

Ways of seeing data: A survey of fields of visualization

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Nov 19, 2012 Part of the talk series “Show and Tell: Visualizing the Life of the Mind”
http://rcc.uchicago.edu/news/show_and_tell_abstracts.html



2012 Presidential Election

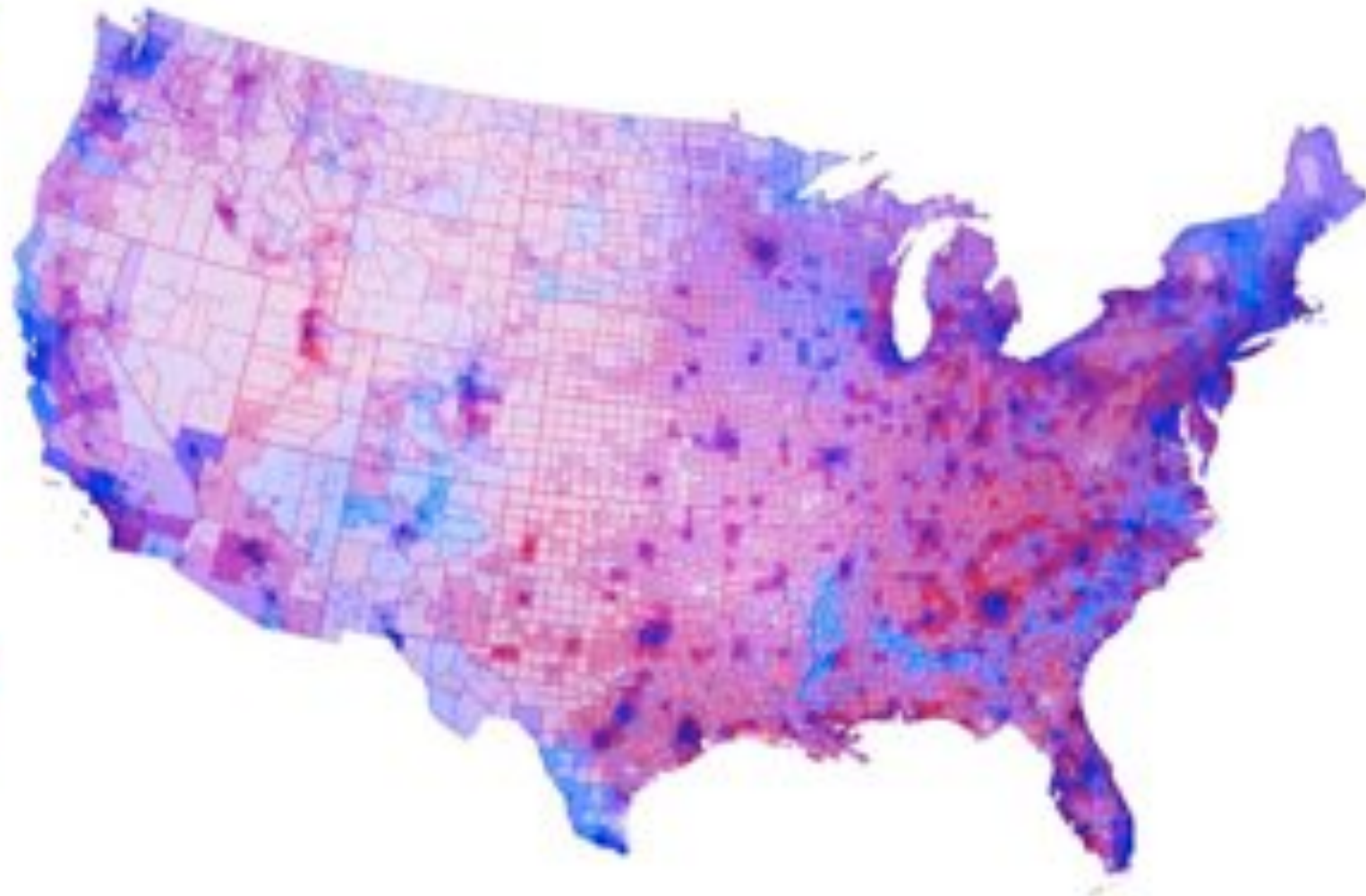
REPUBLICAN

DEMOCRAT



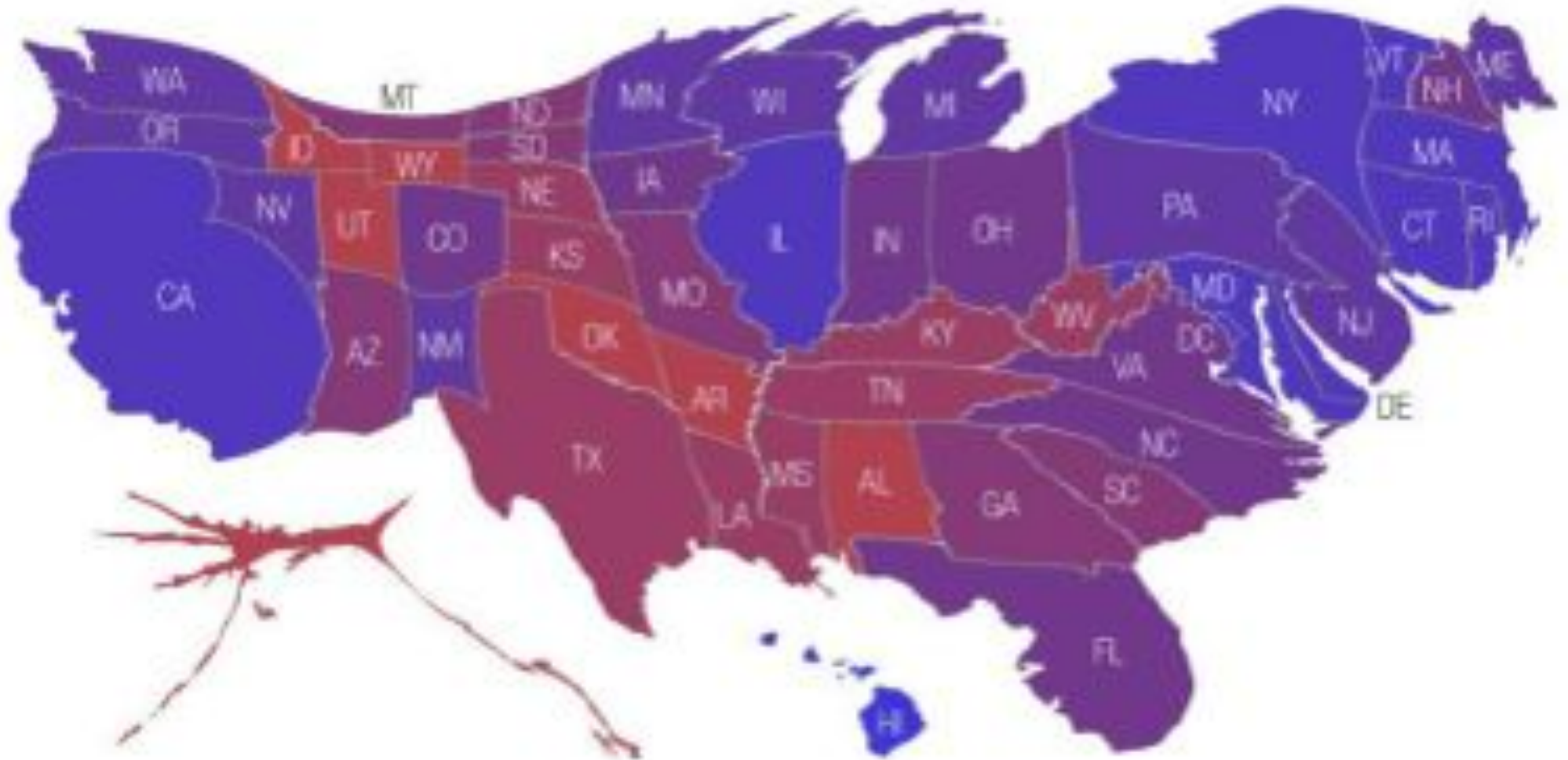
Adam Cook/WPI

2012 Presidential Election



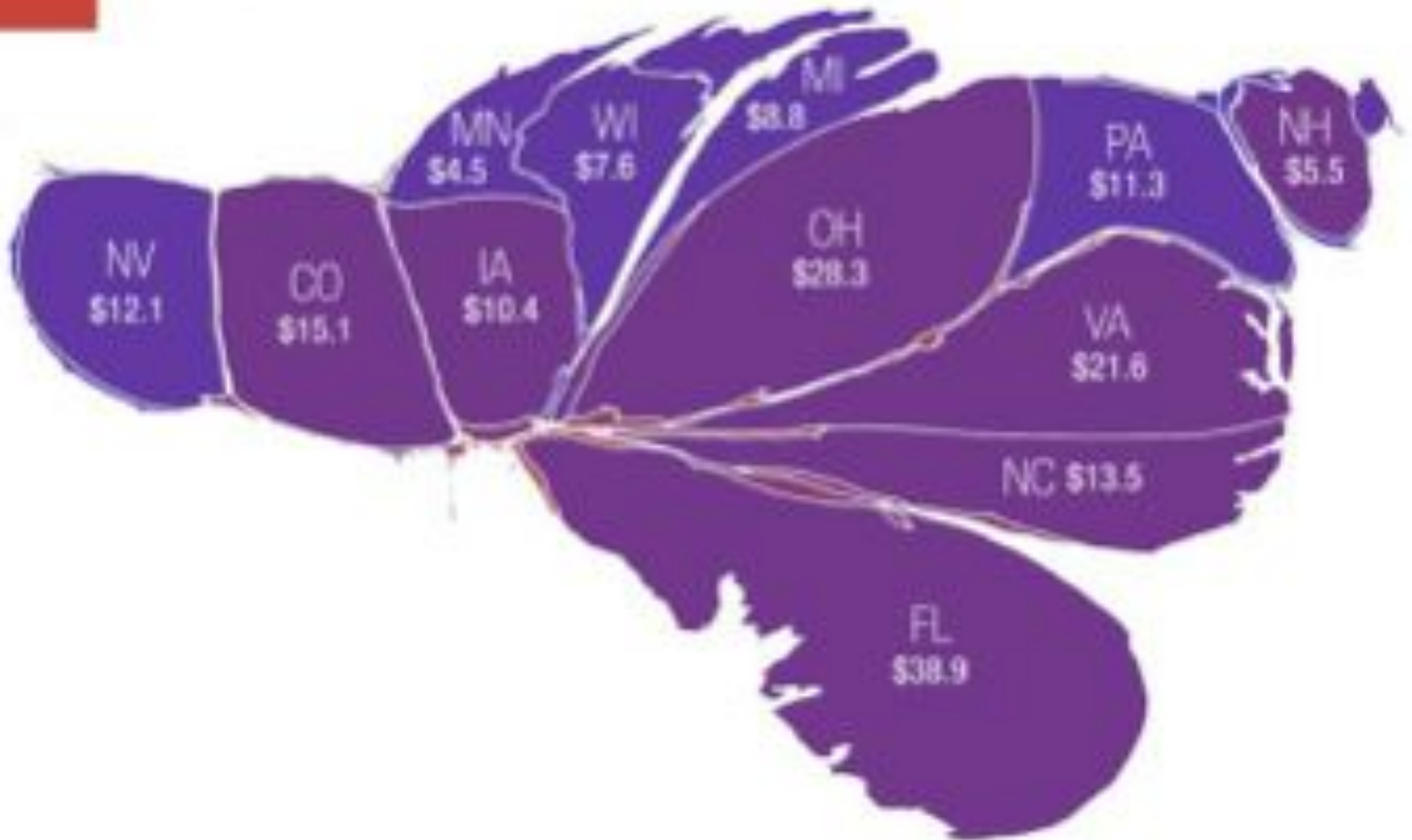
2012 Presidential Election

Electoral Votes



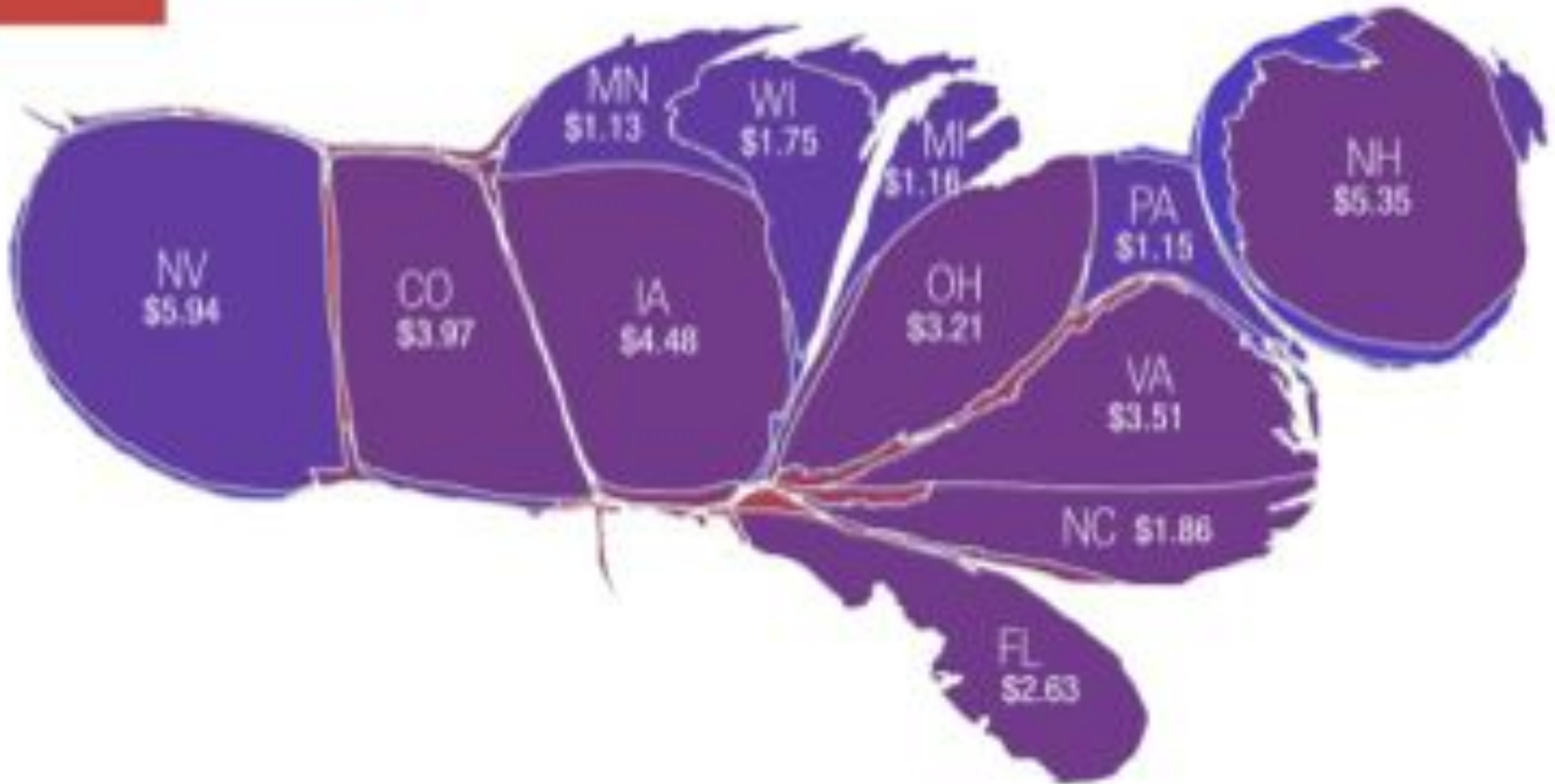
2012 Presidential Election

Ad Spending Per State In Millions Of Dollars



2012 Presidential Election

Ad Spending Per Voter In Dollars



Adam Cole/WPM

Clarifying distortions

Tube map from 1908



Clarifying distortions



Harry Beck 1933



<http://briankerr.wordpress.com/2009/06/08/connections/>
http://en.wikipedia.org/wiki/Harry_Beck

Clarifying distortions



Clarifying distortions



Joachim Böttger, Ulrik Brandes, Oliver Deussen, Hendrik Ziezold,
“Map Warping for the Annotation of Metro Maps”
IEEE Computer Graphics and Applications, 28(5):56-65, 2008

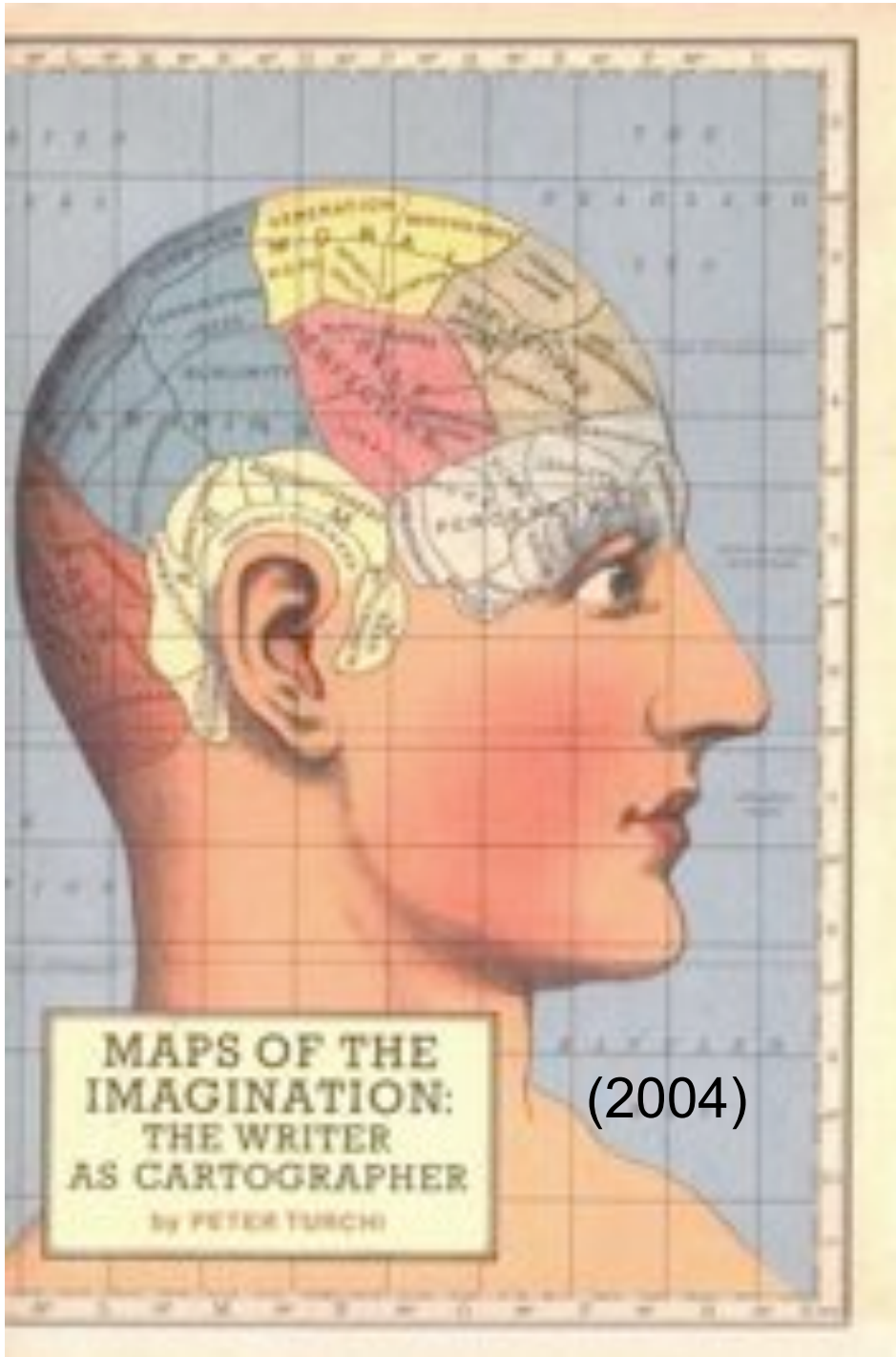
Maps reflect conventions, choices, and priorities



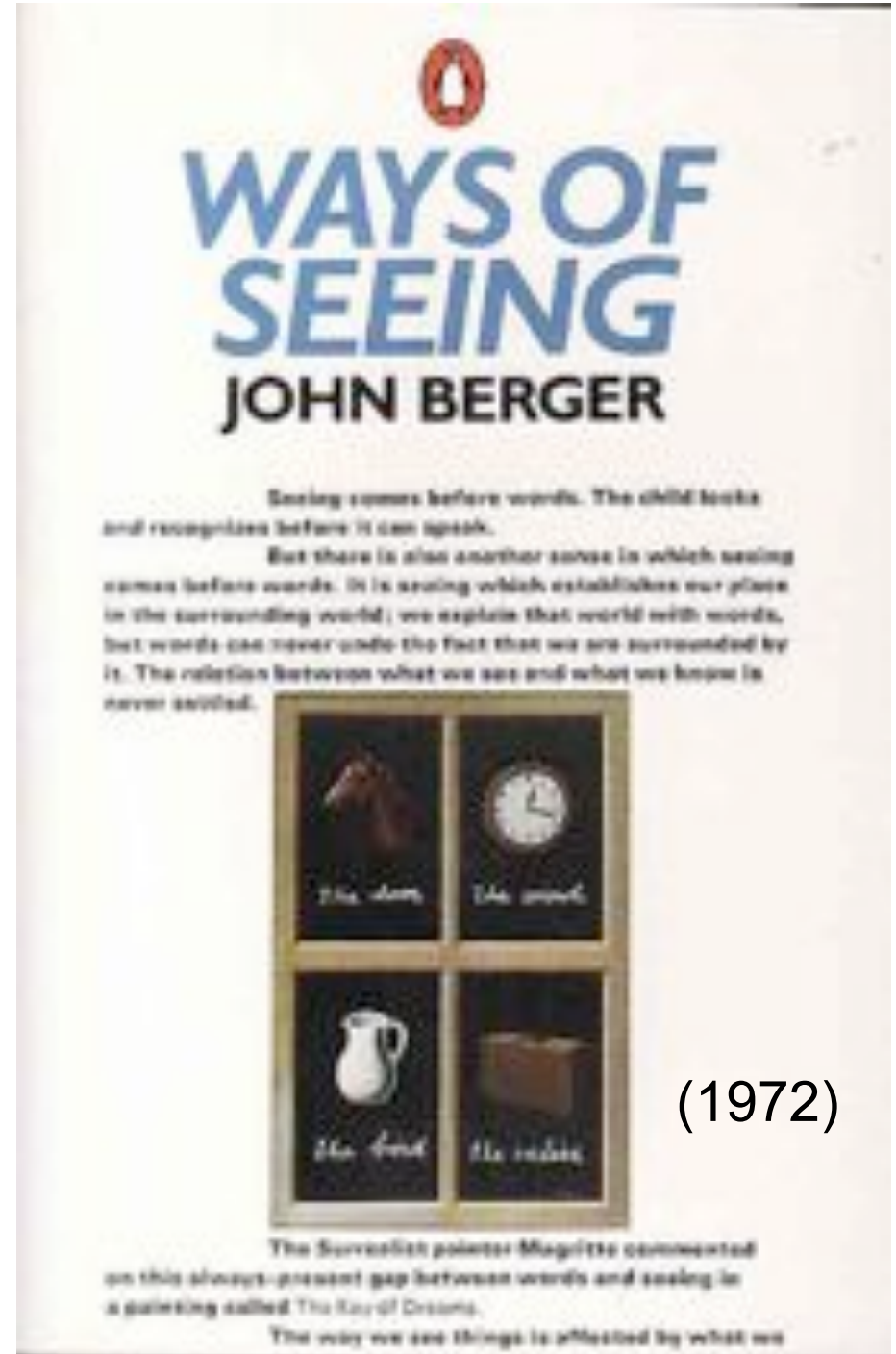
“A single map is but one of an indefinitely large number of maps that might be produced for the same situation or from the same data.”

Mark Monmonier “How to Lie with Maps”, 1991

Books that have influenced me



(2004)



(1972)

Fields of Visualization

Statistics,
Machine
Learning

Computer Science
Computer Graphics
Human-computer interaction
Perceptual Psychology

Calculus,
Numerical
Methods

Information
Visualization

Scientific
Visualization

Data Visualization

Info-
graphics

Scientific
Illustration

What is being visualized?

- Data = set of values (or datum) X
 - Spreadsheet: $\{X_i\}_{i=1..N}$; $X_i=(a_i,b_i,c_i,\dots)$
coordinates may be spatial or geographical
 - Function of time: $X = F(t)$
 - Function over 2D $X = F(u,v)$ i.e. an image,
or volume $F(u,v,w)$, or 3D surface $F(s,t)$
 - Graph: $X = (\text{Vert}, \text{Edge})$ or $(\text{Vert}, \text{Arrow})$
- Each X is a label or number (or vector of them)
- **Each different type (or flavor) of number has its own mathematical structure:**
“scales of measurement”

Scales of measurement

SCIENCE

Vol. 103, No. 2684

Friday, June 7, 1946

On the Theory of Scales of Measurement

S. S. Stevens

Director, Psycho-Acoustic Laboratory, Harvard University

FOR SEVEN YEARS A COMMITTEE of the British Association for the Advancement of Science debated the problem of measurement. Appointed in 1932 to represent Section A (Mathematical and Physical Sciences) and Section J (Psychology), the committee was instructed to consider and report upon the possibility of "quantitative estimates of sensory events"—meaning simply: Is it possible to measure human sensation? Deliberation led only to disagreement, mainly about what is meant by the term measurement. An interim report in 1938 found one member complaining that his colleagues

by the formal (mathematical) properties of the scales. Furthermore—and this is of great concern to several of the sciences—the statistical manipulations that can legitimately be applied to empirical data depend upon the type of scale against which the data are ordered.

A CLASSIFICATION OF SCALES OF MEASUREMENT

Paraphrasing N. R. Campbell (Final Report, p. 340), we may say that measurement, in the broadest sense, is defined as the assignment of numerals to objects or events according to rules. The fact that numerals can be assigned under different rules leads

Stevens' 4 scales of measurements

http://en.wikipedia.org/wiki/Level_of_measurement

Scale	Basic Empirical Operations	Mathematical Group Structure	Permissible Statistics (invariantive)
Nominal Categorical Qualitative	Determination of equality	Permutation group $x' = f(x)$ $f(x)$ means any one-to-one substitution	Number of cases Mode Contingency correlation
Ordinal	Determination of greater or less	Isotonic group $x' = f(x)$ $f(x)$ means any monotonic increasing function	Median Percentiles
Interval	Determination of equality of intervals or differences	General linear group $x' = ax + b$	Mean Standard deviation Rank-order correlation Product-moment correlation
Ratio	Determination of equality of ratios	Similarity group $x' = ax$	Coefficient of variation

Later scales specialize earlier scales

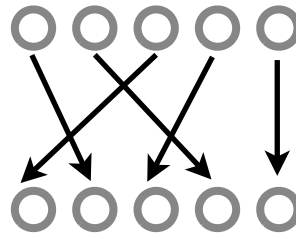
Some examples of these ...

The structure of data values

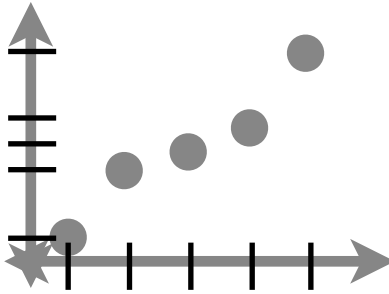
discrete

quali-
tative

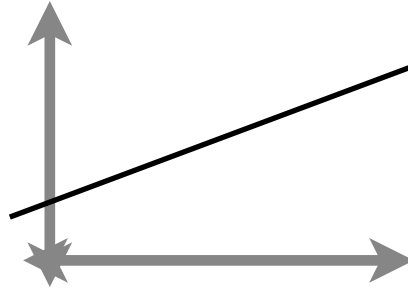
Categorical



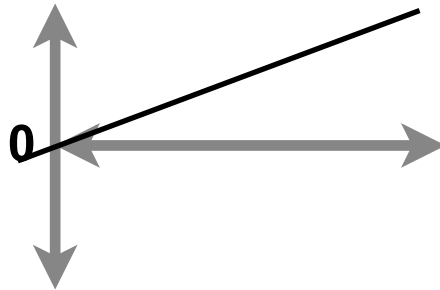
Ordinal



Interval



Ratio



Understanding the nature of the data helps choose sensible ways to show it

continuous

quantitative

Scalars

Vectors

Tensors

Symmetries and visualization

Symmetry of data: $D = T(D)$

nominal: permutation

ordinal: any monotonic function

interval: affine transform: $y = ax + b$ ($a > 0$)

ratio: $y = ax$ ($a > 0$)

Visualization: $V(D)$

V maps from data D to image or image property

colormaps: assignment of colors to values

We will look at multiple examples of these

Keep in mind: $V = V(D, P)$ for parameter set P

Symmetries and visualization

Basic idea: Visualization should reflect the symmetries and preserve structure in data

$$\mathbf{D} = \mathbf{T}(\mathbf{D}) \Leftrightarrow \mathbf{V}(\mathbf{D}) \approx \mathbf{V}(\mathbf{T}(\mathbf{D}))$$

$$-\mathbf{D} = \mathbf{T}(\mathbf{D}) \Leftrightarrow -\mathbf{V}(\mathbf{D}) \approx \mathbf{V}(\mathbf{T}(\mathbf{D}))$$

$$\mathbf{D}_1 = \mathbf{D}_2 \Leftrightarrow \mathbf{V}(\mathbf{D}_1) = \mathbf{V}(\mathbf{D}_2)$$

$$\mathbf{D}_1 < \mathbf{D}_2 \Leftrightarrow \mathbf{V}(\mathbf{D}_1) < \mathbf{V}(\mathbf{D}_2)$$

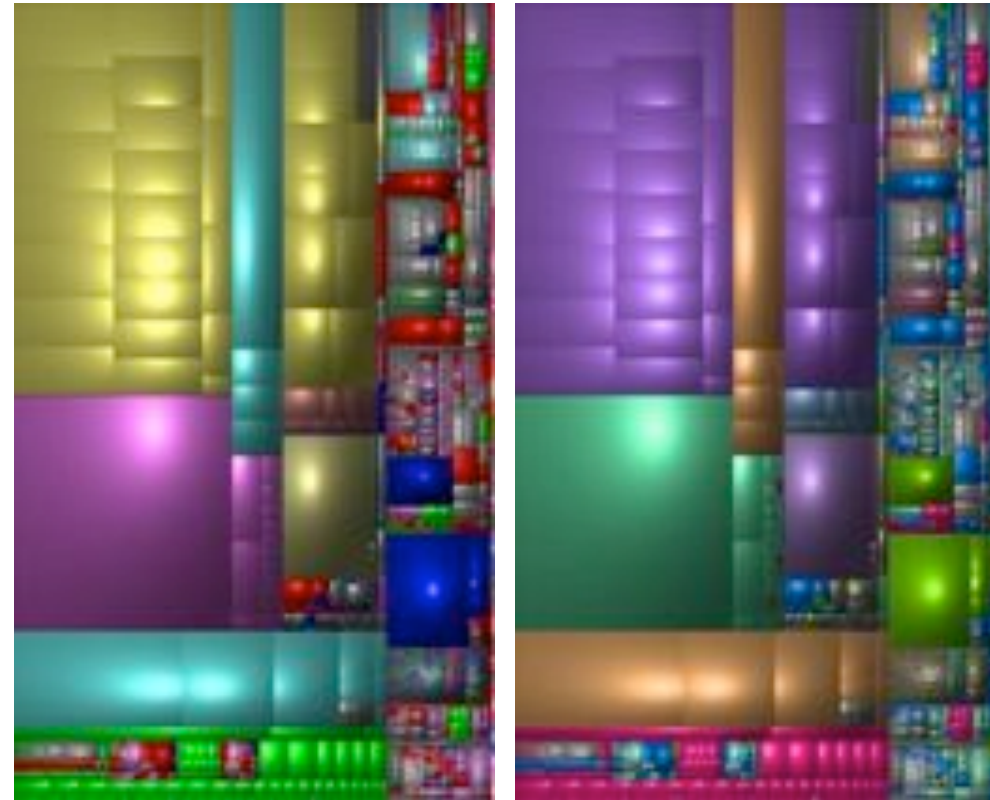
Applies to computational representation of measurements, and to other quantities:

Debugging by symmetry

Colormap for categorical data

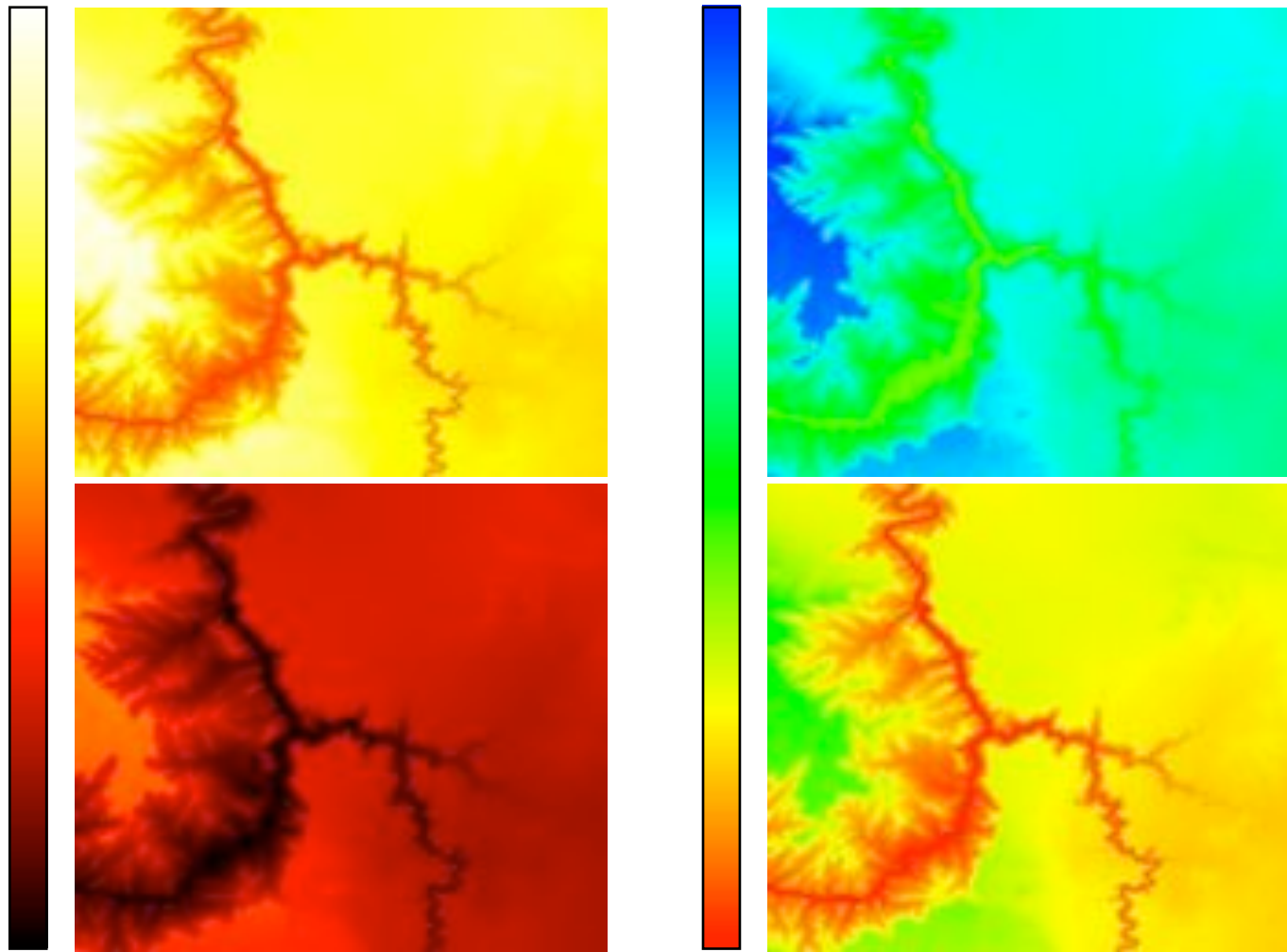


Coloring different types of files (MP3, JPG, TIFF, applications, etc)



Coloring (or effectiveness of coloring) of categorical values should be symmetric under permutation

Colormap for interval data



$$V(D + c) \approx V(D) \quad V(D + c) \neq V(D)$$

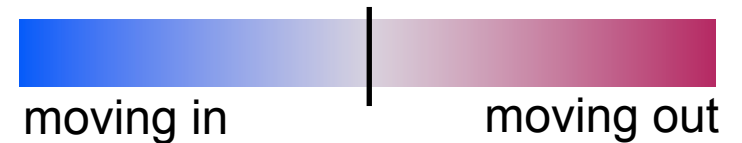
Coloring of **interval** values should be symmetric under addition of constant (can convey intrinsic **ordering**)

Ratio data: Population change

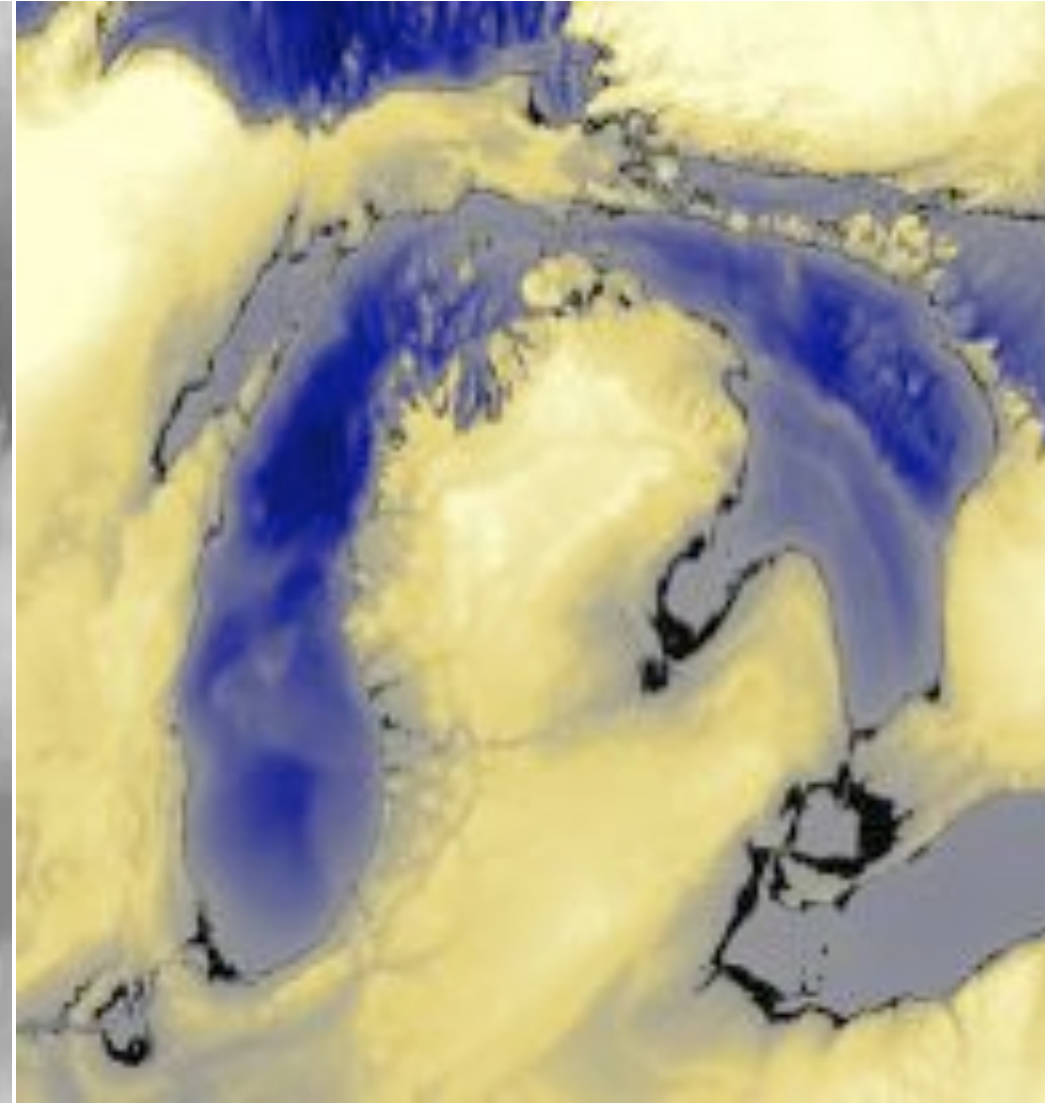
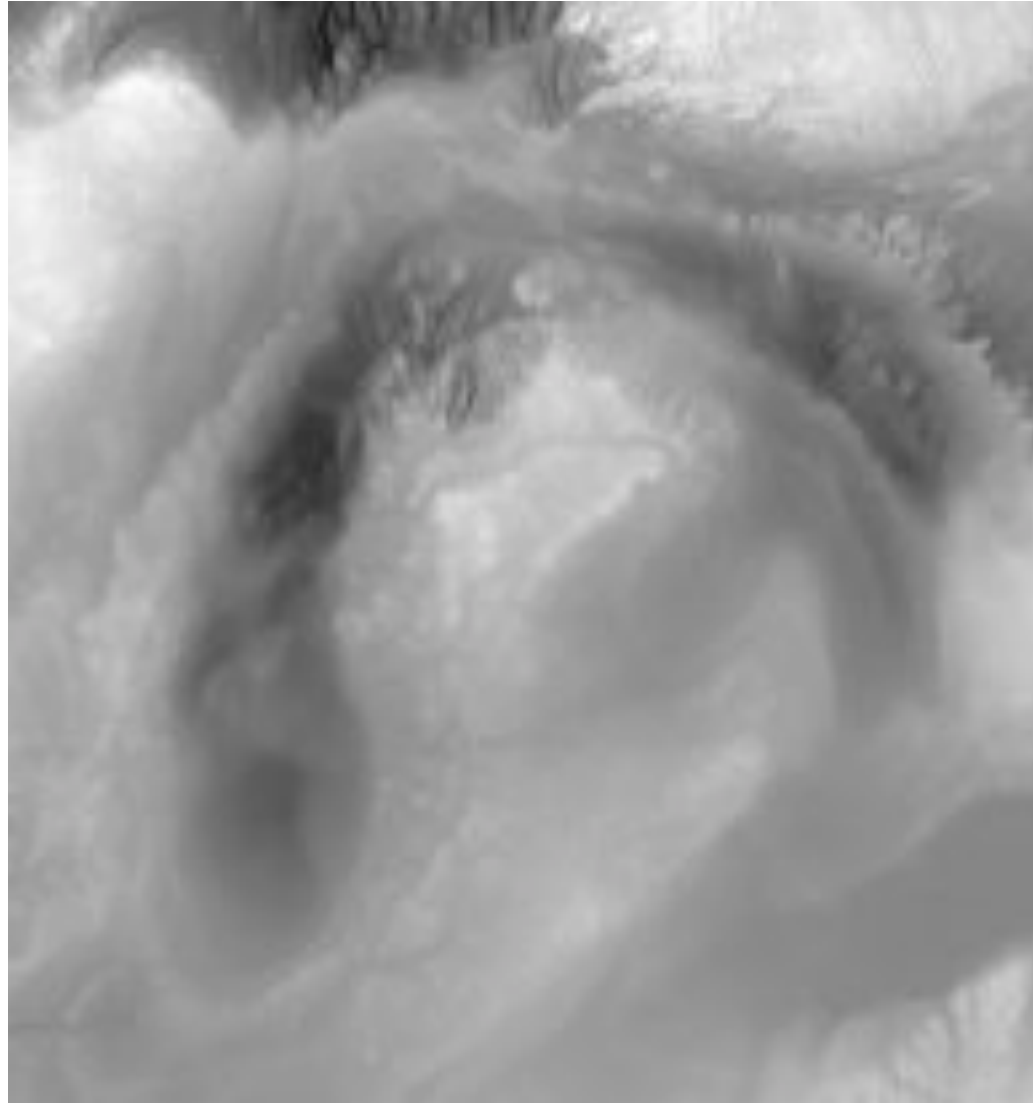
$$T(D) \approx -D \Rightarrow V(T(D)) \approx -V(D)$$

Coloring values with meaningful **zero** should be anti-symmetric under negation (reflection) \Rightarrow

Special color for zero



Value of showing isocontours



What colormap to use?

Data symmetries can inform colormap choices

Should know which “scale” (of 4) your data is

Is there ordering? (is the order crucial?)

Is there a zero? (is showing sign of values crucial?)

Two common tasks

Picking off values at particular locations

(in nominal data: identifying category)

Showing over-all form: depends on **ordering**

Or some balance of both

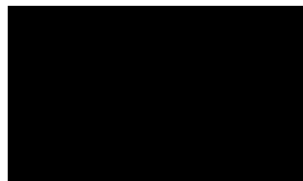
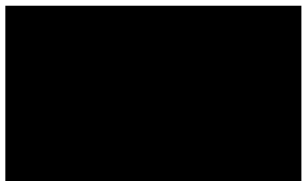
What attributes of color are ordered?

Ordering of color axes

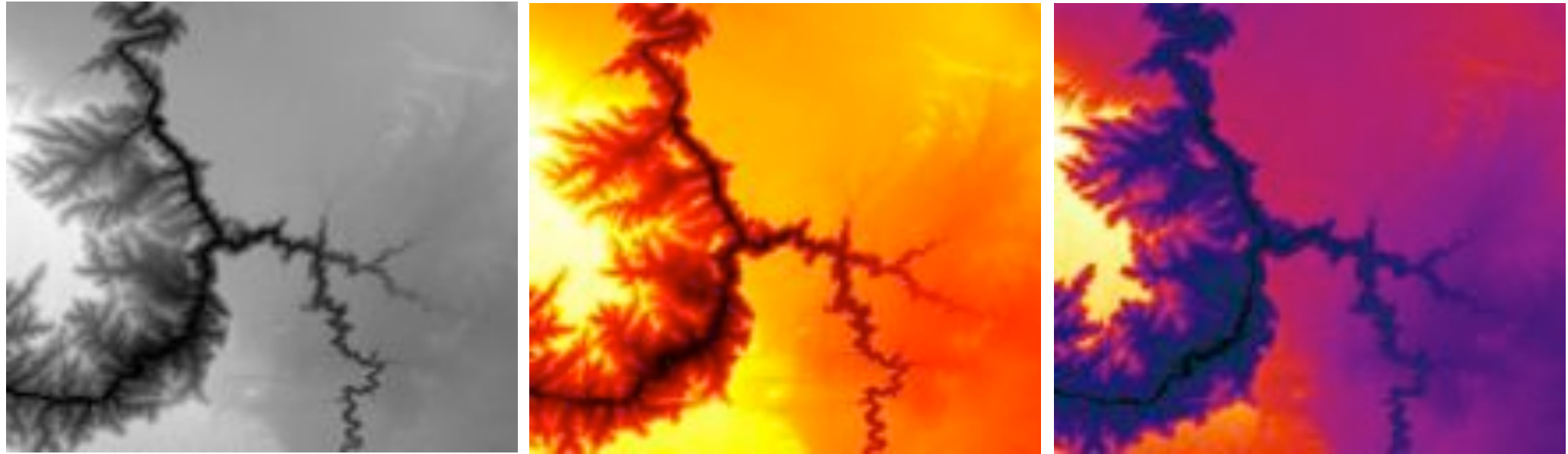
Brightness

Saturation

Hue: not as much



Strategy: combine hue and luminance



Shows basic height relationships

And helps for distant comparisons

Common technique in scientific visualization

Drawback: luminance not free for shading

Fields of Visualization related to data

Information Visualization

$$\{X_i\}_{i=1..N}; X_i=(a_i, b_i, c_i, \dots)$$

$$X = F(t)$$

$$X = (\text{Vert}, \text{Edge})$$

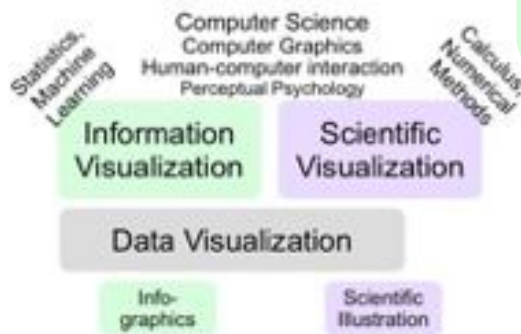
$$X = F(u, v)$$

$$X = F(u, v, w)$$

$$X = F(s, t) \quad (3D \text{ surface})$$

X : vectors, tensors

Scientific Visualization



Fields of Visualization

Information
Visualization

Scientific
Visualization

Data Visualization

Info-
graphics

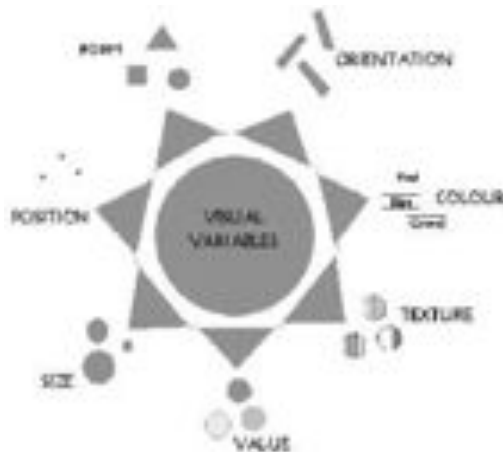
Scientific
Illustration

How to visually encode information?

Jacques Bertin:
French
cartographer

1918 – 2010

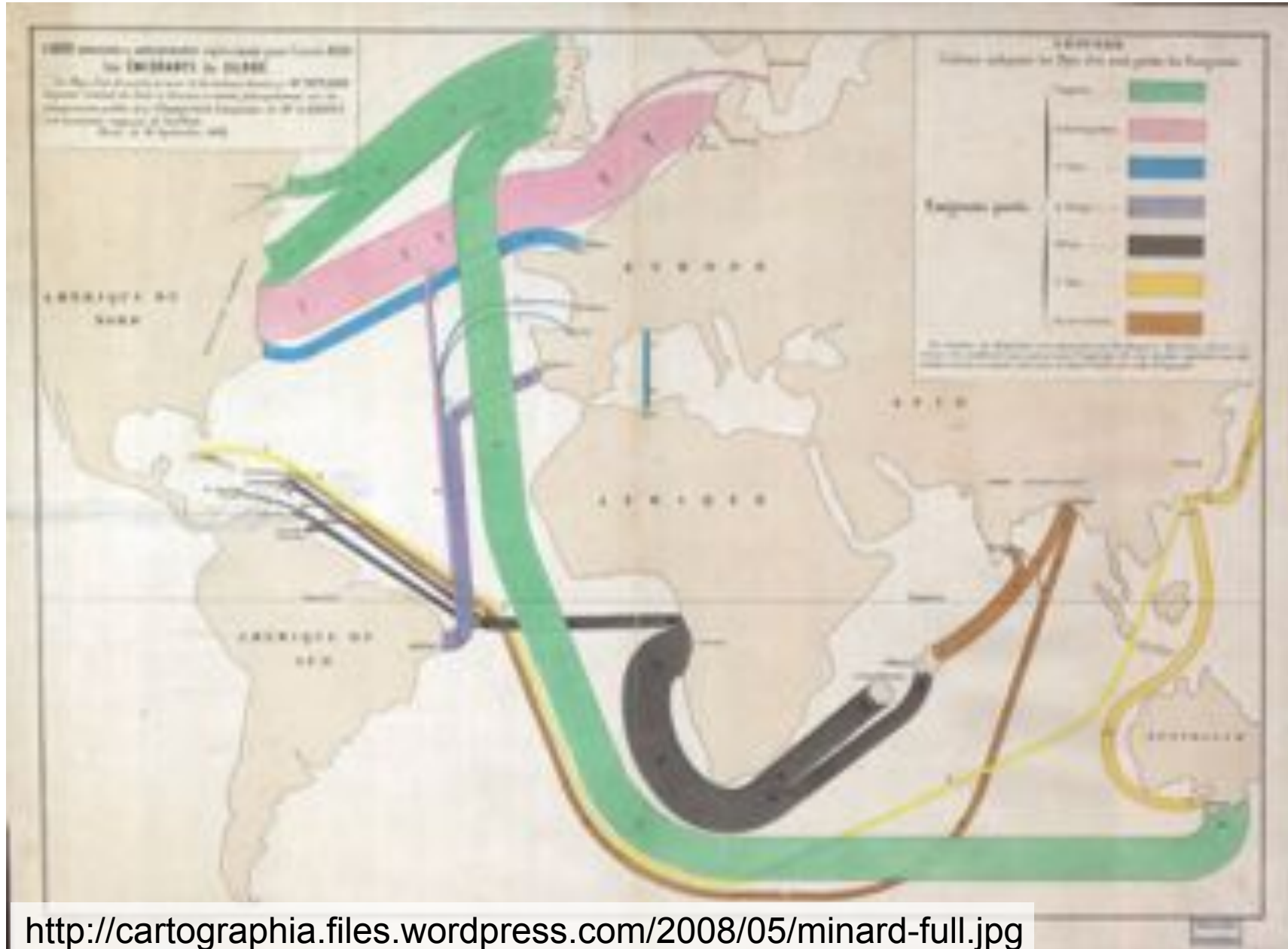
“Semiology
of Graphics”



	<i>Points</i>	<i>Lines</i>	<i>Areas</i>	<i>Best to show</i>
<i>Shape</i>		<i>possible, but too weird to show</i>	cartogram	<i>qualitative differences</i>
<i>Size</i>			cartogram	<i>quantitative differences</i>
<i>Color Hue</i>				<i>qualitative differences</i>
<i>Color Value</i>				<i>quantitative differences</i>
<i>Color Intensity</i>				<i>qualitative differences</i>
<i>Texture</i>				<i>qualitative & quantitative differences</i>

Charles Joseph Minard (1781 – 1870)

Amount and destinations of emigrants from Europe, Africa, China, and South Asia for the year 1858



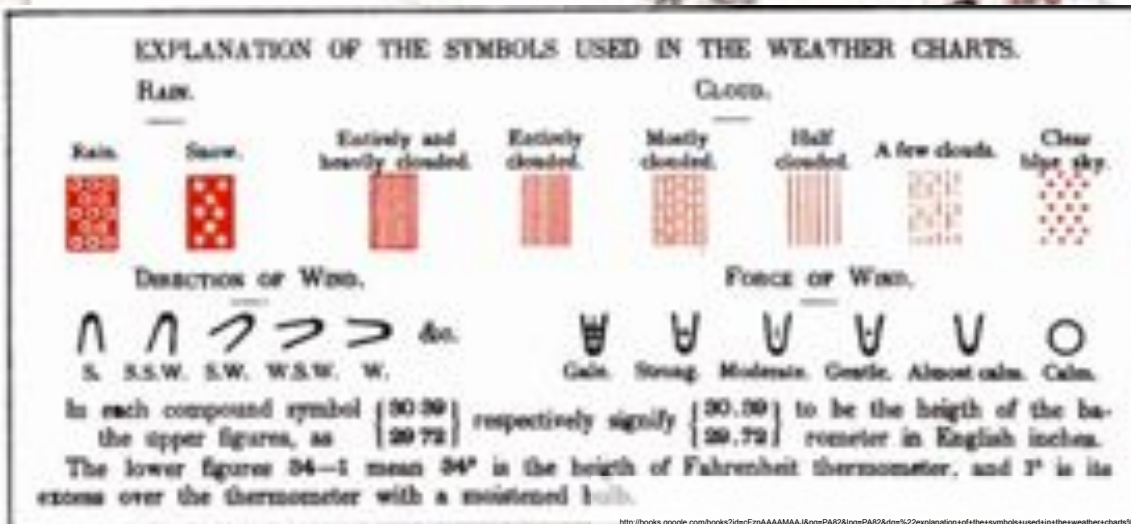
Multi-variate glyphs (or icon)

Francis Galton
(1822 –1911)

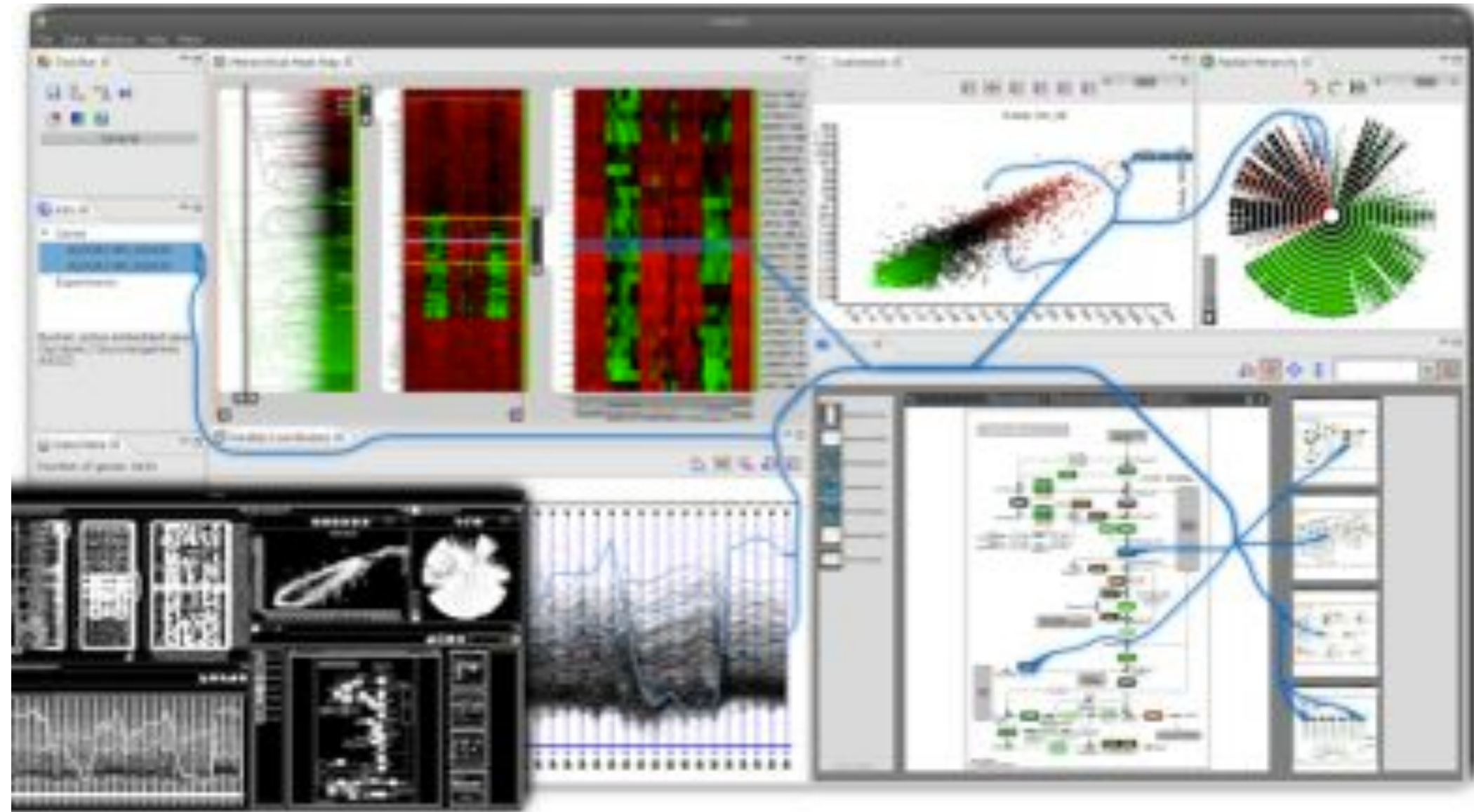
Glyphs shows wind force and direction, cloud, precipitation

Aided in discovery of anti-cyclones

Learn more at
Michael Friendly's
“Milestones
Project”: <http://www.datavis.ca/milestones/>



Linking multiple views



Markus Steinberger, Manuela Waldner, Marc Streit, Alexander Lex, and Dieter Schmalstieg. **Context-Preserving Visual Links**. IEEE Transactions on Visualization and Computer Graphics 17(12):2249-2258, 2011

Fields of Visualization

Information
Visualization

Scientific
Visualization

Data Visualization

Info-
graphics

Scientific
Illustration

Main Data types

Scalar (e.g. Temperature, Pressure, Density, Intensity)

Vector (e.g. Velocity of flow, displacement in deformation)

Tensor (e.g. Jacobian of flow, Diffusion, Stress)

Data types vs attributes

Attributes: Scalar Vector Tensor

Data: Scalar			
Vector			
Tensor			

Data types vs attributes

Attributes: Scalar Vector Tensor

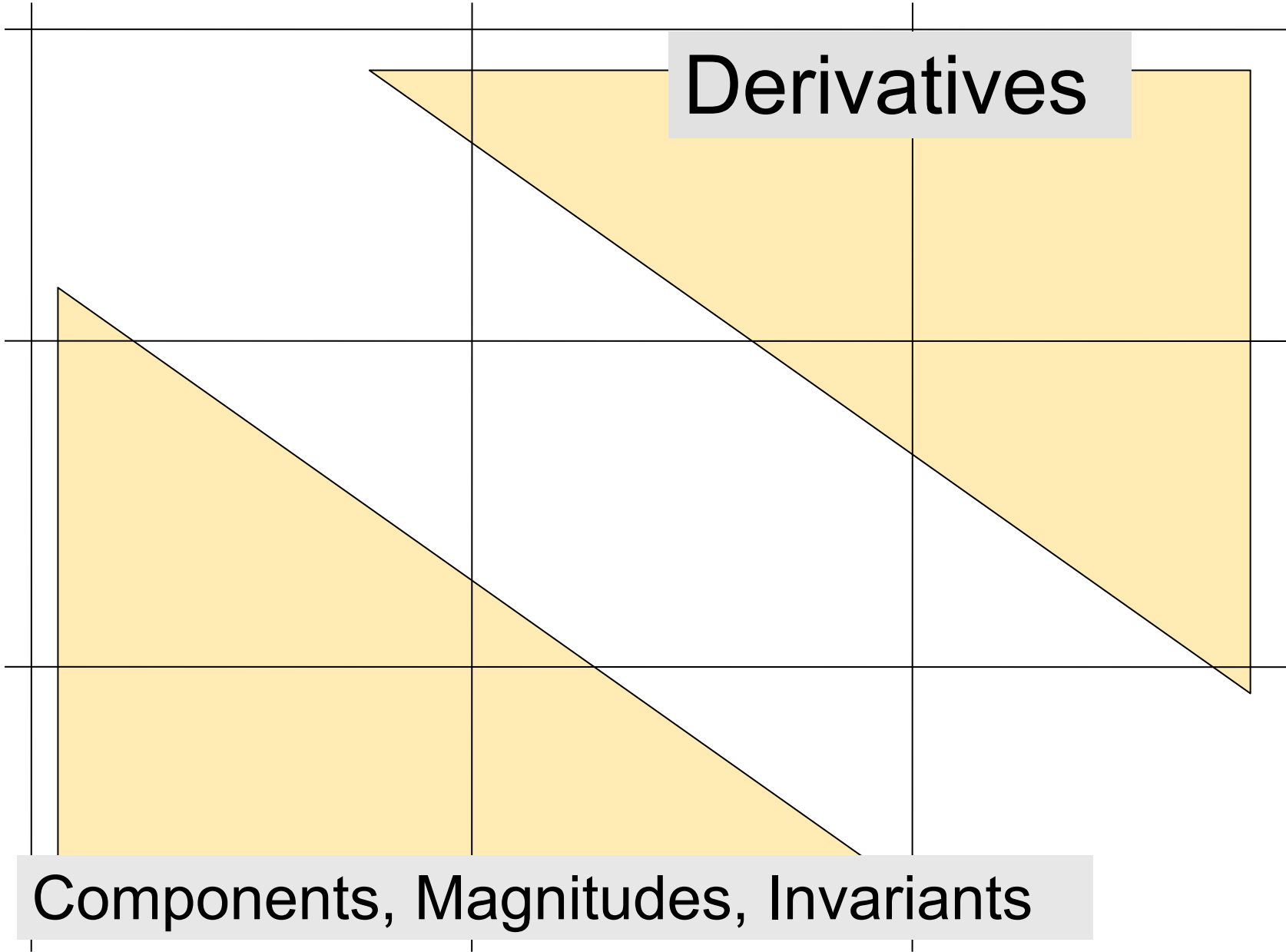
Data:
Scalar

Vector

Tensor

Derivatives

Components, Magnitudes, Invariants



Data types vs attributes

Attributes: Scalar Vector Tensor

Data:
Scalar

Derivatives

Gradient

Hessian,
curvature

Vector

Magnitude
(e.g. speed)

Jacobian

Tensor

Eigenvalues,
Invariants

Eigenvectors

Components, Magnitudes, Invariants

Simple example

Attributes: Scalar

Vector

Tensor

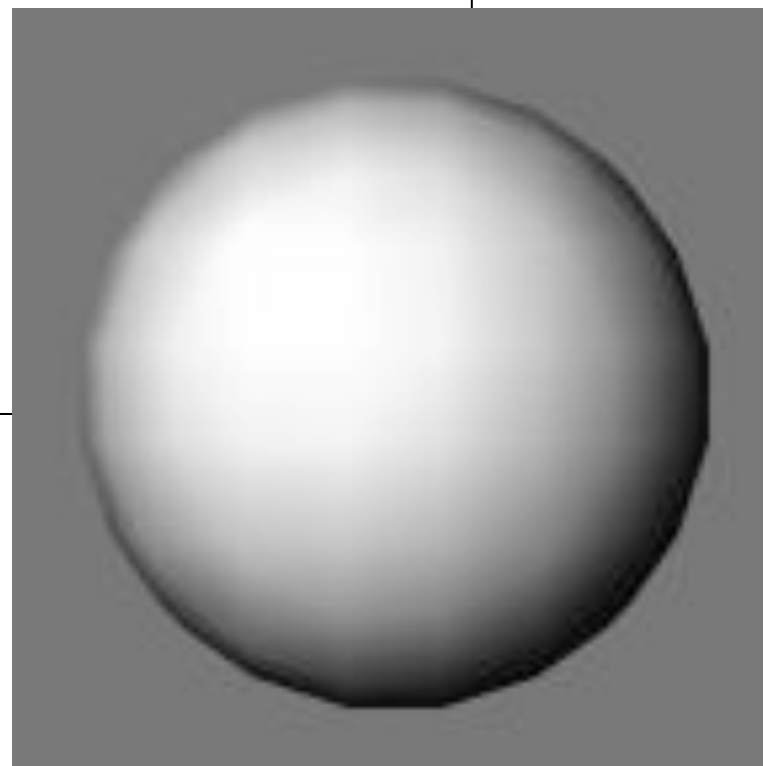
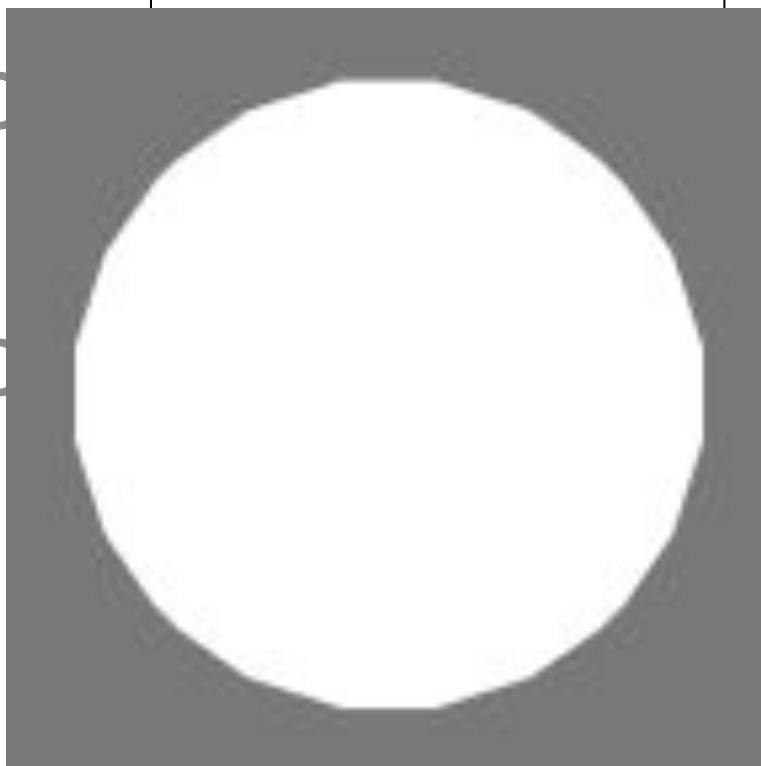
Data:
Scalar

Data itself:
Isocontours

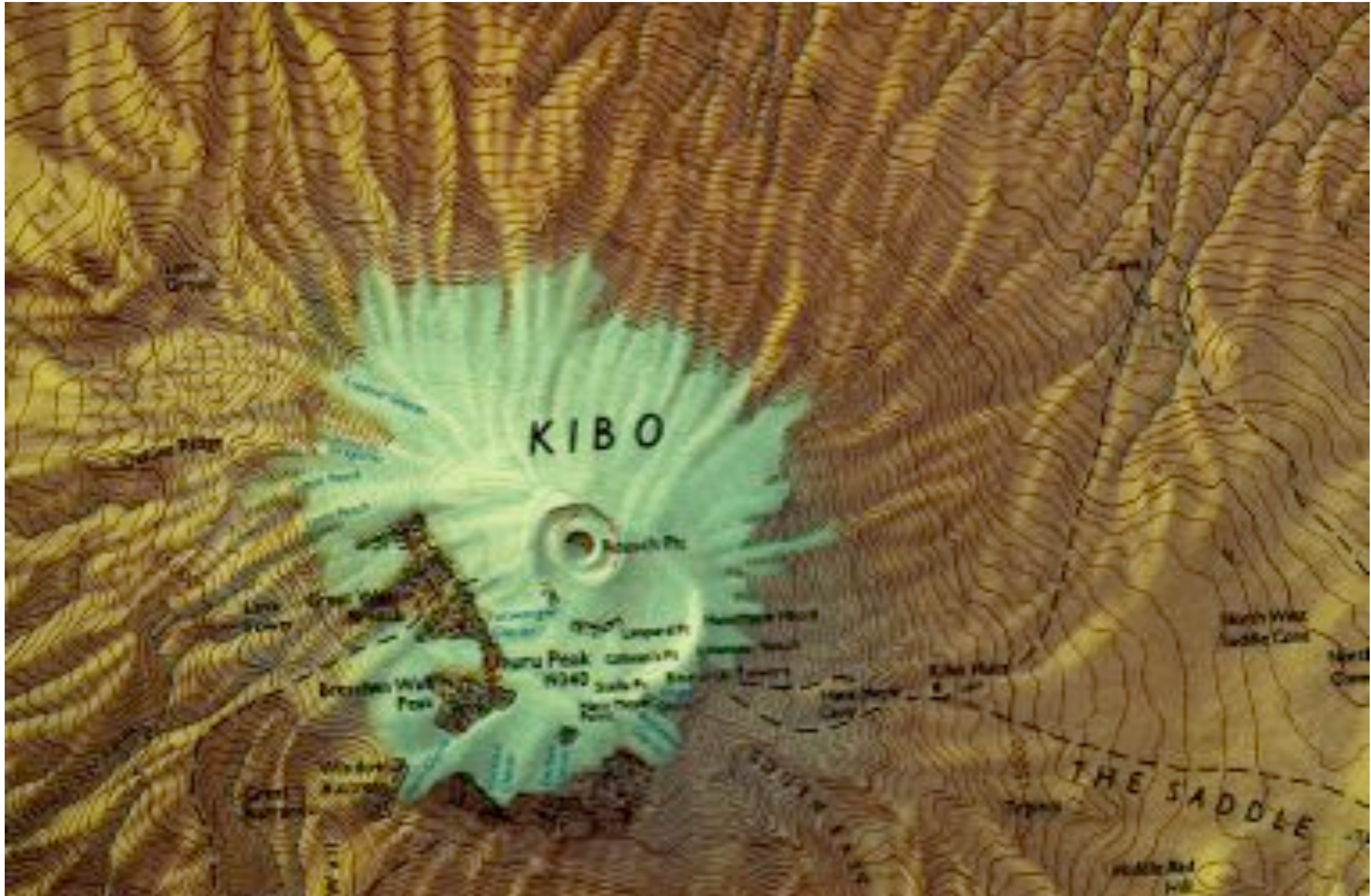
Gradient:
Surface
shading

Vector

Tensor

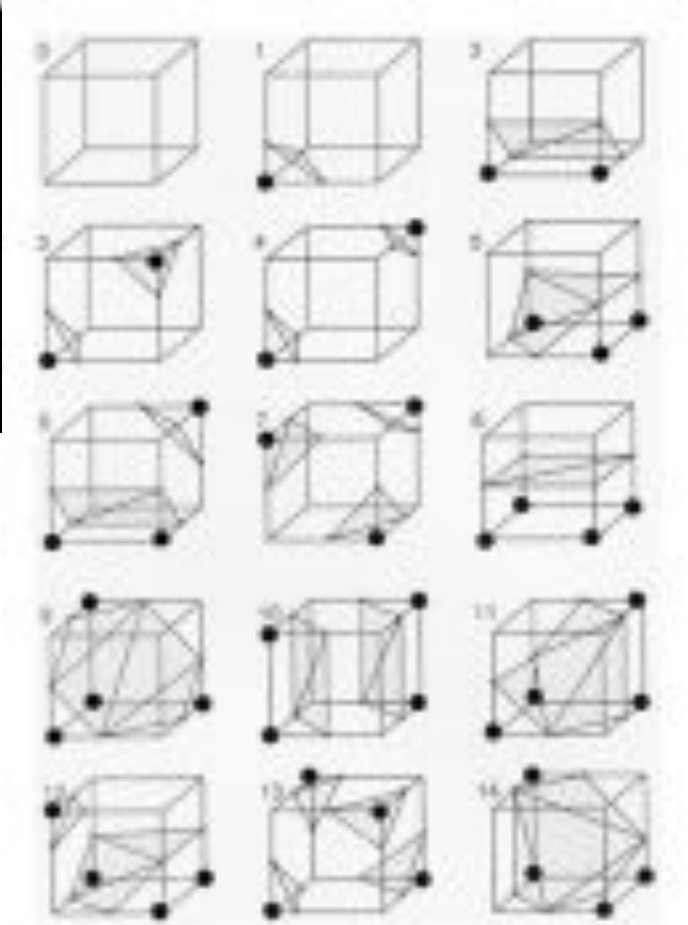
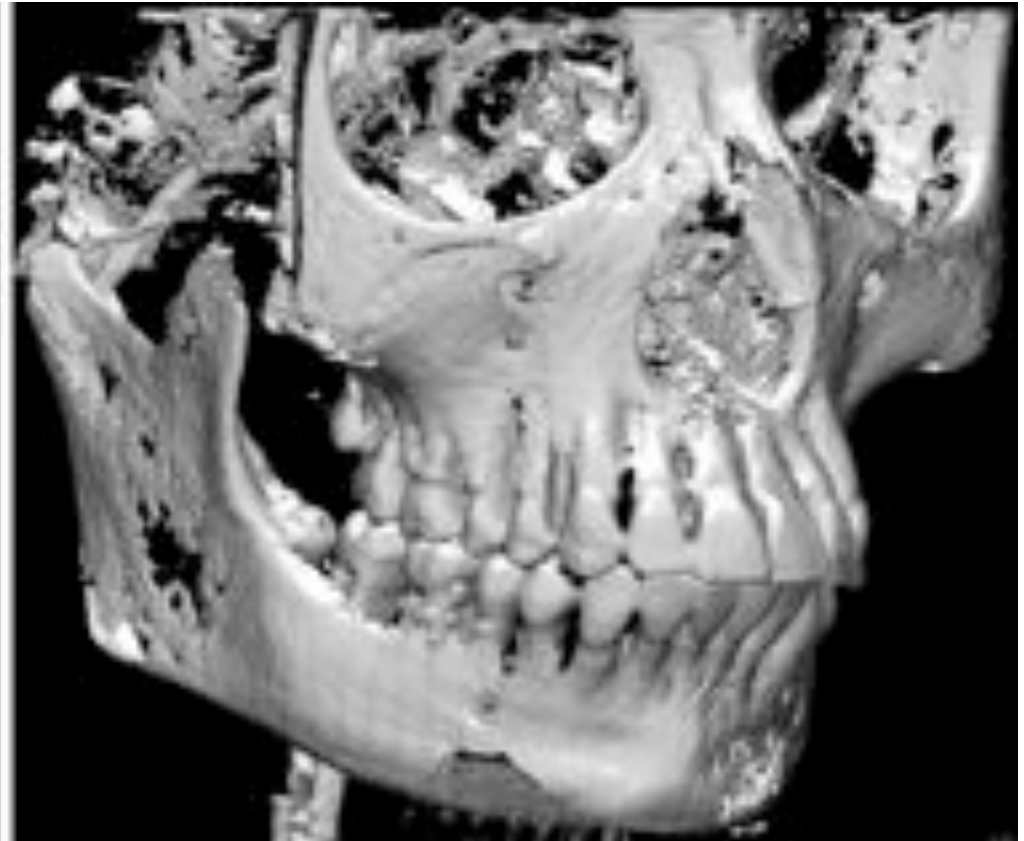
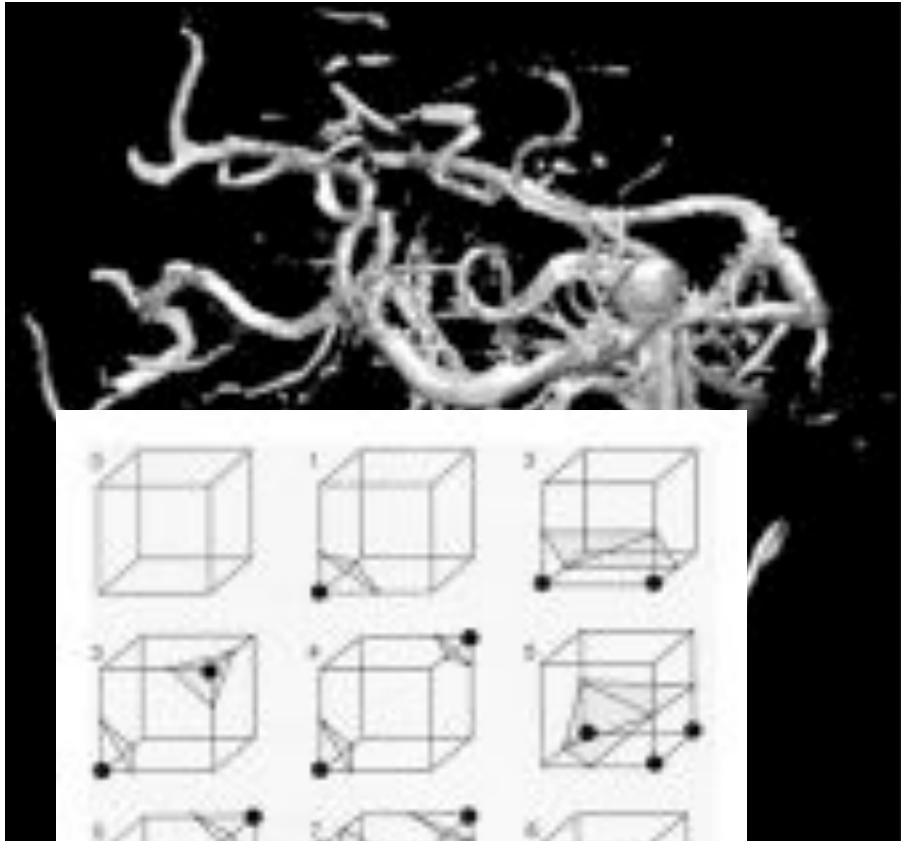


Isocontours on a topo map



<http://cluster3.lib.berkeley.edu/EART/tour/topo.html>
<http://cluster3.lib.berkeley.edu/EART/tour/tanzania100k.gif>

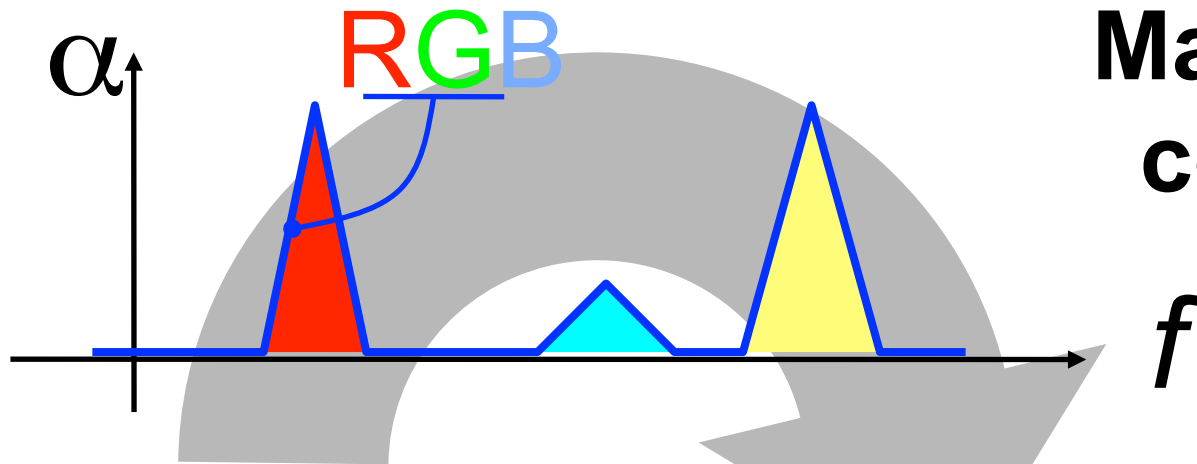
3D Isocontours



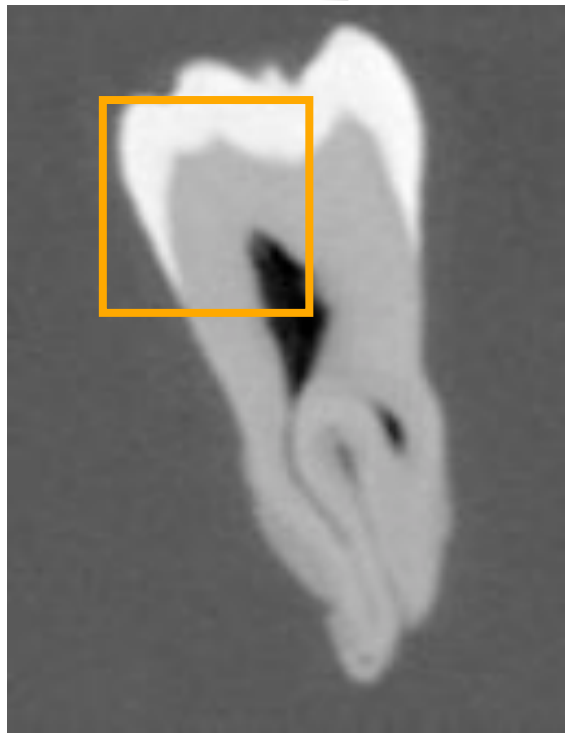
<http://www.thebigblob.com/marching-cubes-implementation-using-opengl-and-opengl/>

William E. Lorensen and William E. Cline, **Marching Cubes: A High Resolution 3D Surface Construction Algorithm**. *Computer Graphics*, 1987, 21, 163-169

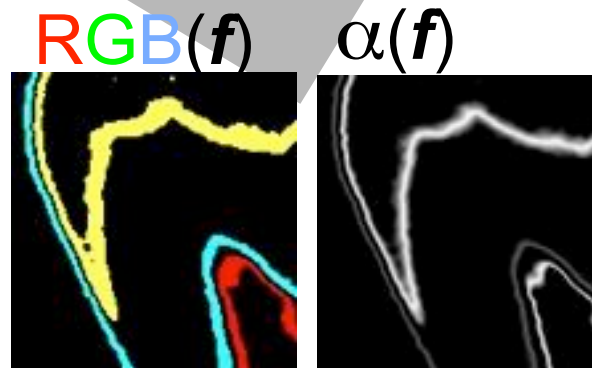
Direct Volume Rendering



Map data value f to
color and opacity



Human Tooth CT

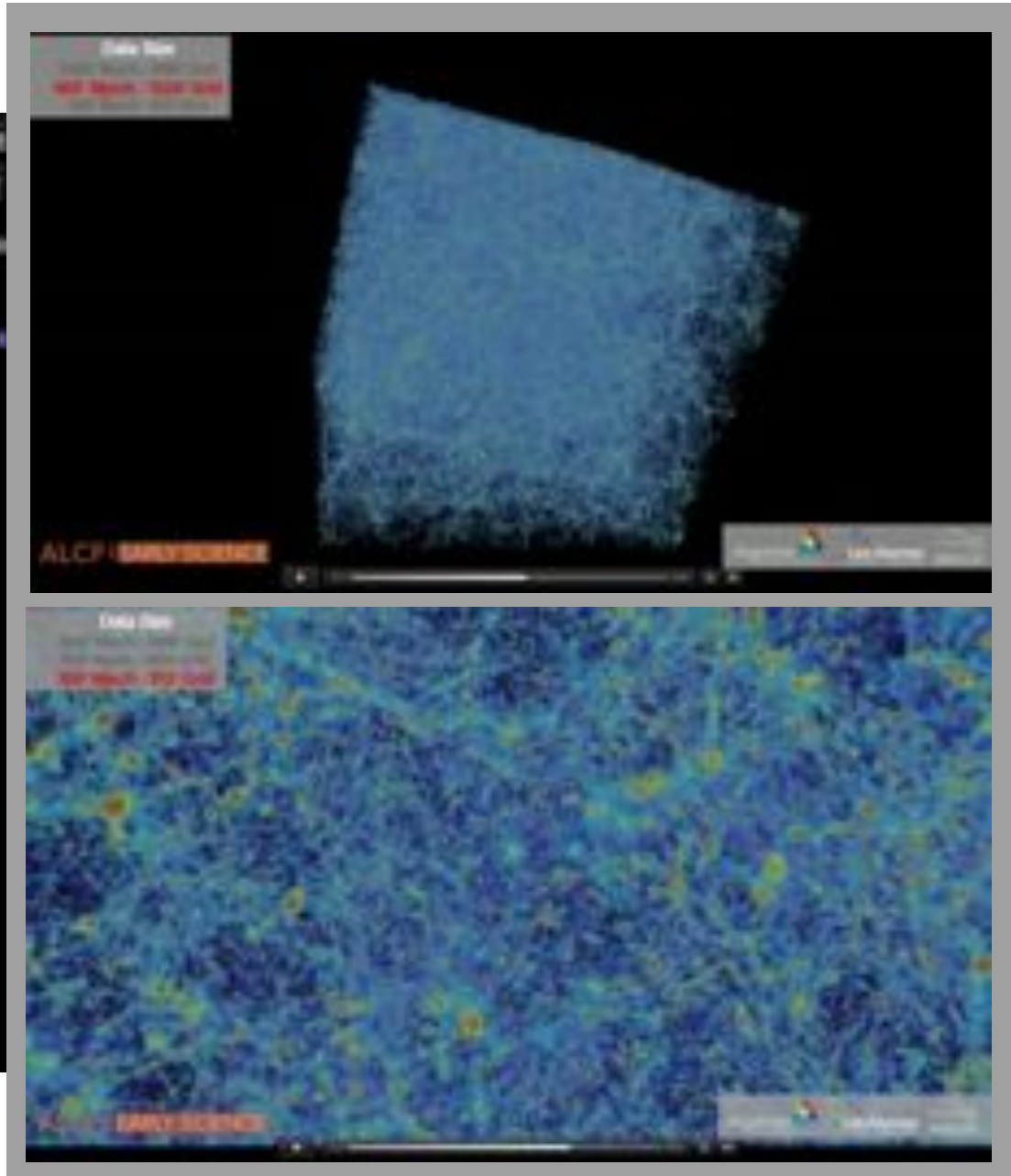


Shading with ∇f ,
Compositing...



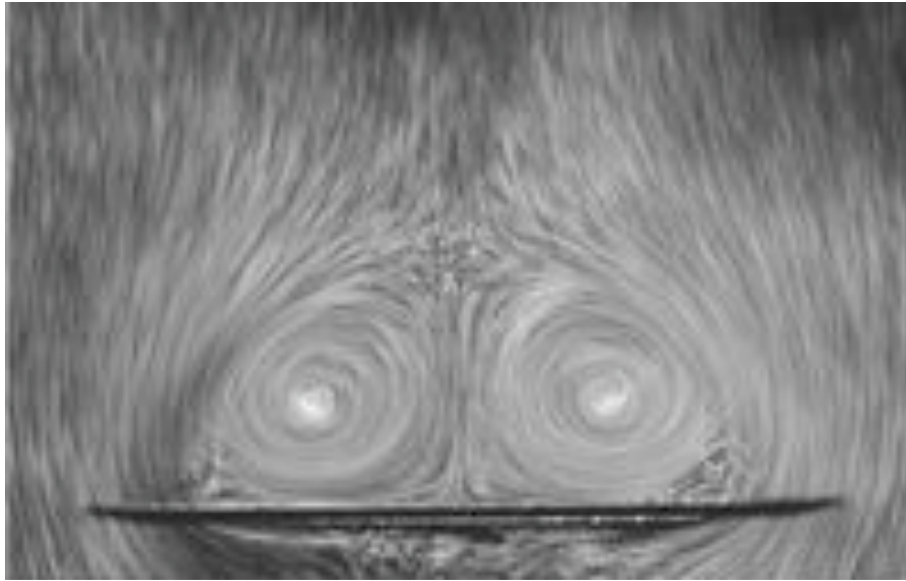
Volume rendering applications

https://commons.wikimedia.org/wiki/File:Fetal_yawning_4D_ultrasound_ecografia_4D_Dr._Wolfgang_Moroder.theora.ogv



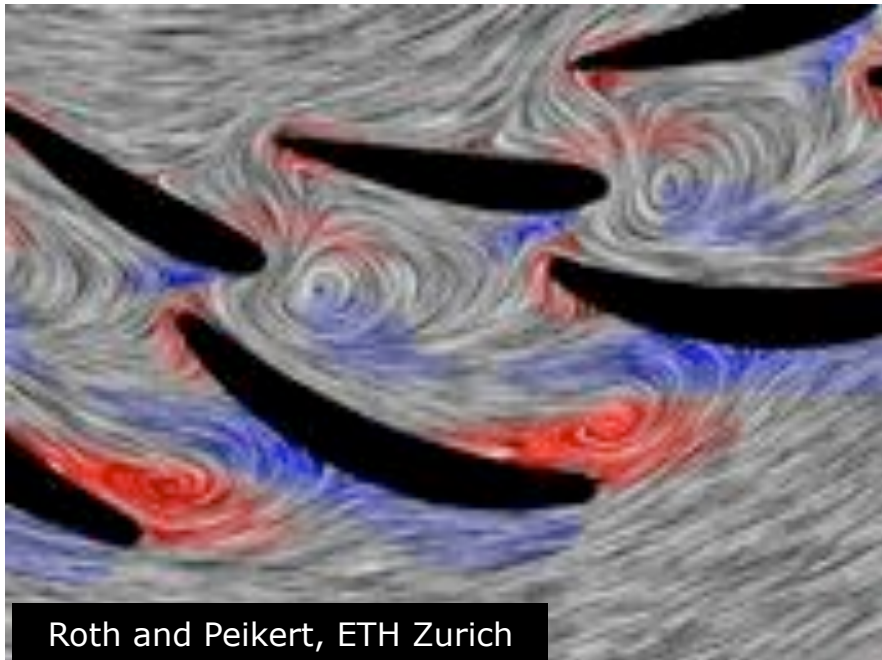
<http://www.popsci.com/technology/article/2012-11/video-largest-most-hi-res-cosmological-simulations-known-universe>

Vector Field Visualization

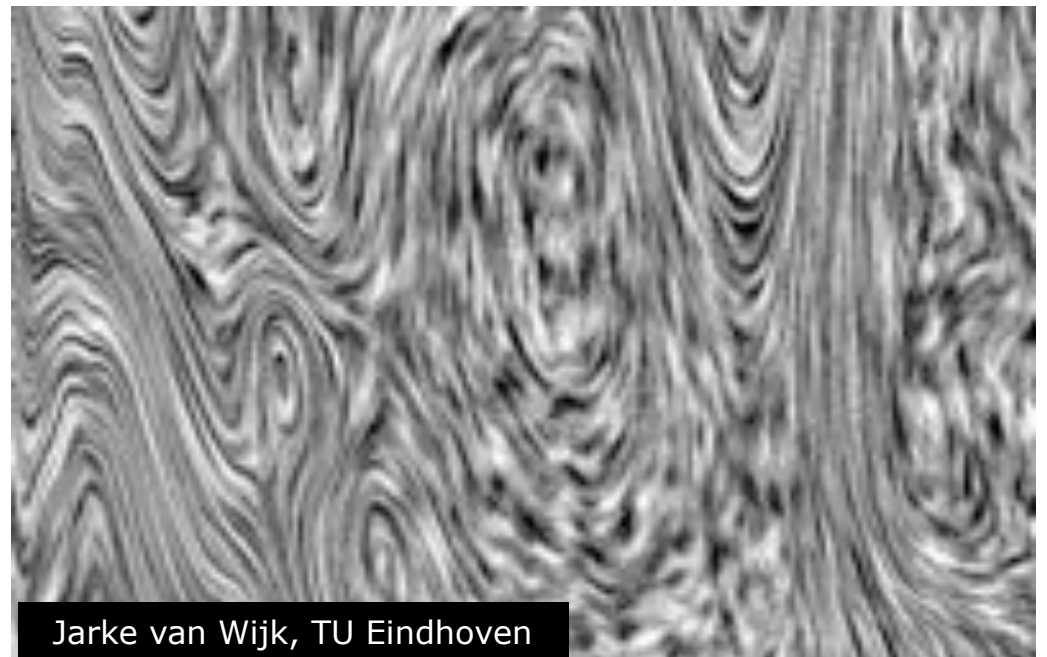


Experimental Fluid Dynamics

Visualization for understanding vortices, optimizing aerodynamics and turbine efficiency



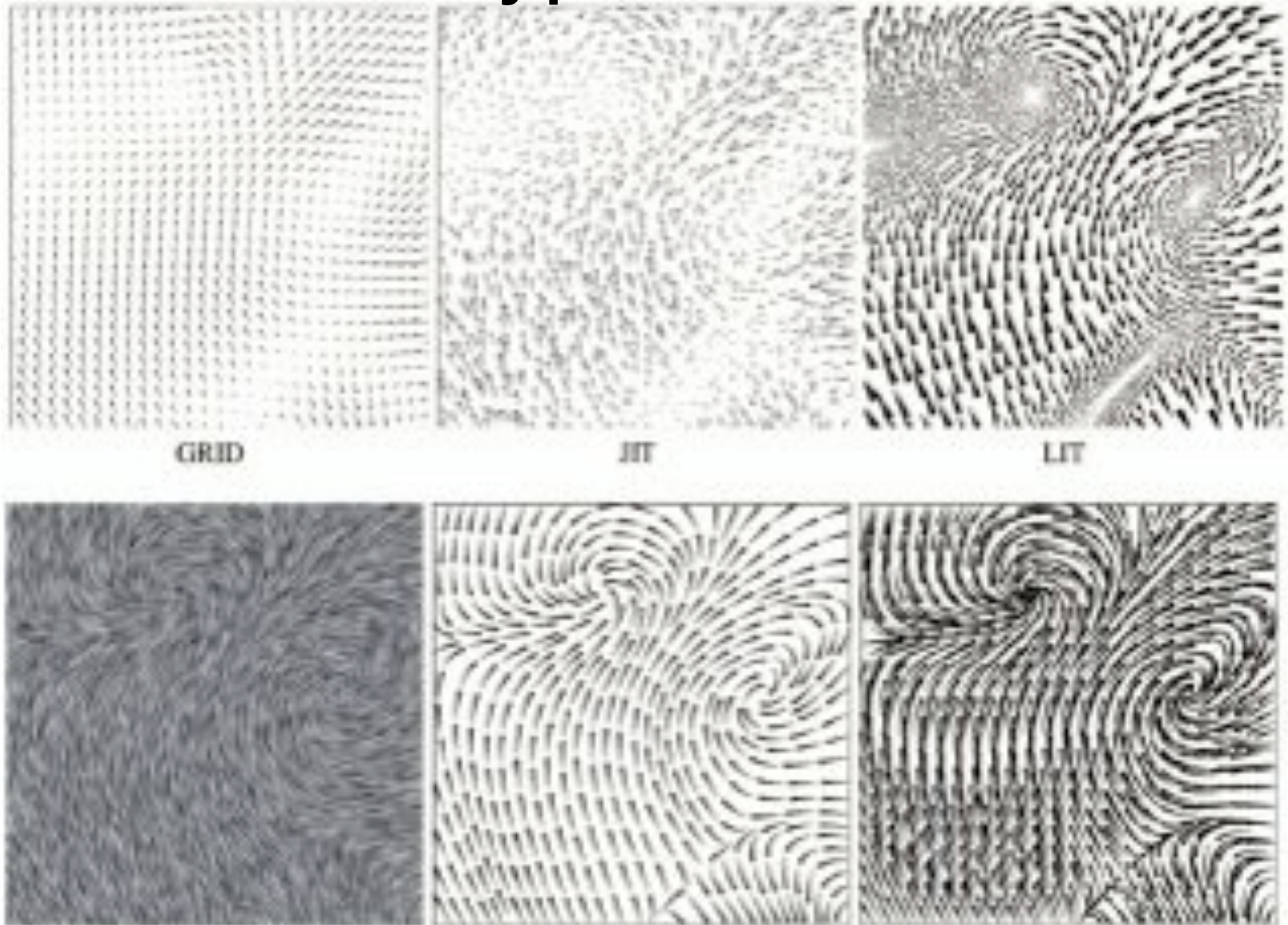
Roth and Peikert, ETH Zurich



Jarke van Wijk, TU Eindhoven

Flow visualization by Line Integral Convolution

Vector Field Glyphs

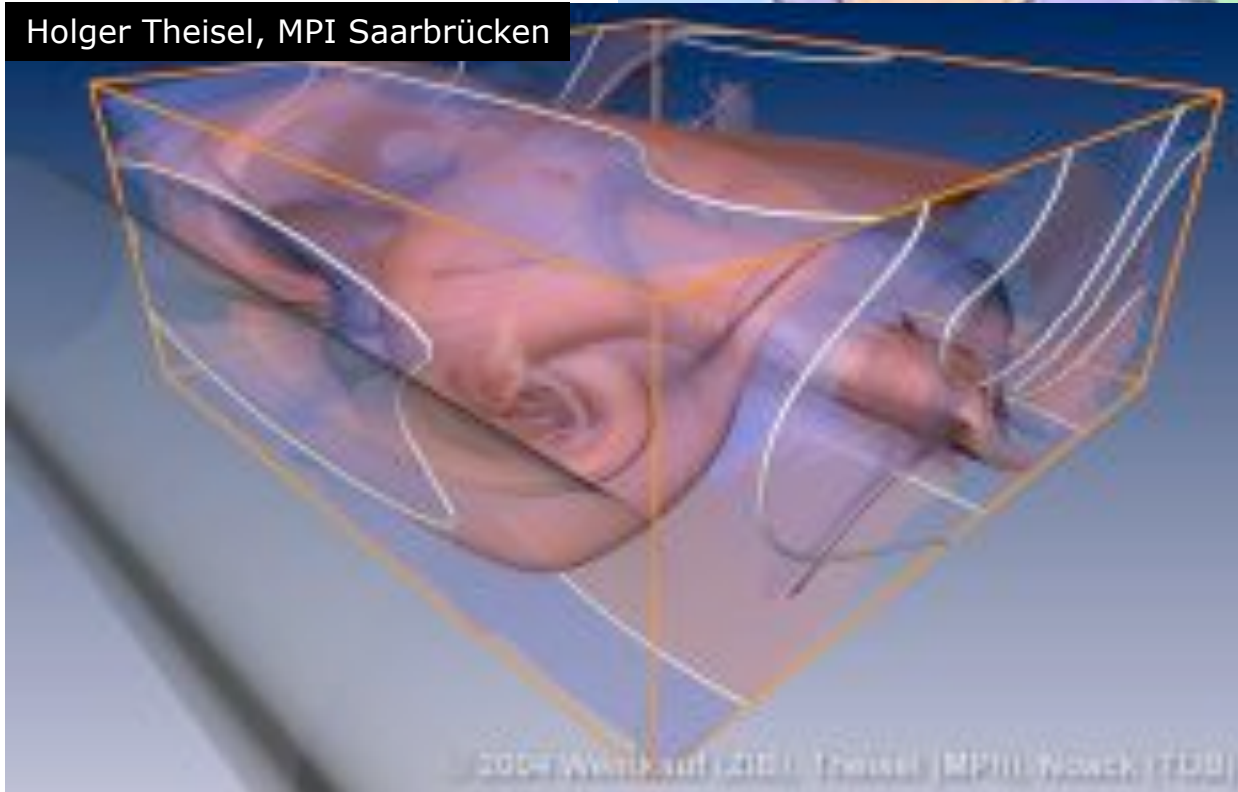


David H. Laidlaw, Robert M. Kirby, Cullen D. Jackson, J. Scott Davidson, Timothy S. Miller, Marco da Silva, William H. Warren, and Michael J. Tarr. **Comparing 2D Vector Field Visualization: Methods: A User Study**. Transactions on Visualization and Computer Graphics 11(1):59-70, 2005

Vector Field Topology ~ River basins



Holger Theisel, MPI Saarbrücken



<http://www.esrl.noaa.gov/psd/climateinfo/drought.html>

What do tensors describe?

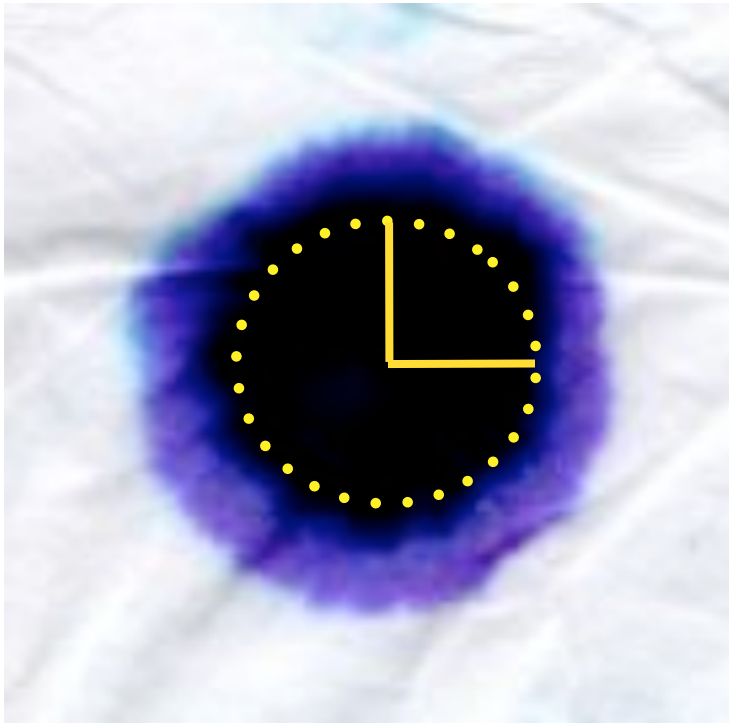
Anisotropy: (adj. anisotropic) how un-sphere-like

Related to the variance of the eigenvalues

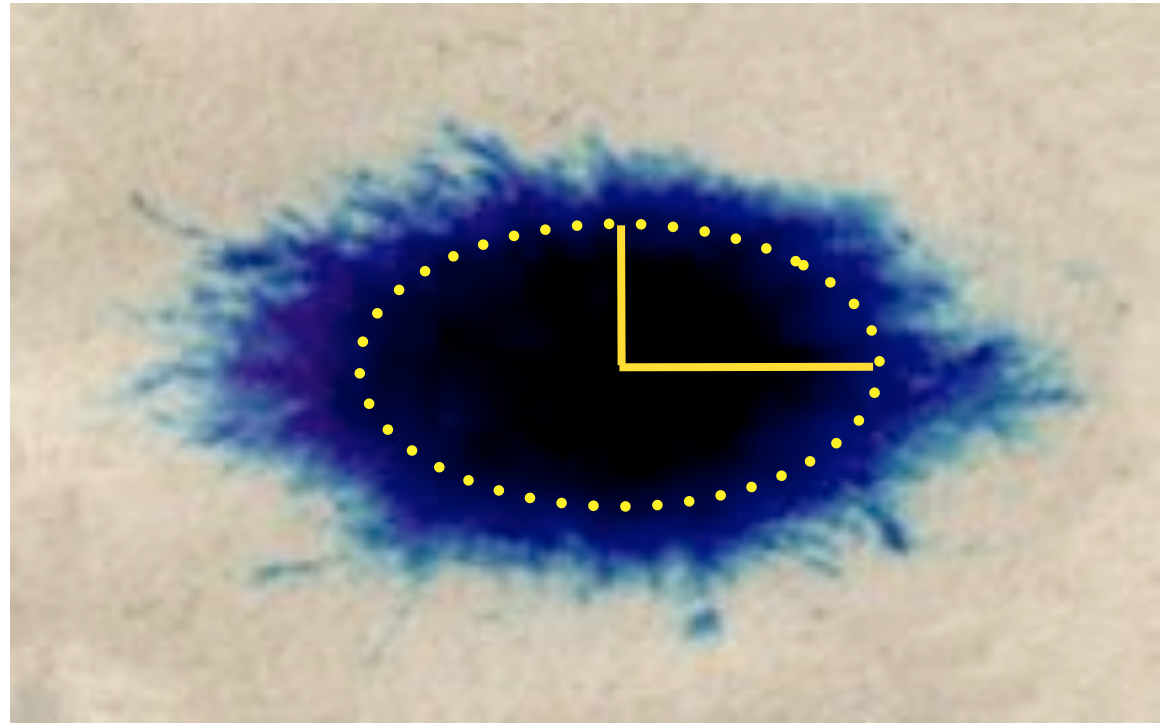
More generally: “different in different directions”

Isotropy (adj. isotropic) like a sphere, all eigenvalues equal

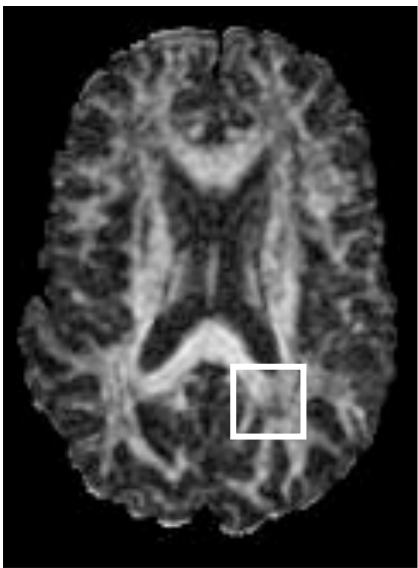
Anisotropy example: water diffusion in newspaper



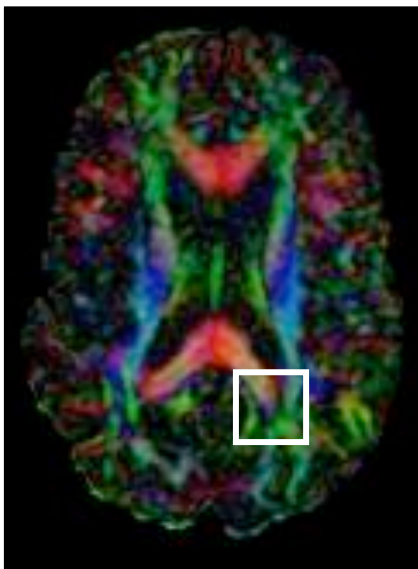
Kleenex: isotropic



Newspaper: anisotropic

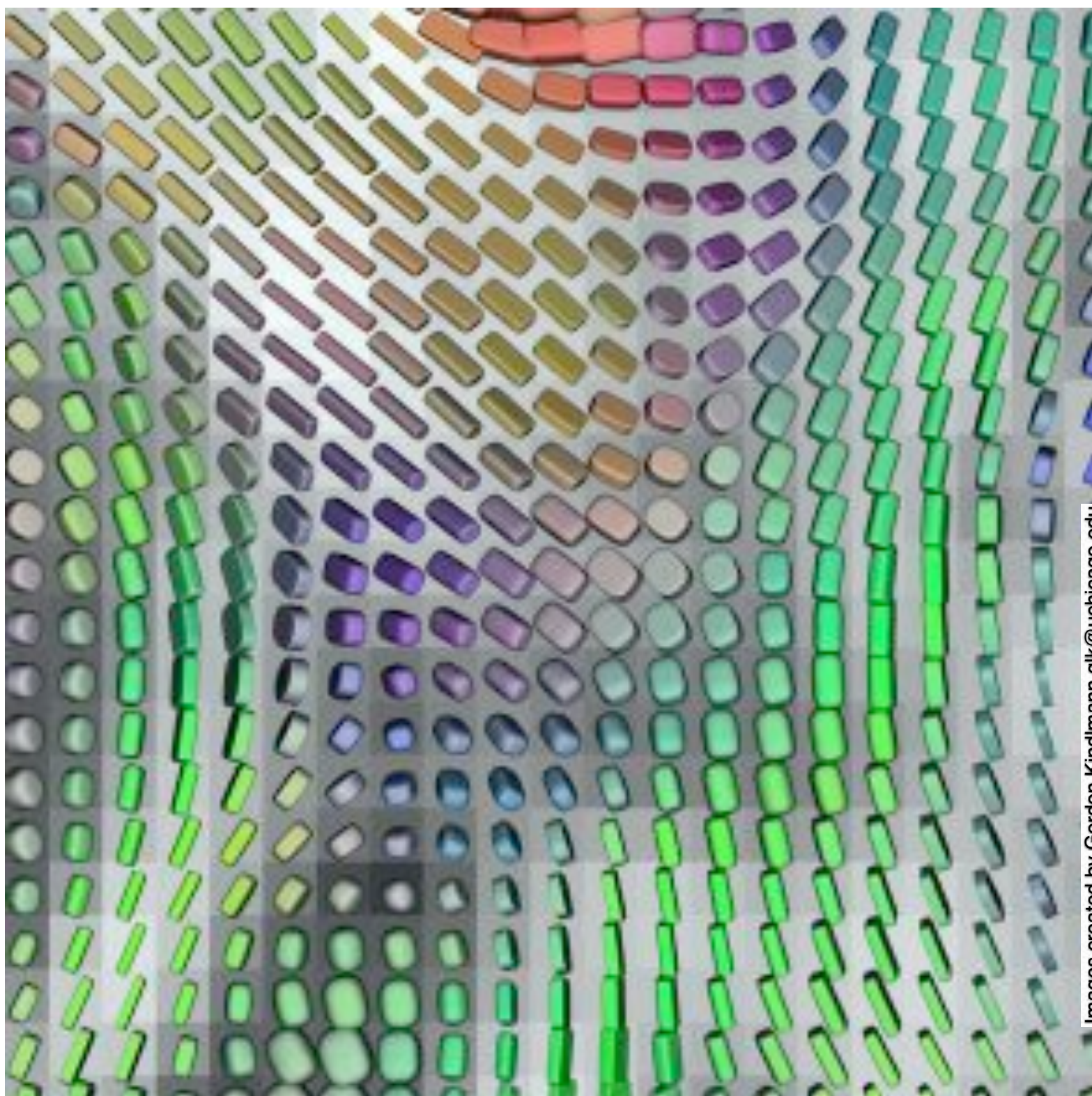


Grayscale: FA
Fractional Anisotropy

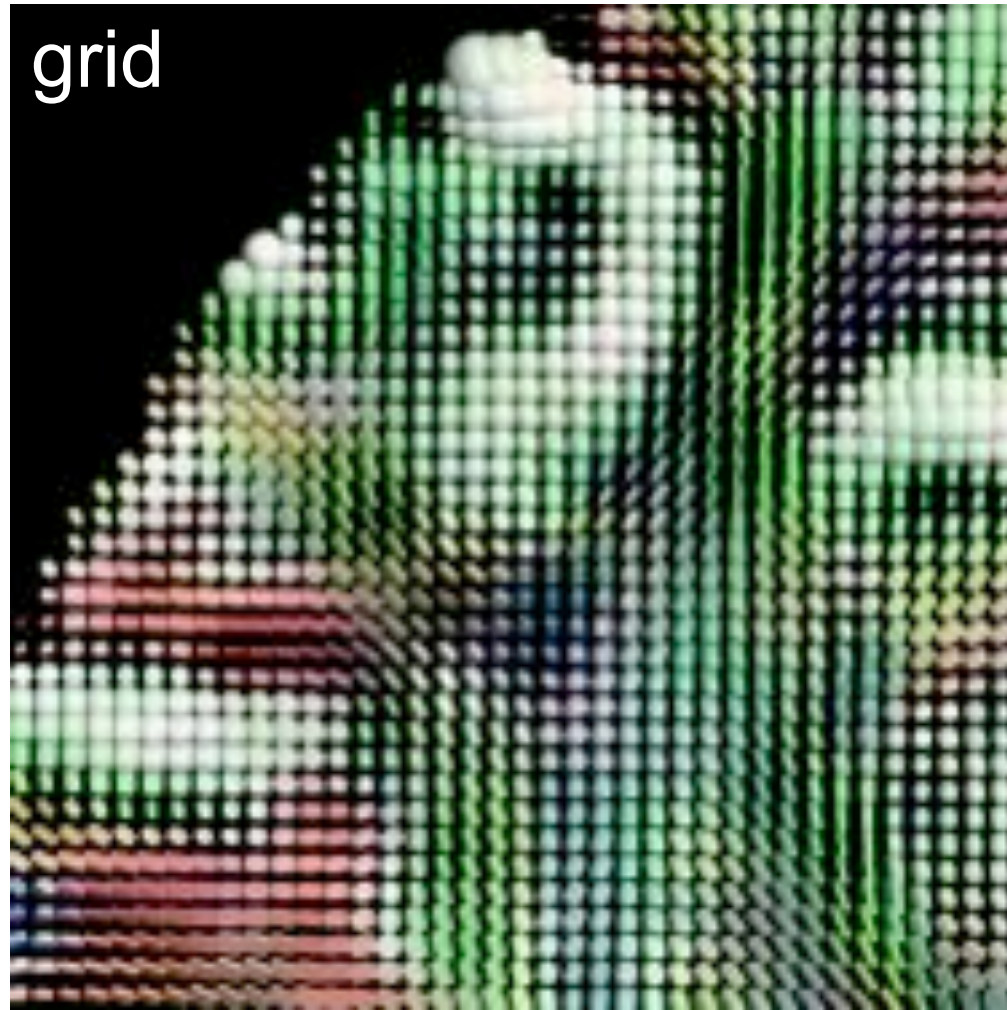


Color: RGB(v_1)
 v_1 principle eigenvector

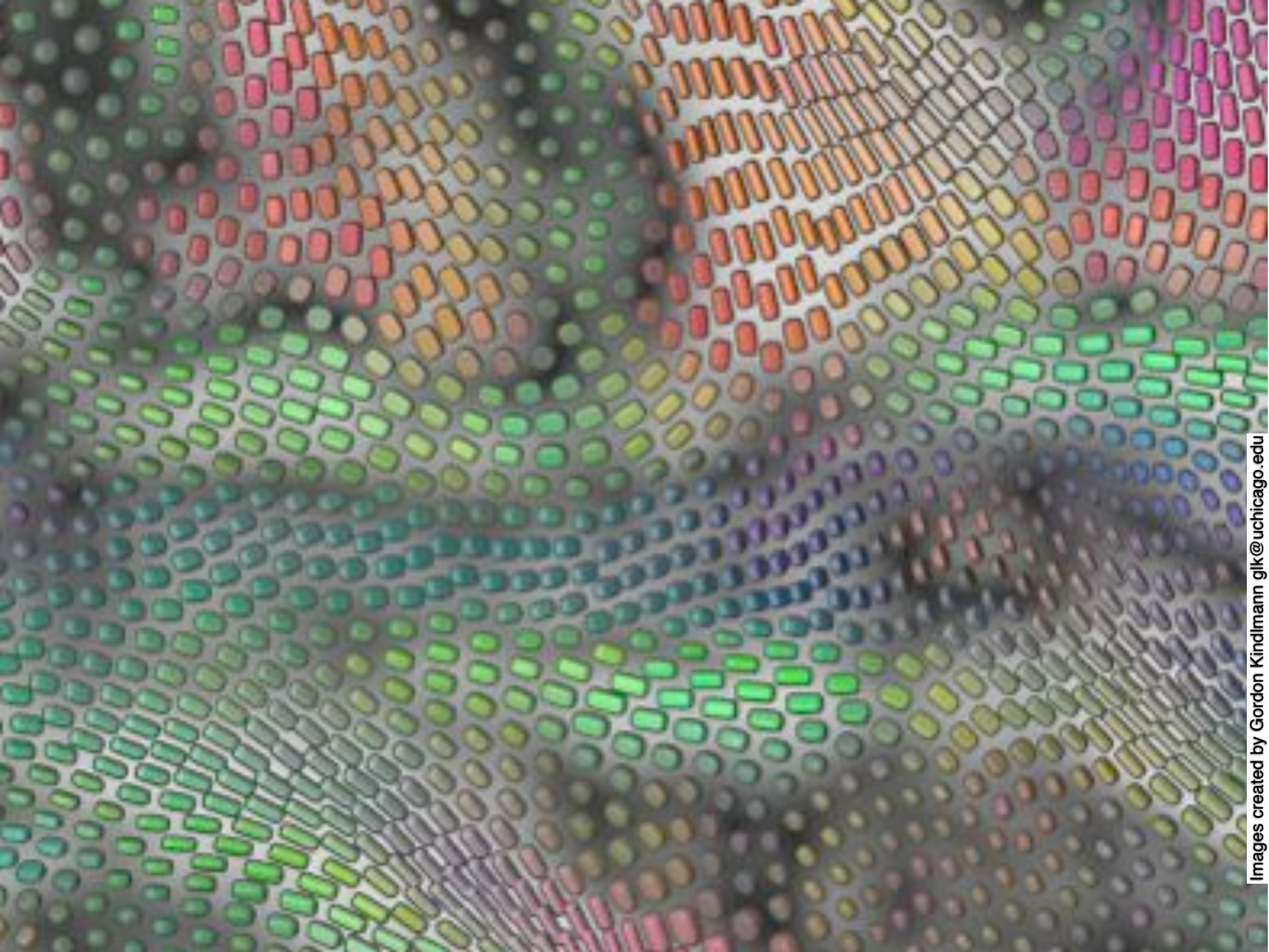
Glyphs: full diffusion
tensor \rightarrow



Can break free of rectangular grid



Gordon Kindlmann and Carl-Fredrik Westin. **Diffusion Tensor Visualization with Glyph Packing**. IEEE Trans. on Visualization and Computer Graphics, 12(5):1329-1335 2006



Uncertainty visualization

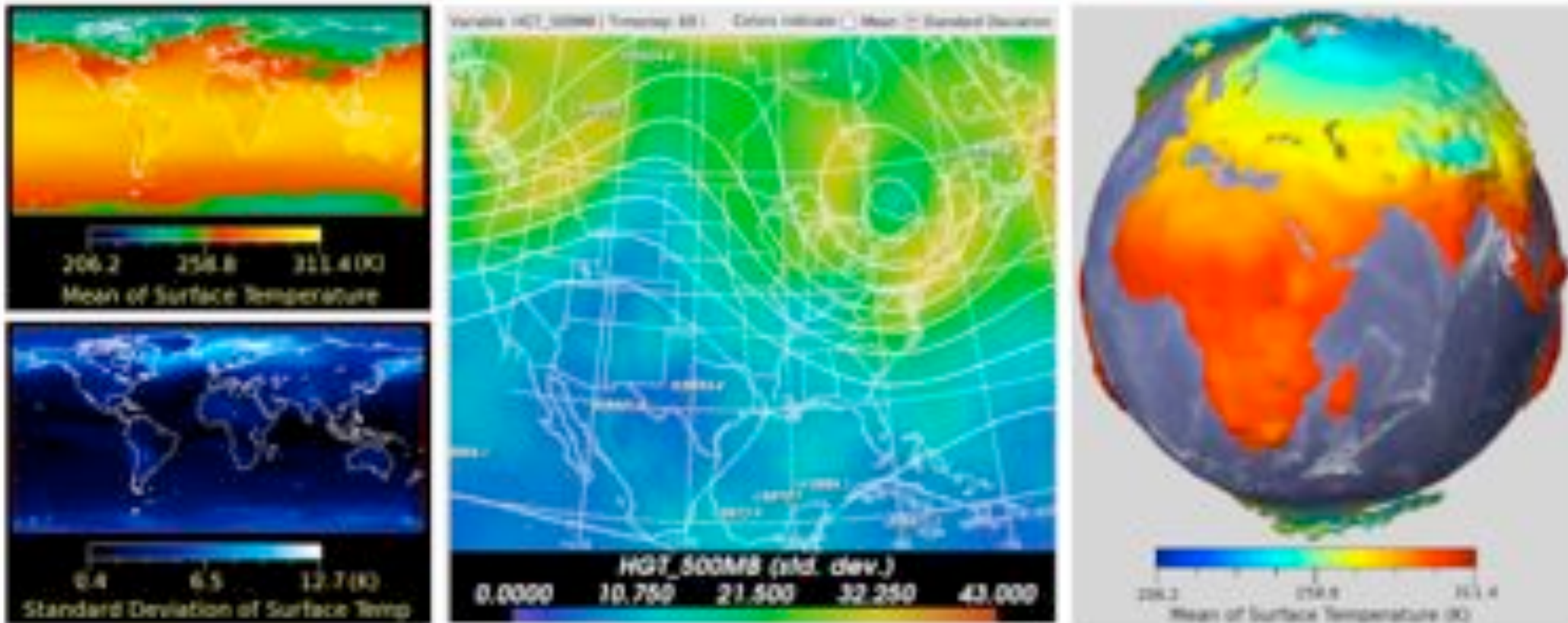


Figure 3. Visualizations of mean and standard deviation. (Left) Mean and standard deviation are visualized independently using color maps. (Center) Mean is presented through a color map, and standard deviation is shown as an overlaid contour. (Right) Standard deviation is mapped to a height field and mean is color mapped.

Fields of Visualization

Information
Visualization

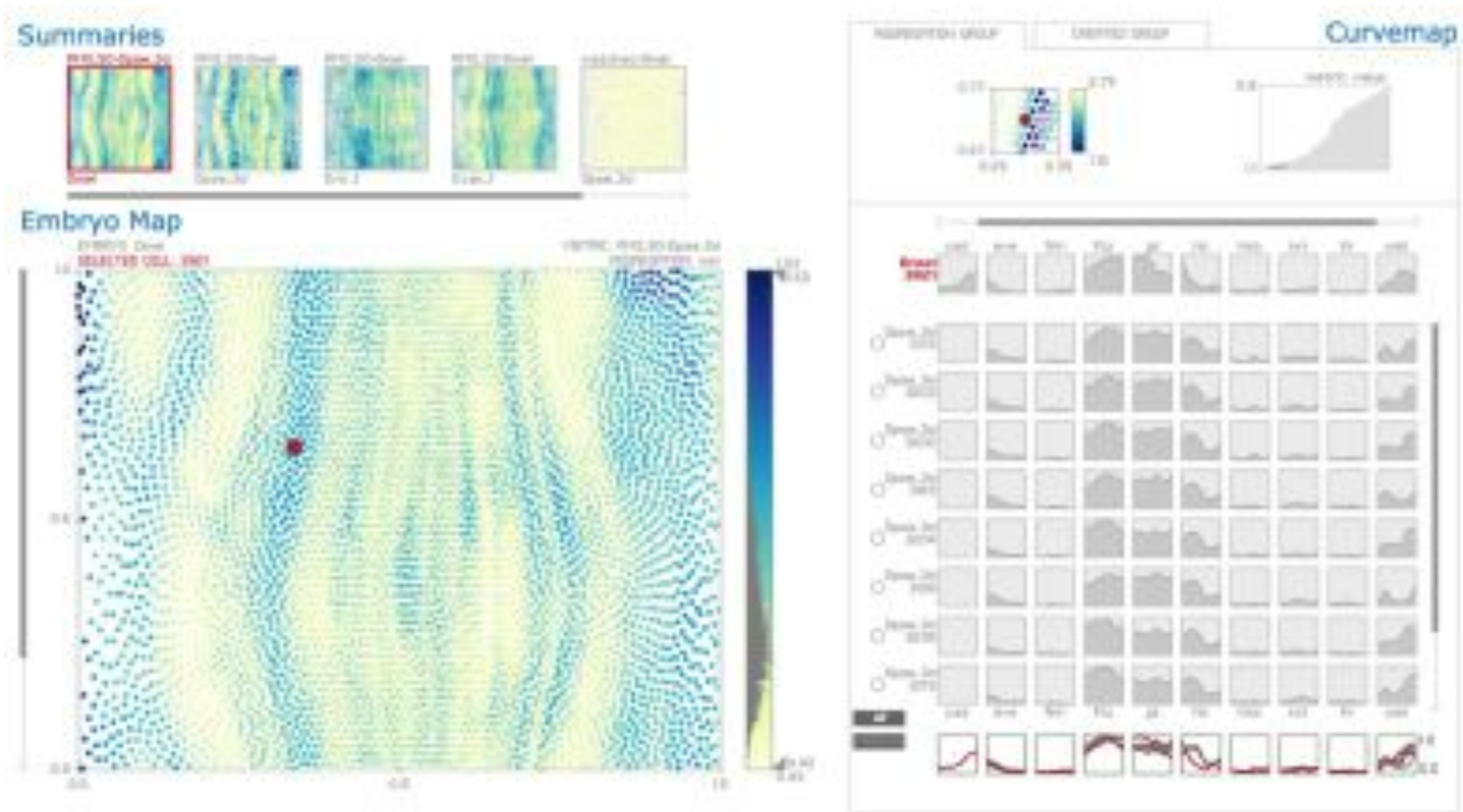
Scientific
Visualization

Data Visualization

Info-
graphics

Scientific
Illustration

Gene expression data



Miriah Meyer, Tamara Munzner, Angela DePace, Hanspeter Pfister. **MulteeSum: A Tool for Comparative Spatial and Temporal Gene Expression Data** IEEE Transactions on Visualization and Computer Graphics (Proc InfoVis 2010), 16(6):908-917, 2010.

Blood vessel visualization by straightening



Michelle A. Borkin, Krzysztof Z. Gajos, Amanda Peters, Dimitrios Mitsouras, Simone Melchionna, Frank J. Rybicki, Charles L. Feldman, and Hanspeter Pfister. **Evaluation of Artery Visualizations for Heart Disease Diagnosis**. Proc Transactions on Visualization and Computer Graphics 17(2): 2479-2488 2011

River straightening



Fields of Visualization

Information
Visualization

Scientific
Visualization

Data Visualization

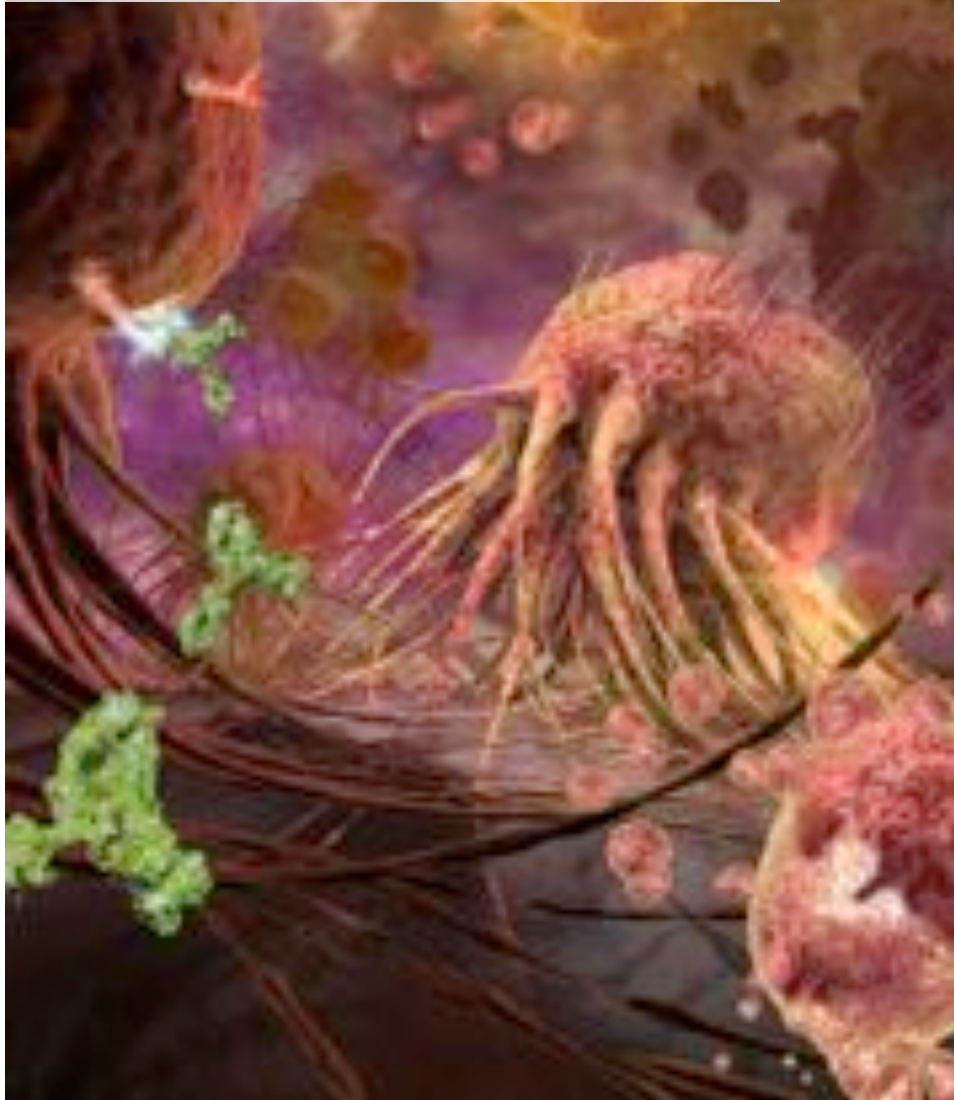
Info-
graphics

Scientific
Illustration

Scientific Illustration

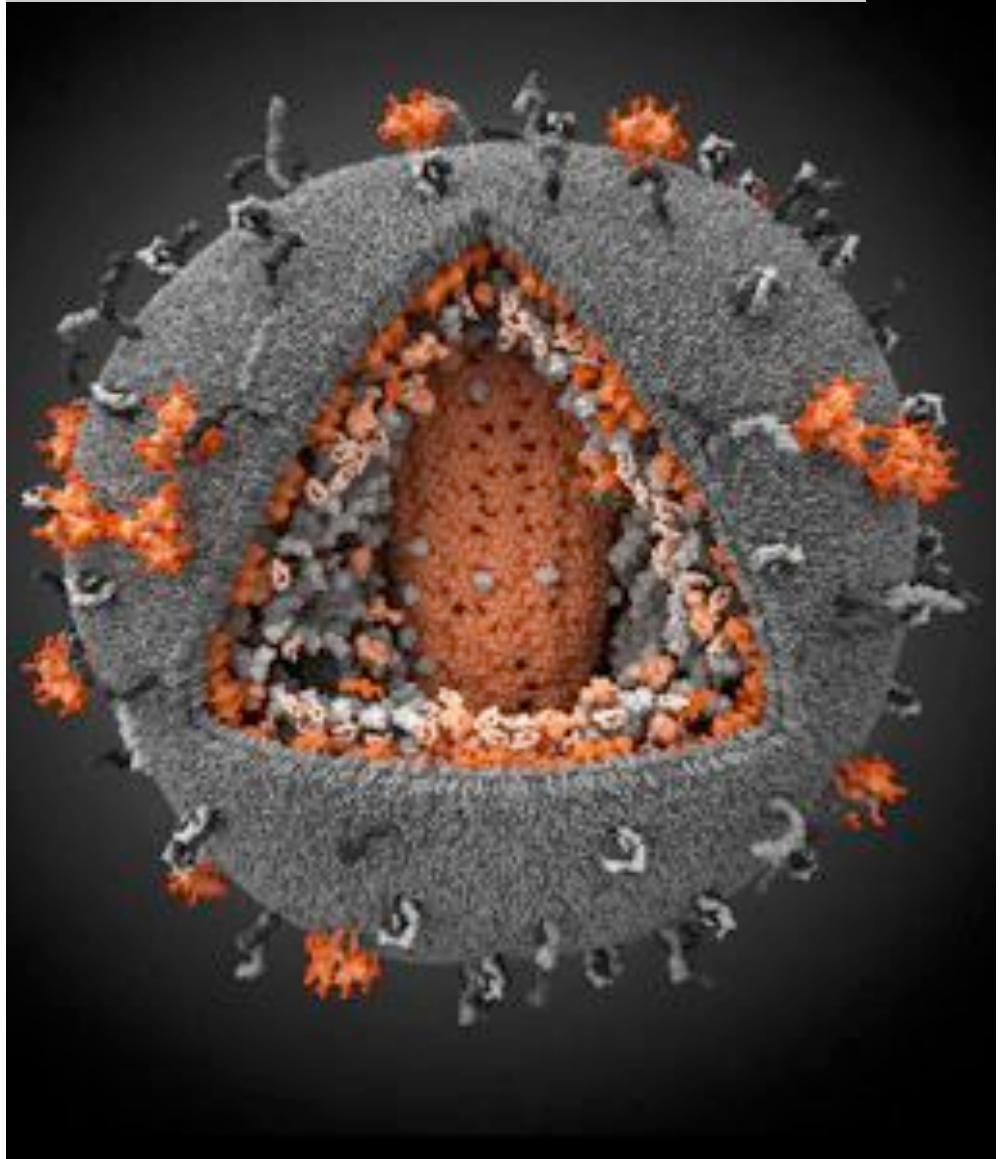
http://www.nsf.gov/news/special_reports/scivis/challenge.jsp

“Tumor Death-Cell Receptors on Breast Cancer Cell”



Emiko Paul, Quade Paul, Echo Medical Media;
Ron Gamble, UAB Insight

“Human Immunodeficiency Virus 3D”



Ivan Konstantinov, Yury Stefanov, Aleksander
Kovalevsky, Yegor Voronin, Visual Science Company

Information graphics

Which Fish are Okay to Eat?

YES: abundant, well-managed or caught in an environmentally-friendly way
 MAYBE: fish are flagged for concern, and may be better-caught
 NO: vulnerable or endangered species, caught or farmed in harmful ways

YES	Farmed	Atlantic	Atlantic/Pacific	Pacific
MAYBE				
NO				

Driving Shifts Into Reverse

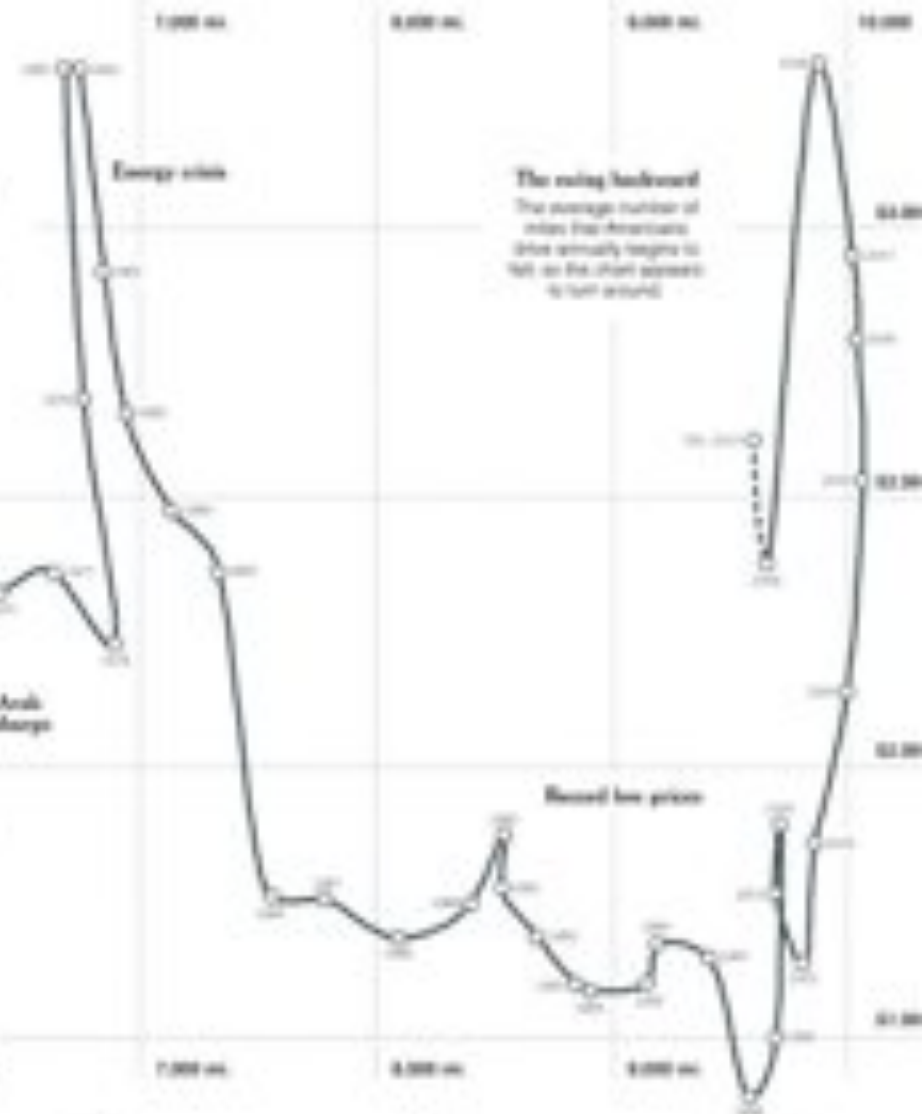
Economists have long predicted that rising energy prices would lead to a long period of profitable driving, and a world where prices are low and many factories in Europe and Japan.

And recently, Americans have driven more miles than in the previous year, with a few brief exceptions. In 2009, Americans drove 10.5 billion miles, about 1.5 billion more than in 2008. This year, that figure has climbed to 11.5 billion.

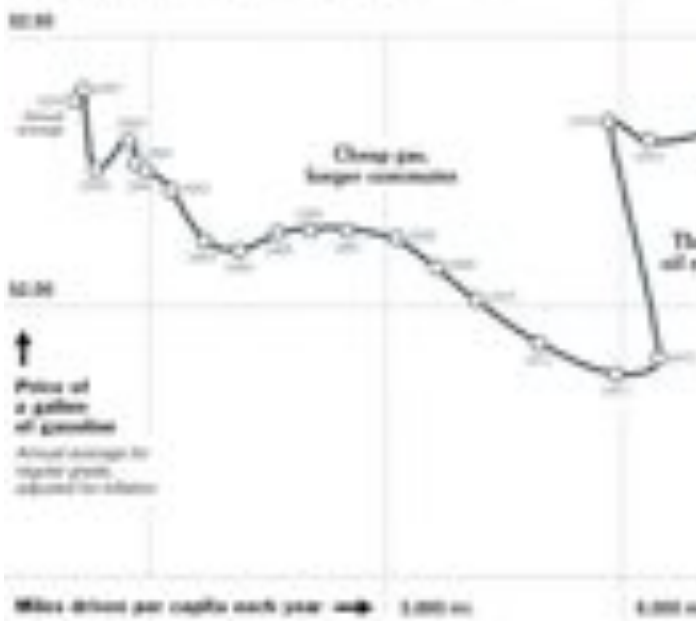
For the first time in 10 years, the number of miles driven has increased. The change is significant because it shows that more people were driving in 2010, and a sign of economic spending

more than ever before. It's a sign that the economy is recovering. As gasoline prices fell, the number of miles driven — including commercial and personal — began to rise, and continued to rise after 2009 even as gasoline prices changed.

"People were motivated by the very high cost of gas prices, and they changed their driving behavior," said Kenneth A. Froot, a transportation economist at the University of California, Irvine. "The one surprise is that it's temporary. As soon as gas prices go back to government levels, we will see Americans driving less than driving again."



The rising backward
The average number of miles that Americans drive annually began to fall as the oil prices went around.



↑ Price of a gallon of gasoline
Annual average for regular grade, adjusted for inflation

Miles driven per capita each year → 1,000 mi. 2,000 mi. 3,000 mi. 4,000 mi. 5,000 mi. 6,000 mi. 7,000 mi. 8,000 mi. 9,000 mi. 10,000 mi.

1970-74
Cheap gas keeps economies

Annual average for regular grade, adjusted for inflation

At 0.25, Americans spent more money on oil than in 1969. The price of a gallon of gasoline fell from 0.35 to 0.25.

1973-74
The Arab oil embargo

At 0.40, every Arab oil-producing country declared an oil embargo against the United States because of its support of Israel in the

1973-74
Energy crisis

Oil prices jumped as the United States and the Arab states entered a cold war. The price of a gallon of gasoline rose from 0.40 to 0.55.

1980-85
Round low prices

Gasoline prices fell for most of a decade, and the average number of miles Americans drive annually, peaked in 1980.

2008-10
The rising backward

The price of a gallon of gasoline rose from 0.70 to 1.40. The number of miles driven fell from 10.5 billion to 9.5 billion.

Explosion of “data science”

New job titles:

“data journalist”, “data designer”, “data scientist”

Many sites with pretty examples:

<http://flowingdata.com>

<http://fathom.info>

<http://www.visualizing.org>

<http://infosthetics.com>

<http://www.datapointed.net>

<http://visual.ly>

<http://weloveinfographics.info>

<http://www.coolinfographics.com>

<http://ilovecharts.tumblr.com>

Companies: <http://www.tableausoftware.com>

Competitions: <http://www.kaggle.com>

Fields of Visualization

Statistics,
Machine
Learning

Computer Science
Computer Graphics
Human-computer interaction
Perceptual Psychology

Calculus,
Numerical
Methods

Information
Visualization

Scientific
Visualization

Data Visualization

Info-
graphics

Scientific
Illustration

Frederik de Wit
“Novissima et
accuratissima
totius Americae
descriptio” (1670)
<http://maps.bpl.org/id/m8711>



World's Most Accurate Pie Chart



Thanks for your attention!