sampling from connectivity
- Practical need: better user interface, more testing
- Theoretical research
 - Economization (right word?) of system optimization
 - Fast rejection of non-feature areas
 - Interested in hearing your ideas
- **Thanks for your attention!**
 - glk@uchicago.edu

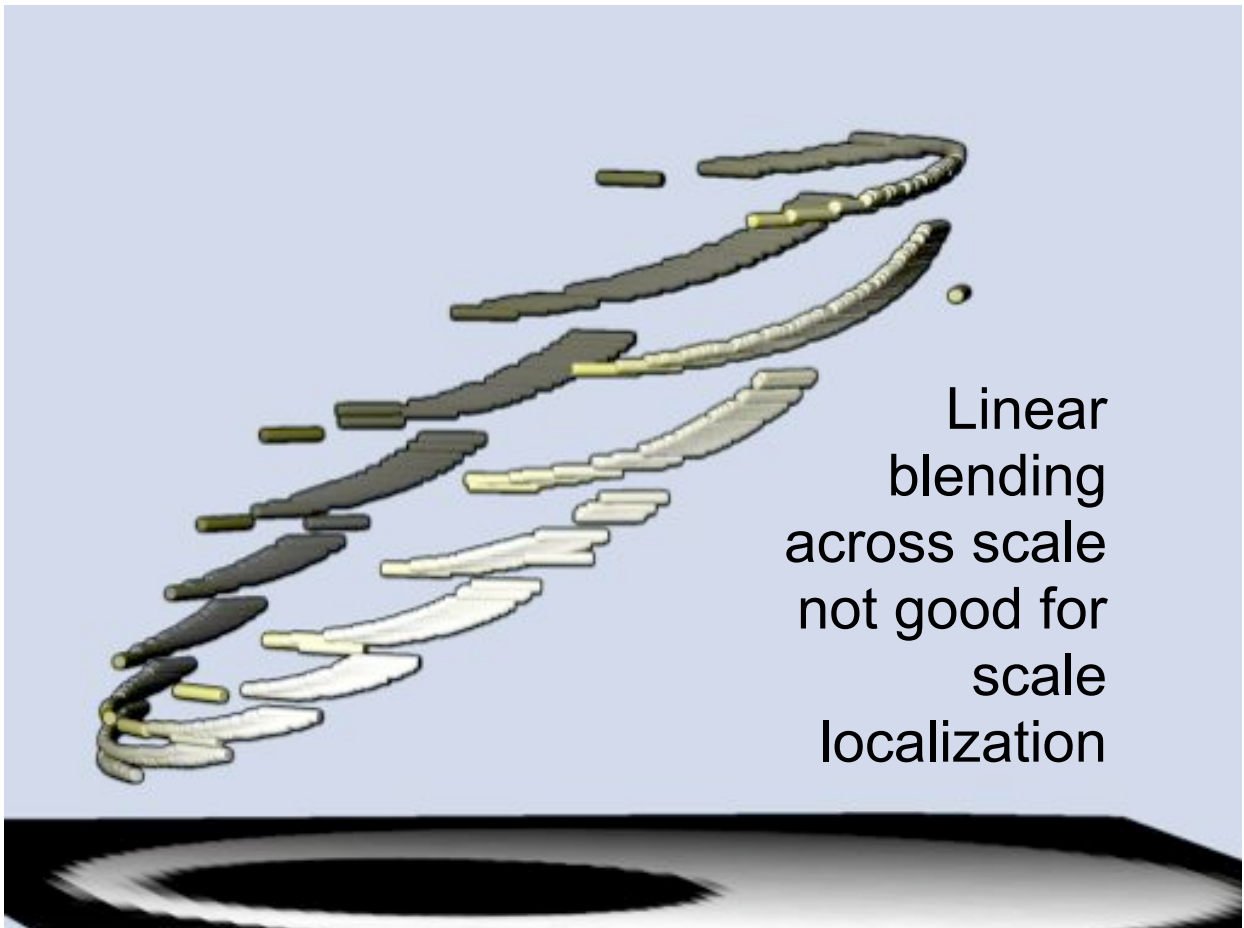
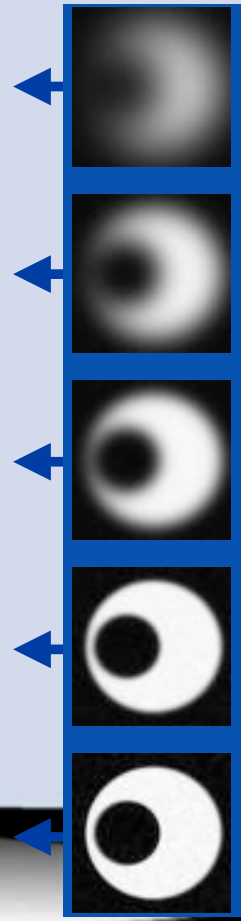




Particle-Image
energy as
function of
feature
strength



Hermite
spline
interpolation
across scale



Linear
blending
across scale
not good for
scale
localization

**The purpose is not images, its
feature sampling**

Glyphs
displaying
scale

Feature
localization and
sampling in
space and scale

